## ORIGIN OF INFLATION FROM VISIBLE SECTOR MODELS OF PARTICLE PHYSICS



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# How to Create

# Matter

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# **Perturbations** ?





## **Generic Predictions for Inflation**

Perturbations for Baryons & CDM have a common origin,

**Iso-curvature perturbations less than 1%** 

#### Flatness

Adiabatic

Gaussian

Tilt

 $\Omega_0 = 1 \pm \mathcal{O}(10^{-5})$ 

 $\Phi = \Phi_g + f_{NL} \Phi_a^2$ 

Confirmed

Confirmed

 $f_{NL}^{\text{Local}} = 2.7 \pm 5.8$  $f_{NL}^{\text{Equi}} = -42 \pm 75$  $f_{NL}^{\text{Ortho}} = -25 \pm 39$ 

$$n_s = 0.9608 \pm 0.0054$$

 $r < 0.12 \left( \frac{V^{1/4}}{1.9 \times 10^{16} \text{ GeV}} \right)^4$ 

Tensor



$$r = \frac{T}{S} = 24\left(1 + \frac{p}{\rho}\right)$$

 $\Phi^2 \propto k^{1-n_s} \qquad n_s = 1 - 3\left(1 + \frac{p}{\rho}\right) + \frac{d}{dN}\ln\left(1 + \frac{p}{\rho}\right)$ 

 $f_{NL} \sim \mathcal{O}(1)$ 

 $\begin{array}{ll} \langle G_{\mu\nu}\rangle = 8\pi G \langle T_{\mu\nu}\rangle & \begin{array}{l} \text{Both sides are} \\ \text{treated quantum} \end{array} \\ \text{If Gravity is Classical, then} & r = \frac{T}{S} = 0 \\ \therefore \quad \Box h_{\mu\nu} = 0 \end{array} \\ \begin{array}{l} \text{Ashoorioon, Dev, AM (2012)} \end{array} \end{array}$ 

Chibisov, Mukhanov (1982)





#### More than one sources of Non-Gaussianity

 $+f_{NL}$  &  $-f_{NL}$   $|A| \le \sqrt{\tau_{NL}}$   $\tau_{NL} < 2800 \ (@95\%)$ 

Wang, AM (2013), 1304.6399

# NO Evidence for DARK/Hidden/Mirror Radiation



$$\rho_r = \rho_\gamma \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{eff} \right] \approx \rho_\gamma (1 + 0.2271 N_{eff})$$

Only SM relativistic d.o.f. + 3 thermalized light neutrinos No need for light sterile states

# **Devil Hides in the Details**



Fig. 1. Marginalized joint 68% and 95% CL regions for  $n_s$  and  $r_{0.002}$  from *Planck* in combination with other data sets compared to the theoretical predictions of selected inflationary models.

#### Useful for Global Fitting but they shed NO light on our understanding of How to create Matter (US) & Perturbations ?

## Challenges for $R + R^2$ It is utterly INCOMPLETE !

$$\begin{split} S_{q} &= \int d^{4}x \sqrt{-g} [RF_{1}(\Box)R + RF_{2}(\Box)\nabla_{\mu}\nabla_{\nu}R^{\mu\nu} + R_{\mu\nu}F_{3}(\Box)R^{\mu\nu} + R^{\nu}_{\mu}F_{4}(\Box)\nabla_{\nu}\nabla_{\lambda}R^{\mu\lambda} \\ &+ R^{\lambda\sigma}F_{5}(\Box)\nabla_{\mu}\nabla_{\sigma}\nabla_{\nu}\nabla_{\lambda}R^{\mu\nu} + RF_{6}(\Box)\nabla_{\mu}\nabla_{\nu}\nabla_{\lambda}\nabla_{\sigma}R^{\mu\nu\lambda\sigma} + R_{\mu\lambda}F_{7}(\Box)\nabla_{\nu}\nabla_{\sigma}R^{\mu\nu\lambda\sigma} \\ &+ R^{\rho}_{\lambda}F_{8}(\Box)\nabla_{\mu}\nabla_{\sigma}\nabla_{\nu}\nabla_{\rho}R^{\mu\nu\lambda\sigma} + R^{\mu_{1}\nu_{1}}F_{9}(\Box)\nabla_{\mu_{1}}\nabla_{\nu_{1}}\nabla_{\mu}\nabla_{\nu}\nabla_{\lambda}\nabla_{\sigma}R^{\mu\nu\lambda\sigma} \\ &+ R_{\mu\nu\lambda\sigma}F_{10}(\Box)R^{\mu\nu\lambda\sigma} + R^{\rho}_{\mu\nu\lambda}F_{11}(\Box)\nabla_{\rho}\nabla_{\sigma}R^{\mu\nu\lambda\sigma} + R_{\mu\rho_{1}\nu\sigma_{1}}F_{12}(\Box)\nabla^{\rho_{1}}\nabla^{\sigma_{1}}\nabla_{\rho}\nabla_{\sigma}R^{\mu\rho\nu\sigma} \\ &+ R^{\nu_{1}\rho_{1}\sigma_{1}}F_{13}(\Box)\nabla_{\rho_{1}}\nabla_{\sigma_{1}}\nabla_{\nu_{1}}\nabla_{\nu}\nabla_{\rho}\nabla_{\sigma}R^{\mu\nu\lambda\sigma} + R^{\mu_{1}\nu_{1}\rho_{1}\sigma_{1}}F_{14}(\Box)\nabla_{\rho_{1}}\nabla_{\sigma_{1}}\nabla_{\nu_{1}}\nabla_{\mu}\nabla_{\nu}\nabla_{\rho}\nabla_{\sigma}R^{\mu\nu\lambda\sigma} \end{split}$$

#### Gravity Invokes 🔿 Higher Order Corrections

$$S = \int d^4x \sqrt{-g} \left[ R + R\mathcal{F}_1(\Box)R + R_{\mu\nu}\mathcal{F}_2(\Box)R^{\mu\nu} + R_{\mu\nu\alpha\beta}\mathcal{F}_3(\Box)R^{\mu\nu\alpha\beta} \right]$$
$$\mathcal{F}_i(\Box) = \sum_n^\infty a_n \Box^n \qquad \Delta \mathcal{L} = \sqrt{-g} \left(\alpha R^2 + \beta R_{\mu\nu}^2 + \gamma R_{\alpha\beta\mu\nu}^2\right)$$

$$2\mathcal{F}_1(\Box) + \mathcal{F}_2(\Box) + 2\mathcal{F}_3(\Box) = 0$$

Biswas, Gerwick, Koivisto & AM, Phys. Rev. Lett. (2012)

Classical Gravity becomes WEAK in the UV (Asymptotic Freedom)



### The Inflaton Vacuum cannot be arbitrary

A.M & Rocher, Phys. Rept. (2011), Particle Physics Models of Inflation & Curvaton

#### Last 50-60 e-folds of Inflation cannot be driven by an Arbitrary Field

## Such as Gauge singlets, or String theory Moduli, or Dilaton, ....

You can always match the perturbations, exotic non-Gaussianity, wiggles, low multipoles, & perhaps what not,..., but creating the right form of matter remains the biggest challenge





## Constructing a Potential ...

$$V(\phi) = V_0 + a(\phi - \phi_0) + \frac{b}{2}(\phi - \phi_0)^2 + \frac{c}{6}(\phi - \phi_0)^3 + \cdots,$$
  
$$V_0 \equiv V(\phi_0) , \ a \equiv V'(\phi_0) , \ b \equiv V''(\phi_0) , \ c \equiv V'''(\phi_0) ,$$



 $\phi - \phi_0 \ll M_p$ 



One requires shape & curvature smooth enough to appreciate the beauty

# **Constructing a Potential ...**

$$V = \frac{1}{2}m^2|\phi|^2 - \frac{A\lambda}{nM_P^{n-3}}\phi^n + \frac{\lambda^2}{M_P^{2(n-3)}}|\phi|^{2(n-1)}$$

 $\frac{A}{m} = \sqrt{8(n-1)\left(1-\frac{(n-2)^2}{4}\beta^2\right)}$ 

$$\begin{split} \phi_0 &= \left(\frac{M_P^{n-3}m}{\lambda\sqrt{2(n-1)}}\right)^{1/(n-2)} \\ V_0 &= \frac{(n-2)^2}{2n(n-1)} m^2 \phi_0^2 \,, \\ a &= \frac{(n-2)^2}{4} \beta^2 m^2 \phi_0 \,, \\ c &= 2(n-2)^2 \, \frac{m^2}{\phi_0} \,. \end{split}$$

$$\begin{aligned} \mathcal{P}_{R}^{1/2} &\equiv \frac{1}{\sqrt{24\pi^{2}}} \frac{V_{0}^{1/2}}{\epsilon^{1/2} M_{P}^{2}} = \frac{V_{0}^{1/2}}{2\pi\sqrt{6}M_{P}^{2}X} \sin^{2}Y \\ n_{s} &\equiv 1 + 2\eta - 6\epsilon = 1 - \frac{4}{\mathcal{N}_{COBE}} Y \cot Y , \\ \alpha &= -\frac{4}{\mathcal{N}_{COBE}^{2}} \left(\frac{Y}{\sin Y}\right)^{2} . \end{aligned}$$

$$\begin{aligned} V(|\phi|) &= \frac{1}{2}m^2|\phi|^2 - \frac{Ah}{3}\phi^3 + h^2|\phi|^4 \quad (n=3)\\ V(|\phi|) &= \frac{1}{2}m^2|\phi|^2 - \frac{A\lambda}{6}\frac{\phi^6}{M_p^3} + \lambda^2\frac{|\phi|^{10}}{M_p^6} \quad (n=6) \end{aligned}$$

#### Inflation takes place always Below Planck VeV

Allahverdi, Enqvist, Garcia-Bellido, AM, PRL (2006), JCAP (2006)

Bueno-Sanchez, Dimopoulos & Lyth, JCAP (2006)

Allahverdi, Kusenko AM, JCAP (2006),

Allahverdi, Dutta & AM, PRL (2007)

#### Inflection-point Inflation: Flexibility of the Potential



# **Visible sector Inflatons**

		Always lifted
	B-L	by $W_{\text{renorm}}$ ?
LH <sub>u</sub>	-1	
$H_uH_d$	0	
udd	-1	
LLe	-1	
QuL	-1	
$QuH_u$	0	
$\mathrm{QdH}_{\mathrm{d}}$	0	
LH <sub>d</sub> e	0	
QQQL	0	
$\mathrm{Qu}\mathrm{Qd}$	0	
QuLe	0	
uude	0	
$QQQH_d$	1	
QuH <sub>d</sub> e	1	
dddLL	-3	
uuuee	1	
QuQue	1	
QQQQu	1	
dddLH <sub>d</sub>	-2	$\checkmark$
uudQdHu	-1	
$(QQQ)_4LLH_u$	-1	
$(QQQ)_4LH_uH_d$	0	
$(QQQ)_4H_uH_dH_d$	1	$\checkmark$
(QQQ) <sub>4</sub> LLLe	-1	
uudQdQd	-1	
(QQQ) <sub>4</sub> LLH <sub>d</sub> e	0	
$(QQQ)_4LH_dH_de$	1	$\checkmark$
$(QQQ)_4H_d\overline{H_dH_d}e$	2	

SU(	$(3) \times SU(2)_l \times U(1)_Y$
$u_1 d_2 d_3$	$d_{2}^{\beta} = \frac{1}{\sqrt{3}}\phi$ $u_{1}^{\alpha} = \frac{1}{\sqrt{3}}\phi$ $d_{3}^{\gamma} = \frac{1}{\sqrt{3}}\phi$
$L_1 L_2 e_3$	$L_1^a = \frac{1}{\sqrt{3}} \begin{pmatrix} 0\\ \phi \end{pmatrix}  L_2^b = \frac{1}{\sqrt{3}} \begin{pmatrix} \phi\\ 0 \end{pmatrix}  e_3 = \frac{1}{\sqrt{3}} \phi$
$H_u H_d$	$H_u = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi \\ 0 \end{pmatrix} \qquad \qquad H_d = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi \end{pmatrix}$
SU(3)	$\times SU(2)_l \times U(1)_Y \times U(1)_{B-L}$
$NH_uL$	$N = \frac{1}{\sqrt{3}}\phi  H_u = \frac{1}{\sqrt{3}} \begin{pmatrix} 0\\ \phi \end{pmatrix}  L = \frac{1}{\sqrt{3}} \begin{pmatrix} \phi\\ 0 \end{pmatrix}$

Allahverdi, Enqvist, Bellido, AM, (PRL, 2006), (JCAP, 2007), Allahverdi, Kusenko, AM, JCAP (2007), Allahverdi, Dutta, AM (PRL 2007), Chatterjee, AM, JCAP (2011)

## **MSSM Inflaton Potentials**



Potentials are constructed by small perturbations around the Enhanced Gauge Symmetry Point

Affleck, Dine, NPB (1985), Dine, Randall, Thomas, NPB (1996)

#### **Renormalizable Potential from a Visible Sector**



Inflaton decays into MSSM dof + LSP ( dark matter candidate)

Allahverdi, Dutta & AM, Phys.Rev.Lett. (2007)

#### **Non-renormalizable Potential from MSSM**



Boehm, DaSilva, AM & Pukartas, PRD (2012), Wang, Pukartas & AM (hep-ph/1303.535)

#### **MSSM dof Via Instant Preheating**



$$T_{rh} = \left(\frac{30}{\pi^2 g_*}\right) \qquad \rho_{\phi}^{1/4}$$

$$\sim 3 \times 10^8 \text{ GeV} (\text{for } m_{\phi} \sim 1 \text{ TeV})$$

Allahverdi, Ferrantelli, Garcia-Bellido & AM PRD (2011)





## Parameter space for Inflaton (udd) + DM within NUHM-2 scenario



Scanning NUHM-2 scenario



## Correlation between Inflaton, Stau & lightest Stop



Boehm, DaSilva, AM & Pukartas, PRD (2012),

#### **Curvaton & Inflaton from MSSM**



## Bench-Mark Points for Visible Sector Models of Inflation & Curvaton

With Hubble-Induced SUGRA Corrections	Inflaton	Both Inflaton & Curvaton	
$\star$ $r < 0.11$	Inflection Point for Saddle Point for		
Relativistic dof [2]	only SM	only SM	
$f_{ m NL}^{orth} = -25 \pm 39$ [3]	< 1, ✓	Constrained, $\checkmark$	1
$f_{\rm NL}^{equil} = -42 \pm 75$ [3]	< 1, ✓	Constrained, $\checkmark$	
$f_{ m NL}^{local} = 2.7 \pm 5.8$ [3]	< 1, ✓	Constrained, $\checkmark$	
$dn_s/d\ln k = -0.0134 \pm 0.0090$ [4]	$\lesssim -0.002, \checkmark$	$\checkmark$	1
$n_s = 0.9603 \pm 0.073$ [2]	$\checkmark$	$\checkmark$	1
$10^9 P_{\zeta} = 2.196^{+0.051}_{-0.060}$ [2]	$\checkmark$	$\checkmark$	
r < 0.11 (95%  CL) [4]	× Negligible, ✓	Negligible, $\checkmark$	1.00
Tensor-to-scalar ratio	No ali aible	No ali aible	Ī
Planck Constraints $(1\sigma)$	MSSM inflation	MSSM Curvaton	
			-

#### Conclusions

Last 50-60 e-folds of Inflation MUST be embedded within a VISIBLE sector

Discovery of B-modes will not only test the Inflationary paradigm but will also test the structure of Space-Time and perhaps the nature of Quantum Gravity itself



# Extra Slides

#### ALARMINGLY LARGE NON-GAUSSINAITY DURING SINGLET PREHEATING



#### Longer this time span of changing e.o.s ----> Larger will be Non-Gaussianity

Enqvist, Jokinen, AM, Multamaki, Vaihkonen, Phys.Rev. Lett. (2005)

Instant Preheating Does NOT generate Non-Gaussianity  $f_{NL} \ll 1$ 

Felder, Kofman, Linde, Phys.Rev.D (1998)

Enqvist, Jokinen, AM, Multamaki, Vaihkonen, JCAP (2005)

## Inflation + Adiabatic Vacuum



### Why is Quantum Gravity so kind towards us? What is the CMB telling us about the Nature of Gravity in UV?

## **Some Issues about Inflation**

### **Quantization of Space Time**



#### Would we ever see B-mode of Polarization ?

**Never: If Gravity is treated Classically** 

Ashoorioon, Dev & AM (1211.4678)

**JCAP (2012)** 

#### Note: B-modes do not require super-Planckian Inflaton VEVs such as Chaotic Inflation Hotchkiss, AM & Nadathur,

Inflection Point Inflation can do so with VeVs below the cut-off

**Beyond the SM:** Where to Embed the Last Phase of Inflation ?



# Planck





FIG. 2: The ratio  $(40m_{\phi}^2/A^2)$  as a function of  $\text{Log}[\frac{\mu}{\text{GeV}}]$  in the case of *udd* flat direction. The curves are for  $M_{\text{GUT}}$  boundary values  $m_{\phi} = 150, 200, 250, 300 \text{ GeV}$  (respectively from left to right), and A = 1.6 TeV.



## Is there a Fine - Tuning ?

 $m_{\phi}(\phi_0), A(\phi_0)$ 

#### **RG - Equations**

#### $m_{\phi}(100 \text{ GeV}), A(100 \text{ GeV})$

FIG. 3: The ratio  $(40m_{\phi}^2/A^2)$  as a function of  $\text{Log}[\frac{\mu}{\text{GeV}}]$  in the case of *udd* flat direction. The curves are for  $M_{\text{GUT}}$  boundary values  $A_{udd}=1.6$ , 1.8, 2.0, 2.2 TeV (respectively from top to bottom), and  $m_{\phi} = 400$  GeV.

#### **Supergravity Induced Potential**



$$V(\phi) = V_c + \frac{c_H H^2}{2} |\phi|^2 - \frac{a_H H}{n M_P^{n-3}} \phi^n + \frac{|\phi|^{2(n-1)}}{M_P^{2(n-3)}}$$

AM & Nadathur Phys. Rev. D ( 2011)

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#### **Attraction Towards Inflection Point**

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#### **Ever Changing models of Inflation**

**980** R\*R, OLD, NEW, CHAOTIC, EXTENDED, SOFT, BRANS-DICKE, SUSY, SUGRA, THERMAL, EXPONENTIAL, DOUBLE, ....

HYBRID, MUTATED HYBRID, INVERTED 1990 HYBRID, F-TERM, D-TERM, K-TERM, TOPOLOGICAL, ASSISTED, .....

N-FLATION, BRANE, BRANE-CHAOTIC/ 2000 HYBRID, TACHYONIC, DBI, RACE-TRACK, HILL-TOP, FAST-ROLL, P-TERM, F+D-TERM, EXTENDED-HIGGS, CYCLIC, Kahler, Non-Kahler, Sweese Cheese, D3/D7, ... None of these models can actually work !!