

# Theory of jets

Mrinal Dasgupta

University of Manchester

DESY, Hamburg, September 12, 2011

- Introduction and jet definitions
  - QCD perturbation theory and jets.
  - IRC safety and jet algorithms
  - IRC safe jet definitions for hadron colliders.
- Properties of jets
  - Perturbative properties
  - Non-perturbative contributions (hadronisation, UE, pile up)
- Using jets at hadron colliders
  - Optimal  $R$  and new physics
  - Substructure and jet grooming
- Summary and outlook

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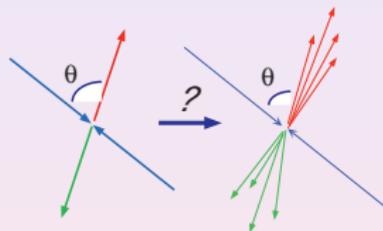
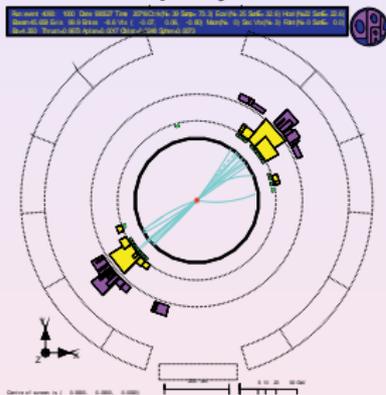
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# pQCD and jets

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QCD is a weird theory. Lagrangian involves **partons** which never make it to detectors. Measured final state involves collimated sprays of hadrons or **jets**.



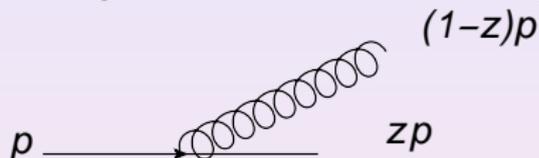
Luckily partons leave some footprints. The game of jet physics involves identifying those elusive partons.

Sterman TASI lectures

# Need for jets

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Need for jets arises from within the theory. Regulate IR divergences to make meaningful predictions in pQCD.

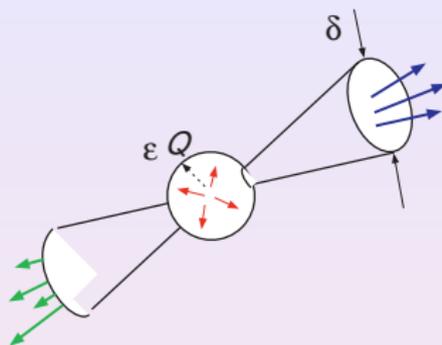


$$P = C_i \int \frac{\alpha_s((1-z)\theta)}{\pi} \frac{dz}{1-z} \frac{d\theta^2}{\theta^2}$$

Probability for extra particle production diverges in PT. For calcs. need to introduce energy and angular resolution.

# Early jet definitions

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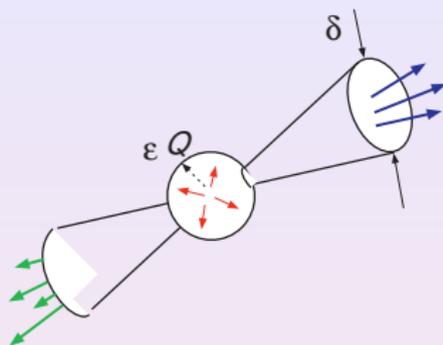


Define a dijet event by including anything below energy  $\epsilon$  or within angle  $\delta$  in dijet. **Sterman and Weinberg 1978**

Probability of particle production can be  $\mathcal{O}(1)$ . Probability of producing **extra jet** costs us  $\alpha_s$ . Jet cross-sections computable in pQCD. But we need IRC safe jet definition at **all orders**.

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SW algorithm too basic. Where to place cones? What to do with overlapping cones? How to generalise to hadron collisions? More sophisticated cones were devised.

Snowmass accord developed laying out properties of an acceptable algorithm:

- Simple to implement in experimental analyses as well as theory calculations.
- Defined at any order in pQCD and yields **finite** results for rates at any order.
- Yields a cross-section relatively insensitive to hadronisation

ESW "More honoured in the breach than the observance!"

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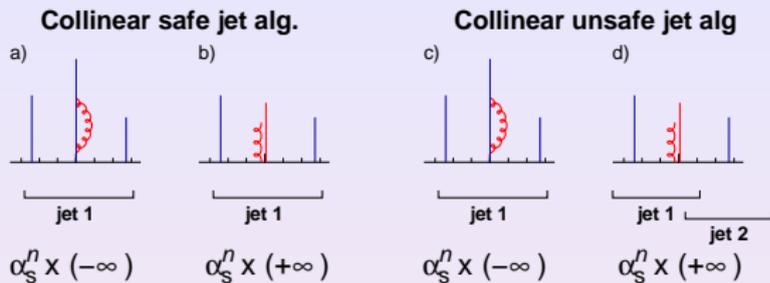
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# Long history of problems

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**Infinites cancel**

**Infinites do not cancel**

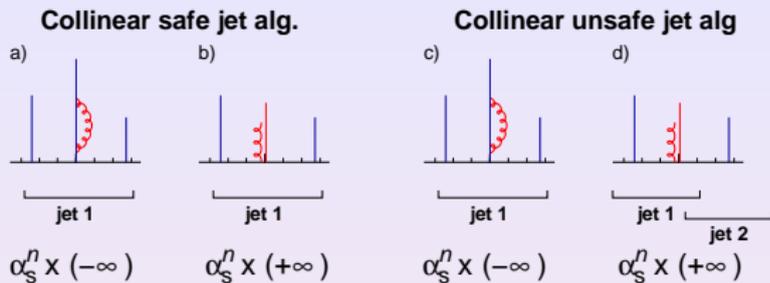
Seeded cone -

emission of a collinear parton changes the jet structure and leads to a **divergence**.

- Cone algorithms have been problematic including **all** the cones used at the Tevatron to date.
- There are also algorithms based on sequential recombination. These are IRC safe but have in the past not been commonly used at hadron colliders.
- Finally we have a set of algorithms of various kinds all of which satisfy Snowmass.

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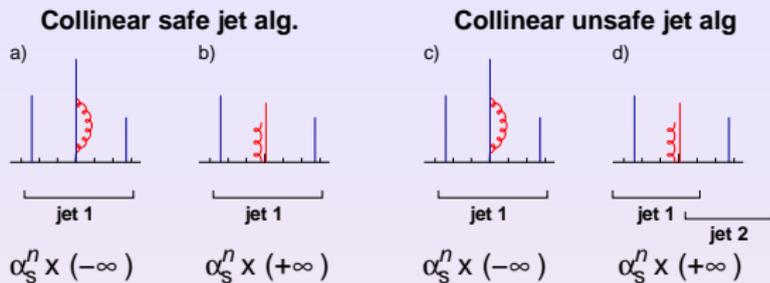
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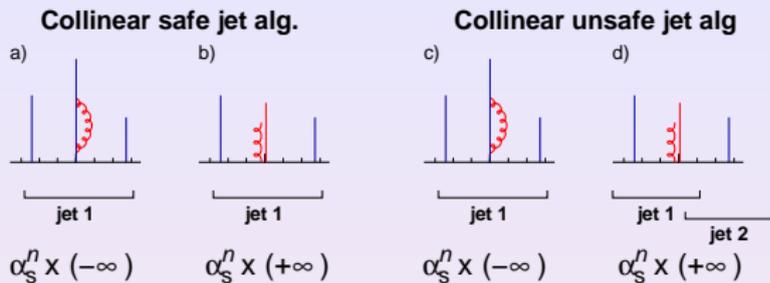
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# IRC safe hadron collider jet definitions

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- 1 Cone type : SISCONe (Seedless Infrared Safe Cone)  
Salam and Soyez 2007
- 2 Sequential Recombination based on a distance measure.
  - $k_t$  or Durham algorithm  
Catani et. al 1993, Ellis et. al 1993
  - Cambridge-Aachen  
Dokshitzer et. al 1997, Wobisch and Wengler 1998
  - Anti- $k_t$   
Cacciari, Salam, Soyez 2008.

# Sequential recombination algorithms

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Most common is inclusive  $k_t$  algorithm with distance measures

$$d_{ij} = \min(p_{t,i}^2, p_{t,j}^2) \frac{\Delta_{ij}}{R^2}, \quad \Delta_{ij} = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$
$$d_{iB} = p_{t,i}^2$$

Ellis and Soper 1993

All quantities defined wrt beam. Radius like parameter  $R$ .

- Find the smallest among  $d_{ij}$  and  $d_{iB}$ . If it is a  $d_{iB}$  call the object a jet and remove from list. If  $d_{ij}$  then merge  $i$  and  $j$ .
- Repeat until all particles are removed.

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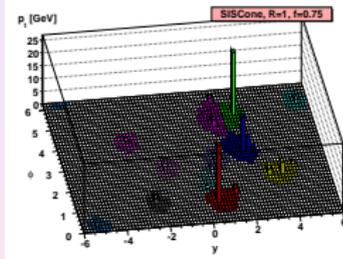
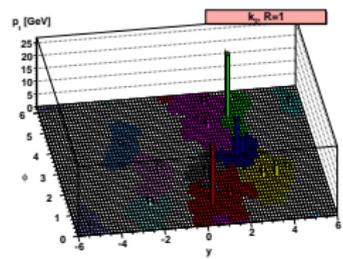
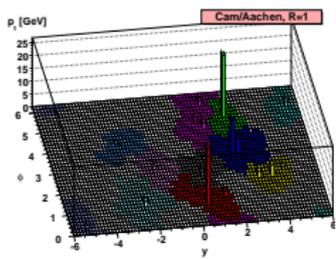
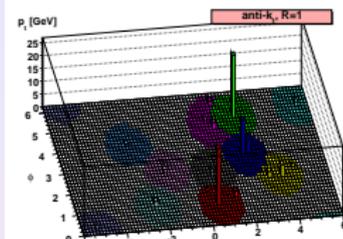
Belong to the  $k_t$  family with

$$d_{ij} = \min(p_{t,i}^{2p}, p_{t,j}^{2p}) \frac{\Delta_{ij}}{R^2}$$

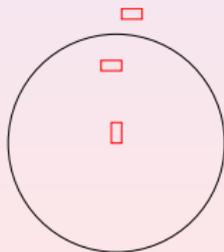
$p = 0$  is C/A algorithm while  $p = -1$  is the **anti- $k_t$**  algorithm. Note that C/A algorithm inverts **angular ordered shower** while anti- $k_t$  not closely related to QCD dynamics.

# Appearance of hadron collider jets

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Salam "Towards Jetography" 2009



# Properties of jets at hadron colliders

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$$\langle \delta p_t \rangle_q = -\frac{C_F \alpha_s}{2\pi} p_t \int_{R^2}^1 \frac{d\theta^2}{\theta^2} \frac{1+z^2}{1-z} \min[(1-z), z]$$

$$\langle \delta p_t \rangle_q = -C_F \frac{\alpha_s}{\pi} p_t \ln \frac{1}{R} \left( 2 \ln 2 - \frac{3}{8} \right)$$

$$\langle \delta p_t \rangle_g = -\frac{\alpha_s}{\pi} p_t \ln \frac{1}{R} \left[ C_A \left( 2 \ln 2 - \frac{43}{96} \right) + T_R n_f \frac{7}{48} \right]$$

MD, Magnea and Salam 2008



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To summarise:

$$\frac{\langle \delta p_t \rangle_q}{p_t} = -0.43 \alpha_s \ln \frac{1}{R}$$

$$\frac{\langle \delta p_t \rangle_g}{p_t} = -1.02 \alpha_s \ln \frac{1}{R}$$

For  $R = 0.4$  quark jet will have 5 percent less and gluon jet 11 percent less  $p_t$  than parent parton.

- Above results are subject to significant finite  $R$  and higher order changes.
- SISCONe has different recombination. Draw cone centred on  $p_1 + p_2$  and require one parton to fall outside it. Similar result with  $R_{kt} \sim 1.3 R_{\text{SIS}}$

MD, Magnea and Salam 2008

- Mean values

$$\langle M_j^2 \rangle_q \sim 0.16 \alpha_s R^2 P_t^2$$

$$\langle M_j^2 \rangle_g \sim 0.37 \alpha_s R^2 P_t^2$$

SISCONE results similar with  $R_{\text{SISCONE}} = 0.75R$ .

- Jet mass distribution Potentially significant logarithmic enhancements:

$$\frac{d\sigma}{dM^2} \sim \frac{\alpha_s}{M^2} \ln \frac{R^2 P_t^2}{M^2}.$$

Resummation? S.D. Ellis et.al 2010, Banfi, MD, Marzani, Khelifa Kerfa 2010

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# NP corrections - hadronisation

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Analytical calculations of hadronisation? Use Dokshitzer Webber model:

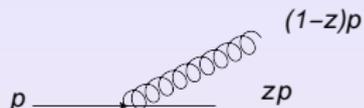
- Emit a soft **gluer** (a gluon that actually glues!) with  $k_t \sim \Lambda$ .
- Consider the change in jet energy  $-(1-z)p_t = -\frac{k_t}{\theta}$ .
- Apply the emission probability to compute the average

$$\langle \delta p_t \rangle_q = -C_F \int \frac{\alpha_s(k_t)}{\pi} \frac{dk_t}{k_t} \frac{d\theta^2}{\theta^2} \frac{k_t}{\theta}$$

for  $\theta > R$

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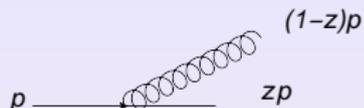
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for  $\theta > R$

We have

$$\langle \delta p_t \rangle_q = -\frac{2C_F}{\pi} \int_0^{\mu_I} \alpha_s(k_t) dk_t \times \frac{1}{R}$$

Take coupling integral from  $e^+e^-$  event shapes to get

$$\langle \delta p_t \rangle_q = \frac{-0.5\text{GeV}}{R}$$

For gluon jets change  $C_F \rightarrow C_A$ .

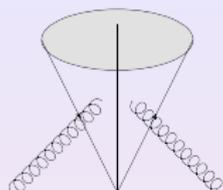
$$\langle \delta p_t \rangle_g = -\frac{1\text{GeV}}{R}$$

Striking singular dependence of hadronisation on  $R$ . Same for all algorithms!

MD, Magnea and Salam 2008

# UE contribution

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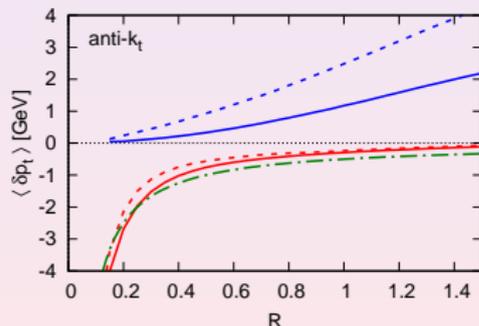
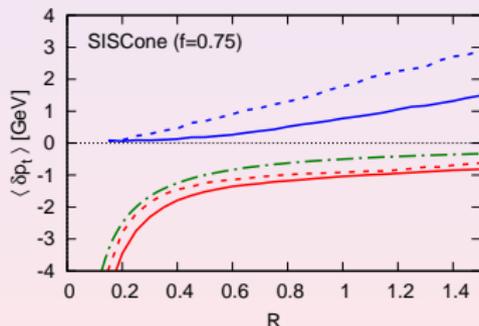
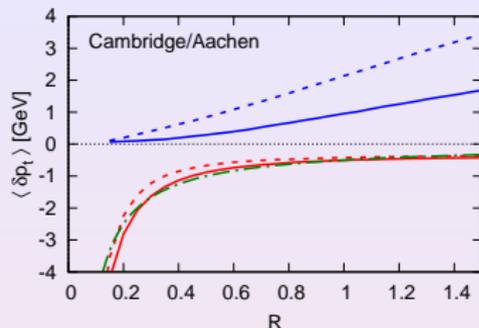
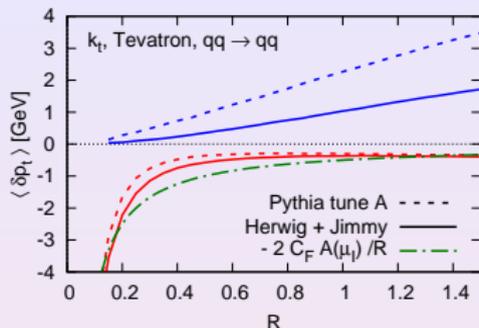
Contrast with underlying event contribution. Assume  $\Lambda_{\text{UE}}$  is energy per unit rapidity of soft UE particles.

$$\langle \delta p_t \rangle_{\text{UE}} = \Lambda_{\text{UE}} \int_{\eta^2 + \phi^2 < R^2} d\eta \frac{d\phi}{2\pi} = \Lambda_{\text{UE}} \frac{R^2}{2}$$

Has a regular dependence on  $R$  (comes from jet area). For jet mass UE contribution goes as  $R^4$ . Similar effects from pile-up but order of magnitude larger at the LHC.

# Comparison to MC models

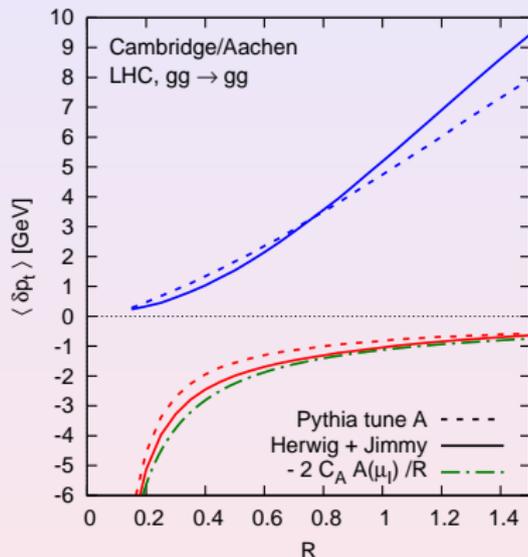
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Agreement with analytical predictions. Same result for all algorithms. UE different between MC models.

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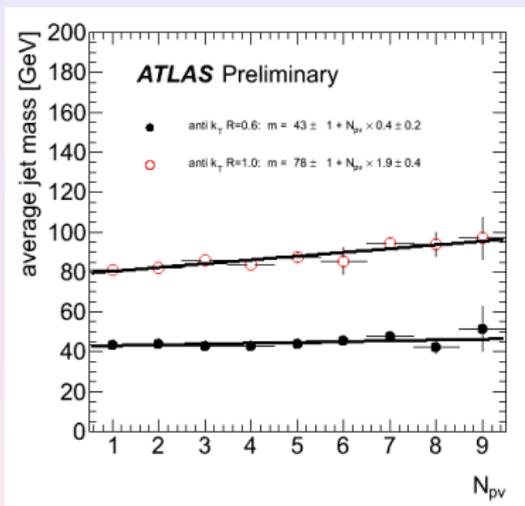
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At LHC underlying event is a large effect.

# Applications - comparison to data

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Ratio of slopes  $R = 4.58 \sim (1.0/0.6)^3$

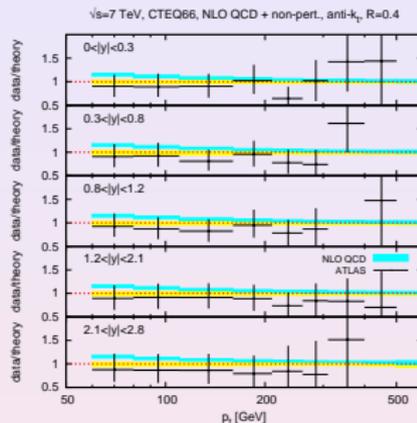
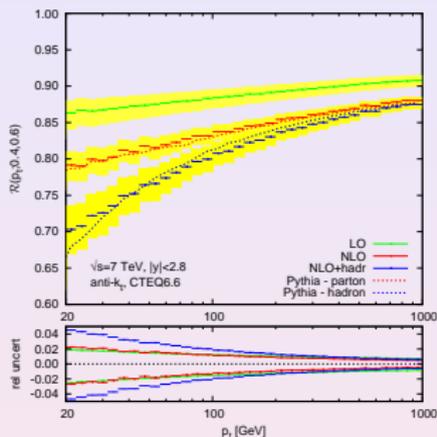
The  $R^3$  scaling is because

$$\delta m = \sqrt{m^2 + \delta m^2} - m \approx \frac{\delta m^2}{2m}.$$

Since  $\delta m^2$  scales as  $R^4$  and  $m$  as  $R$  ( $43/78 \approx 0.55$ ) one gets an  $R^3$  behaviour.

# Applications-Comparison to data

Mrinal Dasgupta

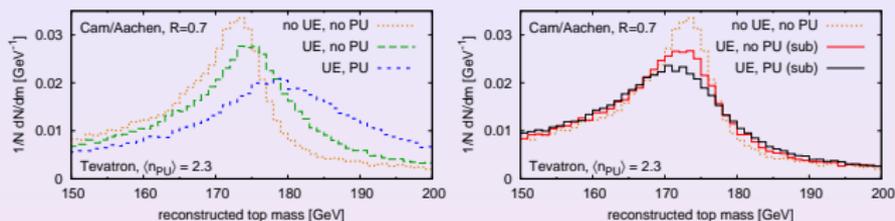


$$R = \frac{\frac{d\sigma}{dp_t}(R_1)}{\frac{d\sigma}{dp_t}(R_2)}$$

Soyez 2010

# Applications - pile up subtraction

Mrinal Dasgupta



Removal of pile-up crucial to quality of kinematic reconstructions.

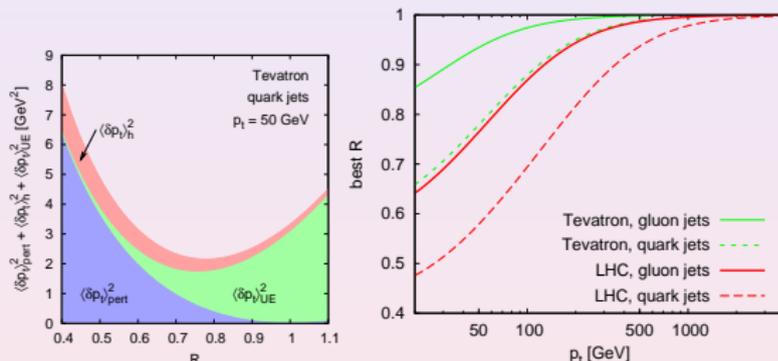
$$p_{t,j} \rightarrow p_{t,j} - \rho A_j$$

Area dependence of UE and pile up behind FASTJET subtraction of UE and pile up. Event by event determination of pile-up with jet-by-jet subtraction based on area.

Cacciari and Salam 2007

Knowing  $R$  dependence gives rise to concept of optimal  $R$  values. Based on minimising

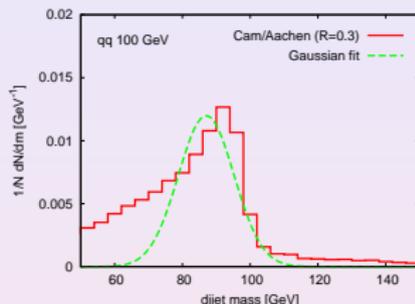
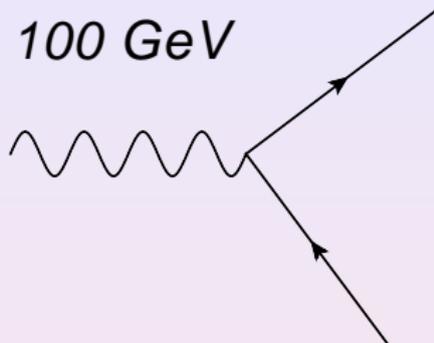
$$\langle \delta p_t^2 \rangle = \langle \delta p_t \rangle_h^2 + \langle \delta p_t \rangle_{UE}^2 + \langle \delta p_t \rangle_{PT}^2$$



At high  $p_t$  one should use a larger  $R$  - minimises perturbative effect. Likewise for gluon jets a larger  $R$  is suggested. For LHC smaller  $R$  values than Tevatron.

# Best $R$ for peak reconstruction

Mrinal Dasgupta

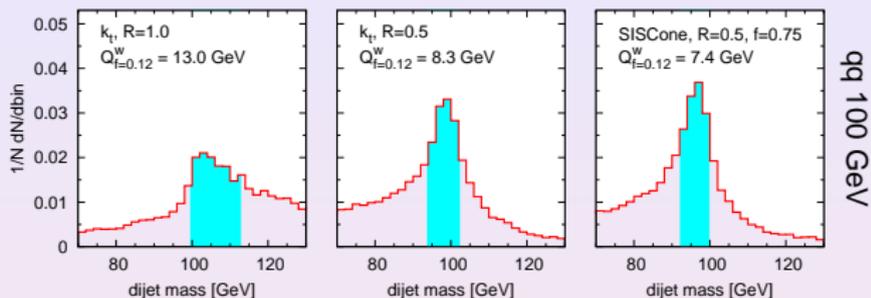


Can illustrate effect of finding best  $R$  on quality of kinematic reconstruction.

One can take a 100 GeV  $q\bar{q}$  resonance to illustrate this.

Need to define a measure of the quality of reconstruction.

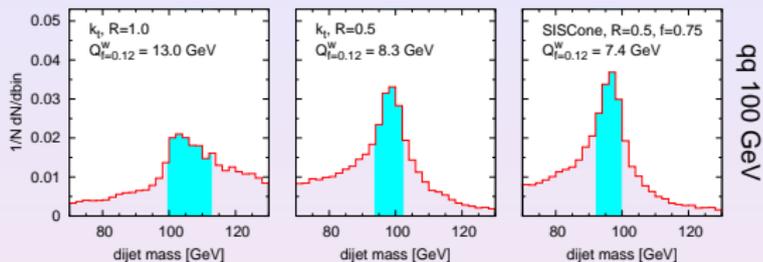
How to assess e.g peak width?



qq 100 GeV

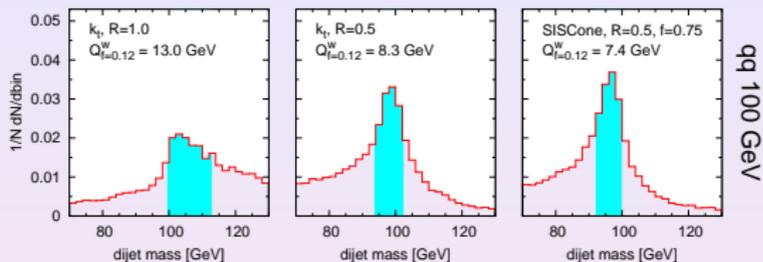
Define quality measure  $Q_{f=z}^w$  as the **width of the narrowest window which contains a specified fraction  $f = z$  of events**. Smaller  $Q$  corresponds to a better peak.

Salam, 2009



Compare different algorithms and choices of  $R$ .

For  $k_t$  algorithm a lower  $R$  value is favoured here suggesting the importance of the UE contribution. What may we expect when we move to a  $2 \text{ TeV}$   $g\bar{g}$  resonance? We learnt that at such high  $p_t$  and for gluon jets one should favour a larger  $R$ .

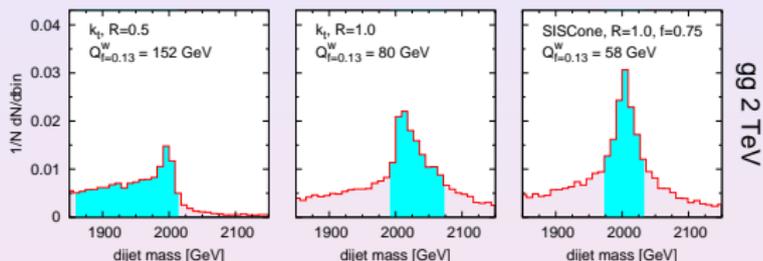


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# 2 TeV gg resonance

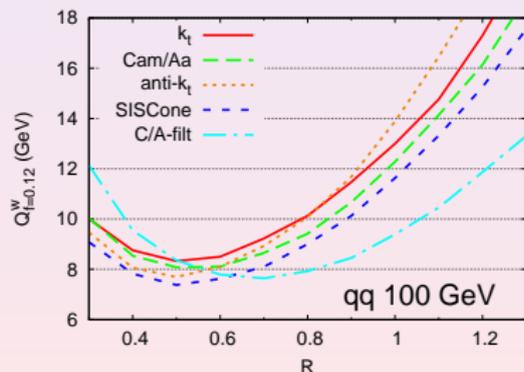
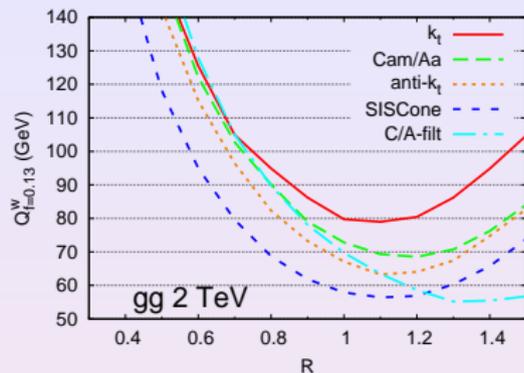
Mrinal Dasgupta



Here  $R = 0.5$  would be a bad choice. Larger  $R$  is favoured as expected. SISCONE seems to perform markedly better than  $k_t$  in this case.

# Comparing algorithms

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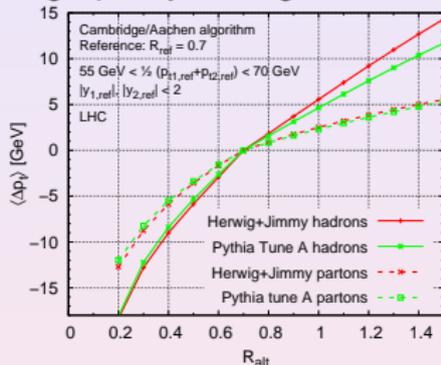


Optimal  $R$  doesn't vary too much across algorithms.  $Q$  does even for optimal  $R$ .

# Applications-new observables

Mrinal Dasgupta

Already seen some applications to data. One further idea could be to directly extract the scale of UE from data. Study e.g  $\delta p_t$  by using a reference and alternative jet



$$\langle \delta p_t \rangle = \langle \delta p_t \rangle_{\text{NLO}} - 2 \langle C_i \rangle \left( \frac{1}{R_{alt}} - \frac{1}{R_{ref}} \right) \mathcal{A}(\mu_f) + (R_{alt} \mathcal{J}_1(R_{alt}) - R_{ref} \mathcal{J}_1(R_{ref})) \Lambda_{\text{UE}}$$

# Applications -boosted objects and substructure

Mrinal  
Dasgupta

Highly boosted objects such as high  $p_T$  Higgs decay to products which have **narrow opening angle**. Can end up in single jet.

Recall

$$M^2 = z(1 - z)p_t^2\theta_{12}^2$$

For  $R \geq \frac{M}{\sqrt{z(1-z)}p_t}$  we will get a single jet. For  $p_t \sim 500$  GeV,  $M \sim 100$  GeV  $R \geq 0.6$  implies that 75 percent of such decays will be clustered to a jet.

# Jet substructure

Mrinal  
Dasgupta

Invariant mass distribution is first clue to identity of jet.  
Significant issue arises of QCD jet backgrounds.

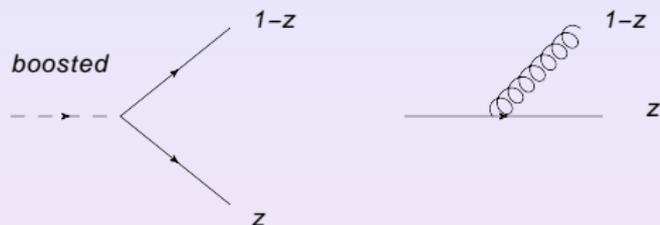
$$\frac{1}{\sigma} \frac{d\sigma}{dM^2} \sim \frac{1}{M^2} \alpha_s \ln \frac{R^2 p_t^2}{M^2}$$

For  $p_t \gg M$  this can be significant contamination even at masses of a 100 GeV.

Remove QCD background and optimise the construction of the mass.

# Substructure techniques

Mrinal Dasgupta



To distinguish jets from QCD from those from heavy particle decays it pays to **look at jet substructure**.

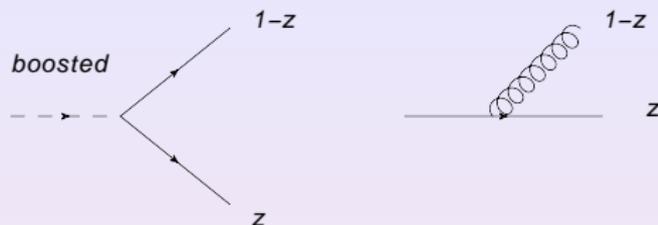
QCD splitting functions different from those for EW bosons like Higgs.

$P(z) \propto \frac{1+z^2}{1-z}$  favours soft emission while for Higgs there is a uniform distribution  $\phi(z) \propto 1$ . Looking at energy sharing within the jet gives a clue to its origin. Since QCD jets dramatically favour large  $z$  cutting on  $z$  will reduce background.

Seymour 1993, Butterworth et.al 1994, Butterworth et. al 2008

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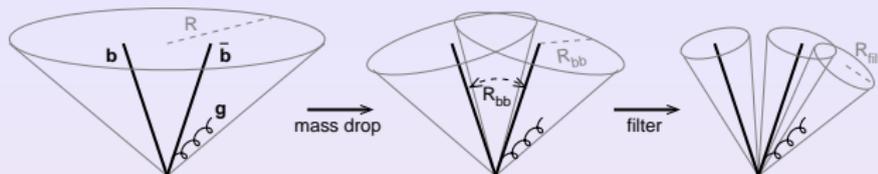
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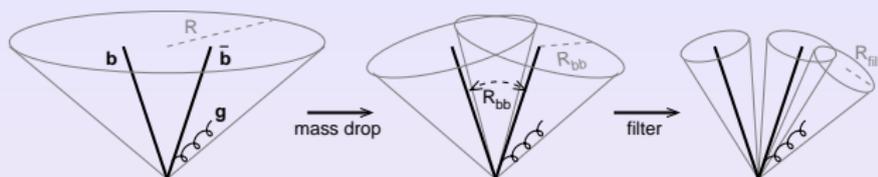
# Filtering

Mrinal Dasgupta



Various substructure techniques proposed e.g filtering, pruning, trimming. Essentially similar ideas but important differences of detail. Example - filtering with Cambridge-Aachen algorithm for Higgs production in association with a vector boson. One goes through the following steps

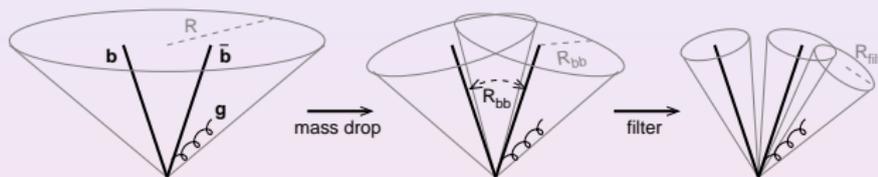
- Undo last step of algorithm so that jet  $j$  splits into  $j_1$  and  $j_2$  where  $m_{j_1} > m_{j_2}$ .
- If there was significant mass-drop  $m_{j_1} < \mu m_j$  and splitting is not very asymmetric  $y_{ij} > y_{\text{cut}}$  then  $j$  is taken to be in heavy particle neighbourhood and one exits the loop.



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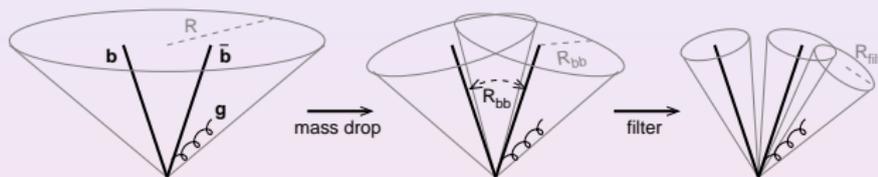
- Otherwise one redefines  $j$  to be  $j_1$  and reverts to step 1. Final jet  $j$  considered as Higgs candidate if both  $j_1$  and  $j_2$  have  $b$  tags.



Due to angular ordering jet  $j$  will contain nearly all radiation from  $b\bar{b}$ . But note that UE contribution  $\propto R^4$ .

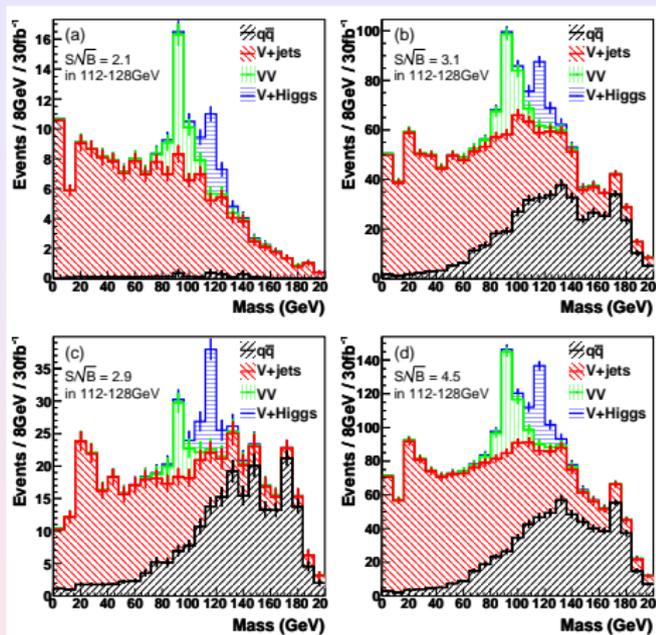
Rerun algorithm on a smaller scale to keep only 3 hardest subjets. Reduce UE but keep dominant PT radiation.

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An unpromising channel rescued.

Other techniques aimed at reducing contamination and eliminating background:

- Pruning Ellis, Vermillion, Walsh 2009
- Trimming Krohn, Thaler, Wang 2009

**Common issues:** Introduce extra parameters in jet finding which need to be tuned

For more details and recent developments see:  
<http://boost2011.org>

- Significant progress in defining, speeding up and understanding jets.
- New ideas aimed at optimizing jet studies in the context of discoveries. Optimal  $R$ , pile up subtraction are examples.
- Substructure techniques developed at an enormous rate in context of boosted heavy particle searches.
- Fast flexible tools for jet analyses available for use (FastJet, SpartyJet)

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