## **PLANCK 2013**, FROM THE PLANCK SCALE TO THE ELECTROWEAK SCALE, BONN UNIV., MAY 20 – 24, 2013

# CRITICAL ISSUES IN FLAVOR PHYSICS

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## IS THERE A "FLAVOR PROBLEM"

## The flavor problem in the SM

- Why 3 fermion families ("who ordered the muon?")
- How to account for the vast spread in the values of fermion masses and mixings ("I cannot believe that I've a final theory as long as it does not tell me why the muon is 200 heavier than the electron")

## The flavor problem in TeV New Physics BSM

How to suppress the new FCNC contributions (with or without CPV) arising from the exchange of the virtual TeV new physics particles

# THE SM AND BSM FLAVOR PUZZLES SM BSM

- The apparent randomness of fermion masses and mixings → it's one the three major "esthetical" deficiencies of the
  - **SM** together with the lack of a true
  - UNIFICATION of

fundamental forces and the

NATURALNESS issue of the GAUGE HIERARCHY

- TeV new Physics could be FLAVOR BLIND (i.e. only sources of flavor remain the SM Yukawa couplings)
   MINIMAL FLAVOR VIOLATION
- If no MFV, the new physics FCNC contribution can be suppressed by specific (like the GIM mechanism) or accidental (like the smallness of the mixing angles, or the largeness of the ~TeV masses) reasons (with effects <10% of the leading SM contributions for some relevant flavor quantities)</li>

**BOTH** THE SM AND BSM FLAVOR PUZZLES CAN FIND A SOLUTION IN THE

EXISTENCE OF A NEW (GAUGE OR GLOBAL OR

**DISCRETE) FLAVOR SYMMETRY** 

## THE FLAVOUR PROBLEMS

#### **FERMION MASSES**

What is the rationale hiding behind the spectrum of fermion masses and mixing angles (our "Balmer lines" problem)

## LACK OF A FLAVOUR "THEORY"

( new flavour – horizontal symmetry, radiatively induced lighter fermion masses, dynamical or geometrical determination of the Yukawa couplings, ...?)

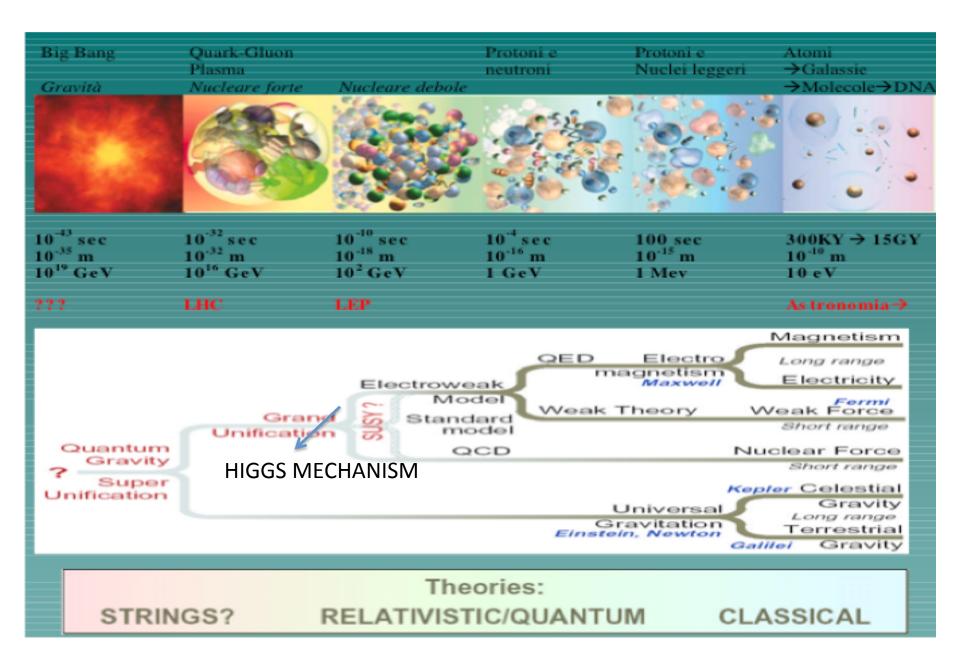
#### **FCNC**

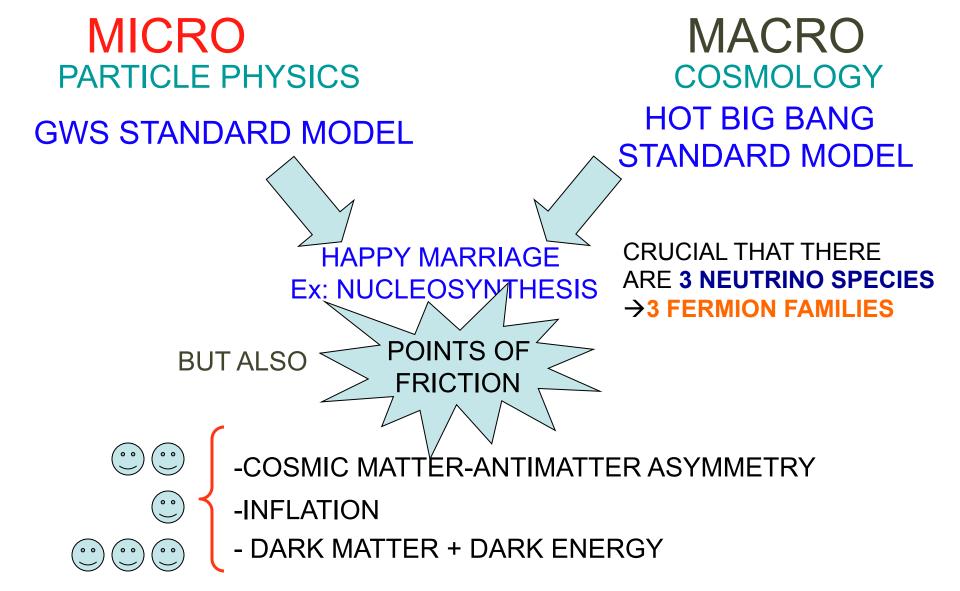
Flavour changing neutral current (FCNC) processes are suppressed.

In the SM two nice mechanisms are at work: the GIM mechanism and the structure of the CKM mixing matrix.

How to cope with such delicate suppression if the there is new physics at the electroweak scale?

## A role for flavor in the Universe evolution?

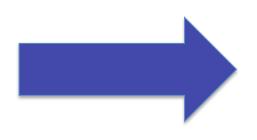




"OBSERVATIONAL" EVIDENCE FOR NEW PHYSICS BEYOND THE (PARTICLE PHYSICS) STANDARD MODEL

## The Energy Scale from the "Observational" New Physics

neutrino masses dark matter baryogenesis inflation



NO NEED FOR THE NP SCALE TO BE CLOSE TO THE ELW. SCALE

The Energy Scale from the "Theoretical" New Physics

 $\star$   $\star$  Stabilization of the electroweak symmetry breaking at M<sub>W</sub> calls for an ULTRAVIOLET COMPLETION of the SM

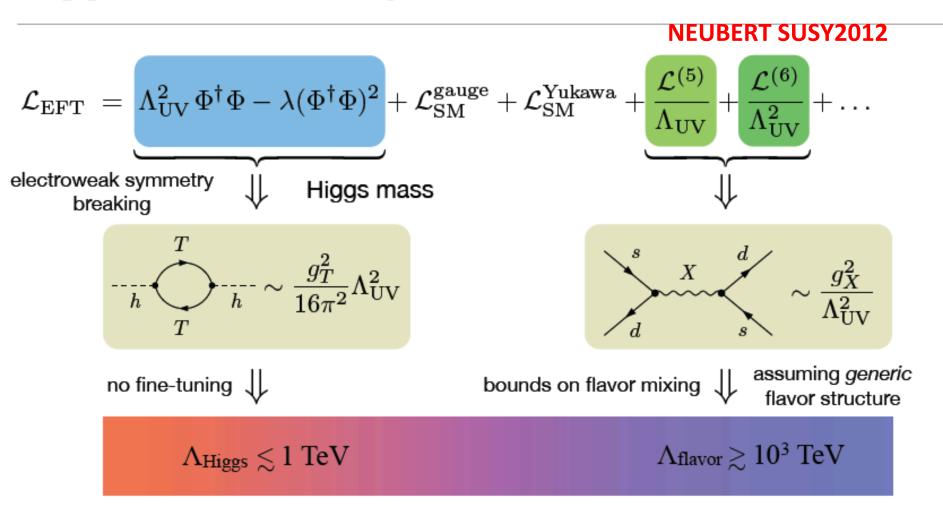
already at the TeV scale





CORRECT GRAND UNIFICATION "CALLS" FOR NEW PARTICLES

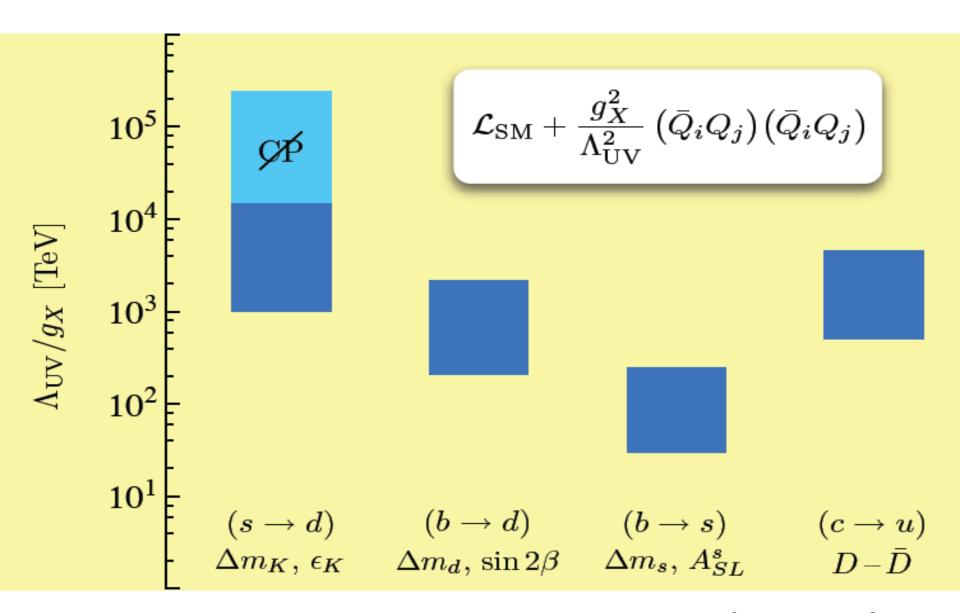
## Higgs and flavor physics as indirect BSM probes



Possible solutions to flavor problem explaining  $\Lambda_{\text{Higgs}} << \Lambda_{\text{flavor}}$ :

- (i)  $\Lambda_{\rm UV}>>1~{
  m TeV}$ : Higgs fine tuned, new particles too heavy for LHC
- (ii)  $\Lambda_{\rm UV} pprox 1~{
  m TeV}$ : quark flavor-mixing protected by a flavor symmetry

## **FCNC and GENERIC FLAVOURED NEW PHYSICS**



Generic bounds on New Physics scale (for g<sub>X</sub>~1)

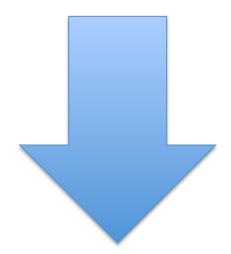
### Isidori, Nir, Perez

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \mathcal{L}_{eff}^{NP}$$

$$\mathcal{L}_{eff}^{NP} = \Sigma_i \frac{c_i}{\Lambda_{NP}^2} O_i$$

Operator	Bounds on $\Lambda$ in TeV $(c_{ij} = 1)$		Bounds on $c_{ij}$ ( $\Lambda = 1 \text{ TeV}$ )		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	$9.8 \times 10^{2}$	$1.6 \times 10^{4}$	$9.0 \times 10^{-7}$	$3.4 \times 10^{-9}$	$\Delta m_K$ ; $\epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	$1.8 \times 10^{4}$	$3.2 \times 10^5$	$6.9\times10^{-9}$	$2.6\times10^{-11}$	$\Delta m_K$ ; $\epsilon_K$
$(ar{c}_L \gamma^\mu u_L)^2$	$1.2 \times 10^{3}$	$2.9 \times 10^{3}$	$5.6 \times 10^{-7}$	$1.0 \times 10^{-7}$	$\Delta m_D;  q/p , \phi_D$
$(\bar{c}_R  u_L) \big(\bar{c}_L u_R)$	$6.2 \times 10^{3}$	$1.5 \times 10^4$	$5.7 \times 10^{-8}$	$1.1 \times 10^{-8}$	$\Delta m_D;  q/p , \phi_D$
$(\overline{b}_L \gamma^\mu d_L)^2$	$6.6 \times 10^{2}$	$9.3 \times 10^{2}$	$2.3 \times 10^{-6}$	$1.1 \times 10^{-6}$	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	$2.5 \times 10^3$	$3.6 \times 10^3$	$3.9\times10^{-7}$	$1.9\times10^{-7}$	$\Delta m_{B_d}; S_{\psi K_S}$
$(ar{b}_L \gamma^\mu s_L)^2$	$1.4 \times 10^{2}$	$2.5 \times 10^{2}$	$5.0 \times 10^{-5}$	$1.7 \times 10^{-5}$	$\Delta m_{B_s}; S_{\psi\phi}$
$(\bar{b}_Rs_L)(\bar{b}_Ls_R)$	$4.8 \times 10^{2}$	$8.3 \times 10^{2}$	$8.8 \times 10^{-6}$	$2.9\times10^{-6}$	$\Delta m_{B_s}; S_{\psi\phi}$

## theoretical (esthetical) SM problems



New physics at the TeV scale

GAUGE HIERARCHY ★★★★★

UNIFICATION \*\*

FLAVOR ???

# FLAVOR AND THE OBSERVATIONAL REASONS TO GO BEYOND THE SM

- MASSIVE NEUTRINOS: new Yukawa couplings related to the appearance of neutrino masses ("Dirac couplings"  $v_L v_R$ , "Majorana couplings"  $v_L v_L$  or  $v_R v_R$ )
- COSMIC MATTER ANTIMITER ASYMMETRY: i)
   new source of CP violation; ii) in leptogenesis
   need more than one fermion generation
- **DARK MATTER** and **INFLATION**: no necessary link with the flavor issue.

## LFV and NEW PHYSICS

- Flavor in the HADRONIC SECTOR:
   CKM paradigm
- Flavor in the LEPTONIC SECTOR:
  - Neutrino masses and (large) mixings
  - Extreme smallness of LFV in the charged lepton sector of the SM with massive neutrinos:

$$I_i$$
 suppressed by  $(m_v^2 - m_v^2)/M_W^2$ 

## LFV IN SUSY SEE-SAW

SEE- SAW (type 1)

New source of (leptonic) flavor:

YUKAWA COUPLINGS OF THE NEUTRINO DIRAC MASS
CONTRIBUTIONS, i.e. **THE YUKAWAS** of the **HIGGS** couplings to the **LETF-** and **RIGHT** —

HANDED NEUTRINOS

**LOW-ENERGY SUSY** 

The scalar lepton

masses through their

running bring memory of

those new sources of

leptonic flavor at the TeV

scale, i.e. at energies much

below the (Majorana) mass

of the RH neutrinos

# THE STRONG ENHANCEMENT OF LFV IN SUSY SEESAW MODELS CAN OCCUR

EVEN IF THE MECHANISM
RESPONSIBLE FOR SUSY
BREAKING IS ABSOLUTELY
FLAVOR BLIND

## SUSY SEESAW: Flavor universal SUSY breaking and yet large lepton flavor violation

Borzumati, A. M. 1986 (after discussions with W. Marciano and A. Sanda)

$$L = f_l \overline{e}_R L h_1 + f_v \overline{v}_R L h_2 + M v_R v_R$$

$$\tilde{L} = \int_l \overline{e}_R L h_1 + f_v \overline{v}_R L h_2 + M v_R v_R$$

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Non-diagonality of the slepton mass matrix in the basis of diagonal lepton mass matrix depends on the unitary matrix U which diagonalizes  $(f_v^+f_v^-)$ 

## **How Large LFV in SUSY SEESAW?**

- 1) Size of the Dirac neutrino couplings f<sub>v</sub>
- 2) Size of the diagonalizing matrix U

In **MSSM seesaw** or in **SUSY SU(5)** (Moroi): not possible to correlate the neutrino Yukawa couplings to know Yukawas;

In **SUSY SO(10)** (A.M., Vempati, Vives) at least one neutrino Dirac Yukawa coupling has to be of the **order of the top Yukawa coupling** one large of O(1) f<sub>v</sub>

U two "extreme" cases:

- b) U with "large" entries with the exception of the 13 entry

<u>U = PMNS</u> matrix responsible for the diagonalization of the neutrino mass matrix

### LFV in SUSYGUTs with SEESAW



Scale of appearance of the SUSY soft breaking terms resulting from the spontaneous breaking of supergravity Low-energy SUSY has "memory" of all the multi-step RG occurring from such superlarge scale down to M<sub>w</sub>

**→**potentially large LFV

Barbieri, Hall; Barbieri, Hall, Strumia; Hisano, Nomura, Yanagida; Hisano, Moroi, Tobe Yamaguchi; Moroi;A.M.,, Vempati, Vives; Carvalho, Ellis, Gomez, Lola; Calibbi, Faccia, A.M, Vempati LFV in MSSMseesaw: μ eγ-Borzumati, A.M.

 $\tau$  μ $\gamma$  Blazek, King;

General analysis: Casas Ibarra; Lavignac, Masina, Savoy; Hisano, Moroi, Tobe, Yamaguchi; Ellis, Hisano, Raidal, Shimizu; Fukuyama, Kikuchi, Okada; Petcov, Rodejohann, Shindou, Takanishi; Arganda, Herrero; Deppish, Pas, Redelbach, Rueckl; Petcov, Shindou

L. Calibbi, NuFact 2012

In SUSY, new fields interacting with the MSSM fields enter the radiative corrections of the sfermion masses Hall Kostelecky Raby '86

This applies to the new seesaw interactions: generically induce LFV in the slepton mass matrix!

Type I 
$$(\tilde{m}_L^2)_{ij} \propto m_0^2 \sum_k (\mathbf{Y}_N^*)_{ki} (\mathbf{Y}_N)_{kj} \ln \left(\frac{M_X}{M_{R_K}}\right) \quad \text{Borzumati Masiero '86}$$
 Type II 
$$(\tilde{m}_L^2)_{ij} \propto m_0^2 (\mathbf{Y}_\Delta^\dagger \mathbf{Y}_\Delta)_{ij} \ln \left(\frac{M_X}{M_\Delta}\right) \propto m_0^2 (\mathbf{m}_\nu^\dagger \mathbf{m}_\nu)_{ij} \ln \left(\frac{M_X}{M_\Delta}\right)$$
 Type III Similar to type I

Biggio LC '10; Esteves et al. '10

Thorough analysis of LFV in these 3 kinds of Seesaw in the SUSY context M. HIRSCH, F. JOAQUIM, A. VICENTE arXiv: 1207.6635 [hep-ph]

## IMPACT OF

HIGGS 
$$124.5 \text{ GeV} \lesssim m_h \lesssim 126.5 \text{ GeV}$$

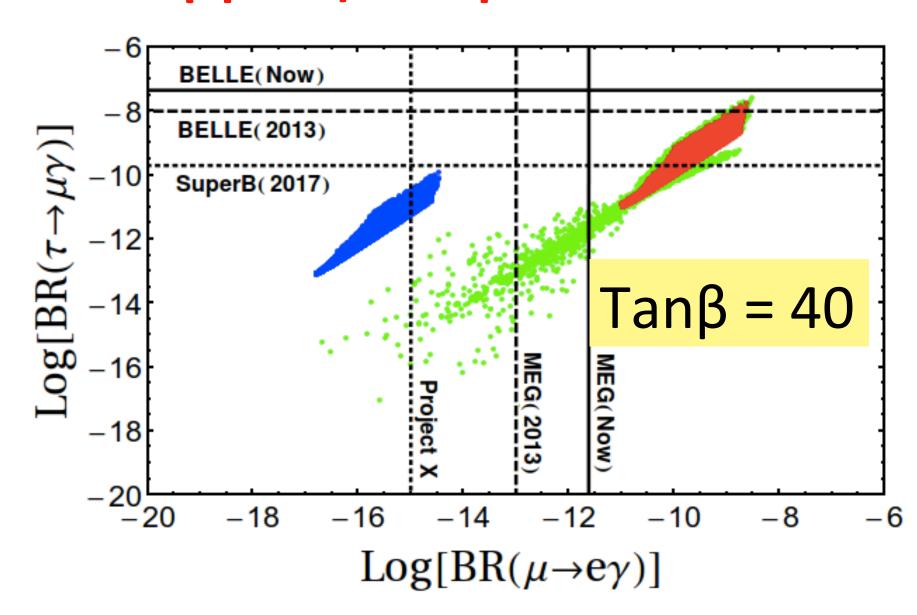
**LFV LIMITS** BR(
$$\mu \to e + \gamma$$
) < 2.4 × 10<sup>-12</sup> (90% CL).

$$\sin^2 2\theta_{13} = 0.092 \pm 0.016(\text{stat.}) \pm 0.005(\text{syst.})$$
$$\sin^2 2\theta_{13} = 0.113 \pm 0.013(\text{stat.}) \pm 0.019(\text{syst.})$$

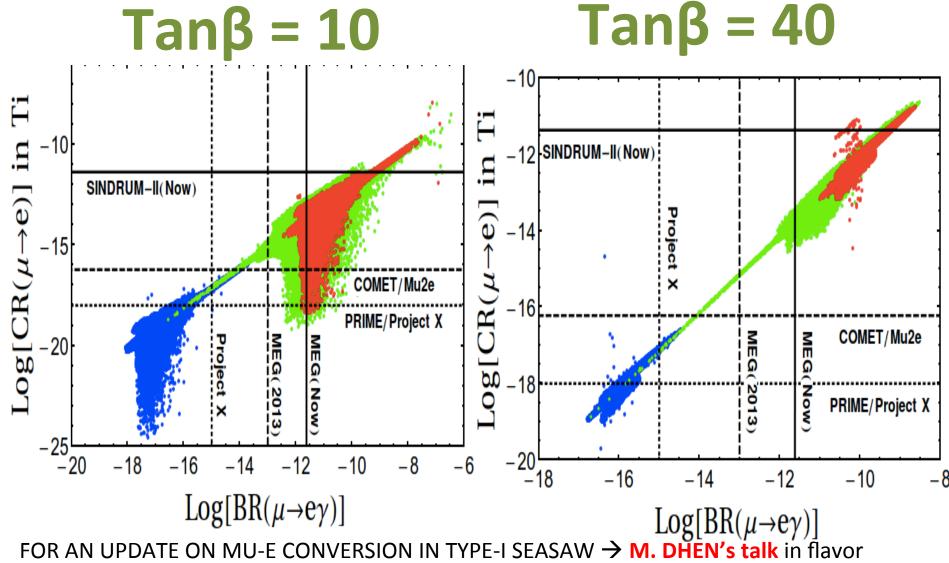
on SUSY GUTs where neutrinos get mass through the SEE-SAW MECHANISM

L. Calibbi, D. Chowdhury, A.M., K.M. Patel and S.K. Vempati arXiv:1207.7227v1 [hep-ph]

## $\tau \rightarrow \mu \gamma$ vs. $\mu \rightarrow e \gamma$ sensitivities

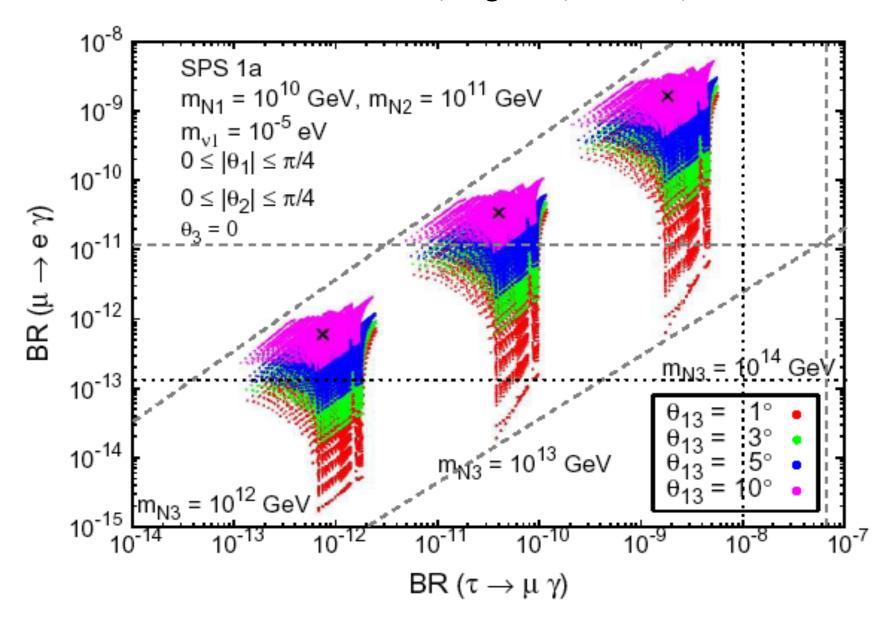


## $\mu$ – e conversion vs $\mu$ $\rightarrow$ e $\gamma$



FOR AN UPDATE ON MU-E CONVERSION IN TYPE-I SEASAW → M. DHEN's talk in flavor parallel session

#### Antusch, Arganda, Herrero, Teixeira



## **DEVIATION** from μ - e UNIVERSALITY

#### A.M., Paradisi, Petronzio

• Denoting by  $\Delta r_{NP}^{e-\mu}$  the deviation from  $\mu - e$  universality in  $R_{K,\pi}$  due to new physics, i.e.:

$$R_{K,\pi} = R_{K,\pi}^{SM} \left( 1 + \Delta r_{K,\pi NP}^{e-\mu} \right),$$

• we get at the  $2\sigma$  level:

$$-0.063 \le \Delta r_{KNP}^{e-\mu} \le 0.017 \text{ NA48/2}$$

$$-0.0107 \le \Delta r_{\pi NP}^{e-\mu} \le 0.0022$$
 PDG

**Presently**: error on  $R_K$  down to the **1% level** ( KLOE (09) and NA48 (07 data); using 40% of the data collected in 08, NA62 is now decreasing the uncertainty at the **0.7% level Prospects**: Summer conf. we'll have the result concerning the 40% data analysis by NA62 and when the analysis of the whole sample of data is accomplished **the stat. uncertainty will be < 0.3%** 

#### HIGGS-MEDIATED LFV COUPLINGS

- When non-holomorphic terms are generated by loop effects (HRS corrections)
- And a source of LFV among the sleptons is present
- Higgs-mediated (radiatively induced)
   H-lepton-lepton LFV couplings arise

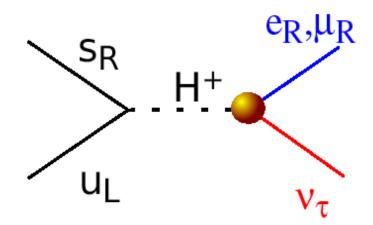
Babu, Kolda; Sher; Kitano, Koike, Komine, Okada; Dedes, Ellis, Raidal; Brignole, Rossi; Arganda, Curiel, Herrero, Temes; Paradisi; Brignole, Rossi

## **DEVIATION** from μ - e UNIVERSALITY

A.M., Paradisi, Petronzio

## H mediated LFV SUSY contributions to R<sub>K</sub>

$$R_K^{LFV} = \frac{\sum_i K \to e\nu_i}{\sum_i K \to \mu\nu_i} \simeq \frac{\Gamma_{SM}(K \to e\nu_e) + \Gamma(K \to e\nu_\tau)}{\Gamma_{SM}(K \to \mu\nu_\mu)} , \quad i = e, \mu, \tau$$



$$eH^{\pm} rac{oldsymbol{
u}_{ au}}{\sqrt{2}} 
ightarrow rac{oldsymbol{g}_2}{M_W} \Delta_R^{31} an^2 eta$$

$$\Delta_R^{31} \sim rac{lpha_2}{4\pi} \, \delta_{RR}^{31}$$

$$\Delta_R^{31} \sim 5 \cdot 10^{-4} \ t_\beta = 40 \ M_{H^{\pm}} = 500 \text{GeV}$$

Analysis in various SUSY models: see R. Fonseca's talk in yesterday Flavor parallel

Session

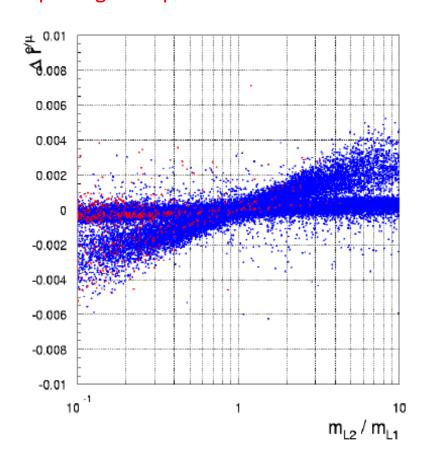
$$\Delta r_{KSUSY}^{e-\mu} \simeq \left(\frac{m_K^4}{M_{H^+}^4}\right) \left(\frac{m_\tau^2}{m_e^2}\right) |\Delta_R^{31}|^2 \tan^6 \beta \approx 10^{-2}$$

Extension to B Iv deviation from universality Isidori, Paradisi

#### A.M., PARADISI. PETRONZIO

LFU breaking occurs in a **LF conserving** case because of the splitting in slepton masses

#### LFU breaking occurs with LFV



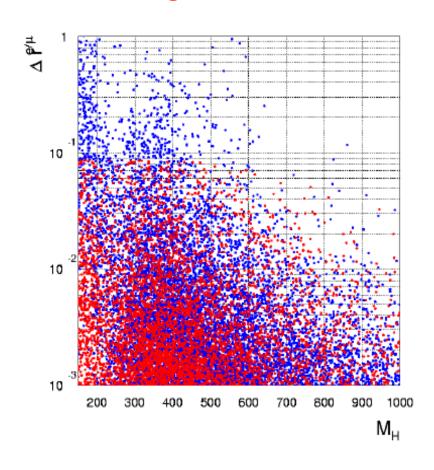


Figure 2: Left: $\Delta r_K^{e/\mu}$  as a function of the mass splitting between the second and the first (left-handed) slepton generations. Red dots can saturate the  $(g-2)_{\mu}$  discrepancy at the 95% C.L., i.e.  $1 \times 10^{-9} < (g-2)_{\mu} < 5 \times 10^{-9}$ . Right:  $\Delta r_K^{e/\mu}$  as a function of  $M_{H^+}$ .

#### V: WHERE WE STAND AND WHERE WE'RE HEADING TO

$$\delta m_{12}^2$$



SOLARS+KAMLAND  

$$\delta m_{12}^2 = (7.9 + /-0.7) \cdot 10^{-5} \text{ eV}^2$$

$$\theta_{12}$$



SOLARS+KAMLAND  $\sin^2(2\theta_{12}) = 0.82 + /-0.055$ 

#### Addressed by accelerator neutrino experiments

$$\delta m^2_{23} \ \ {\color{red} \swarrow}$$

$$\delta m^2 = (2.4 + /- 0.4) 10^3 \text{ eV}^2$$



 $\sin^2(2\theta_{23}) > 0.95$ 

$$\theta_{13}$$



$$\sin^2 2\theta_{13} = 0.1$$

 $\sin^2 2\theta_{13} = 0.1$  LSND/Steriles ?









$$\Sigma \, m_{\nu}$$



 $\Sigma m_v < 6.6 \text{ eV}$ 

BETA DECAY END POINT

Dirac/Majorana







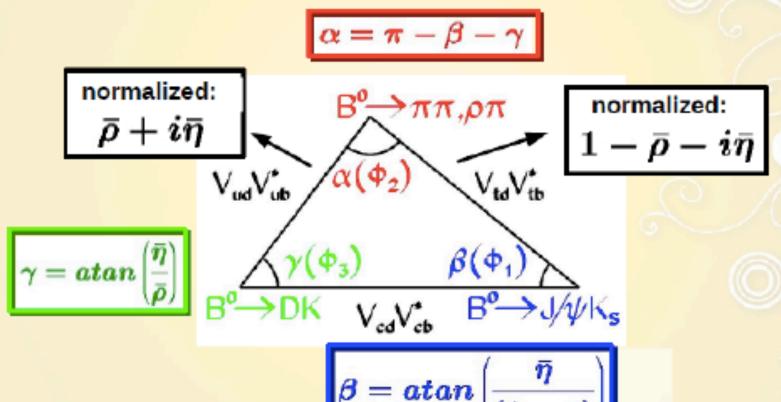


ACCORDING TO MY PERSONAL TASTE

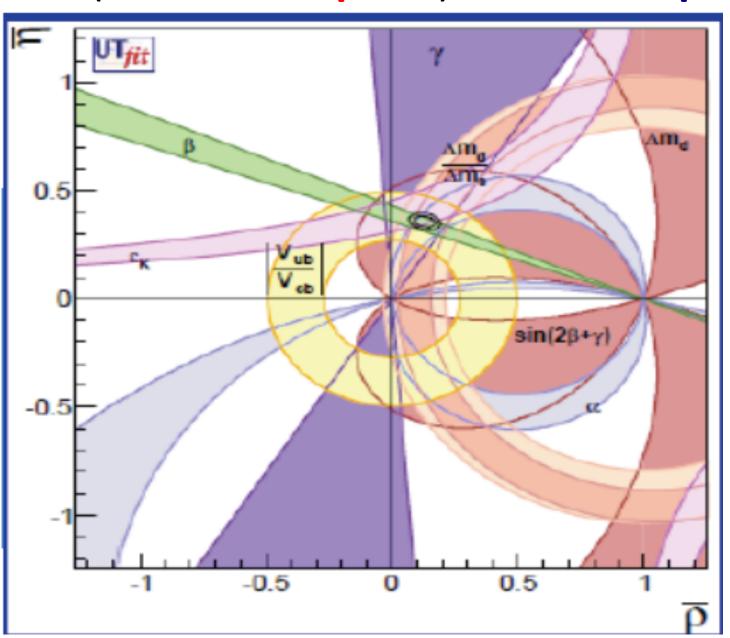
## **CKM matrix and Unitarity Triangle**

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

many observables functions of ρ and η: overconstraining



## the (almost complete) CKM triumph



# What to make of this triumph of the CKM pattern in hadronic flavor tests?

New Physics at the Elw. Scale is Flavor Blind CKM exhausts the flavor changing pattern at the elw. Scale

MINIMAL FLAVOR VIOLATION

**New Physics introduces** 

NEW FLAVOR SOURCES in addition to the CKM pattern. They give rise to contributions which are <10% in the "flavor observables" which have already been observed!

MFV: Flavor originates only from the SM Yukawa coupl.

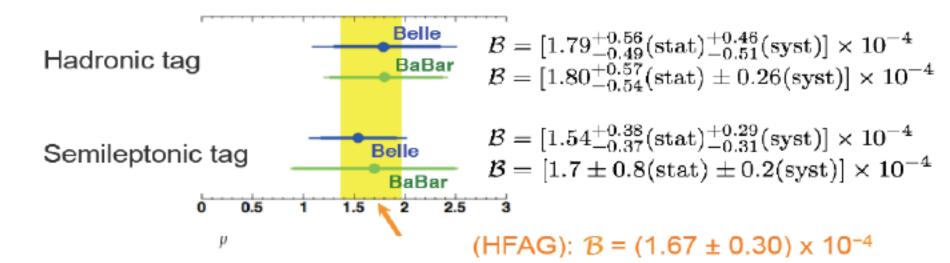
## From a closer look



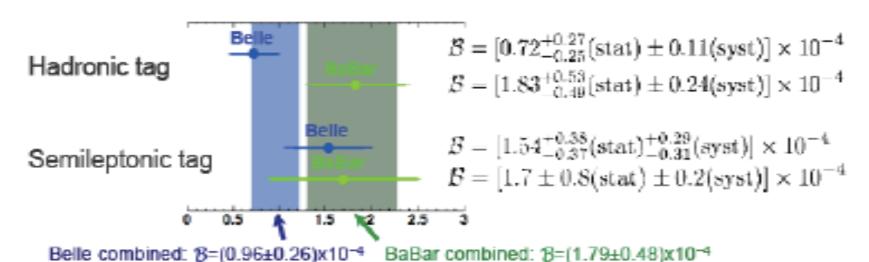
From the UTA (excluding its exp. constraint)

	Prediction	Measurement	Pull
sin2β	0.81±0.05	0.680±0.023	2.4 ←──
γ	68°±3°	76°±11°	<b>&lt;1</b>
α	88°±4°	91°±6°	<1
V <sub>cb</sub>   · 10 <sup>3</sup>	42.3±0.9	41.0±1.0	<1
$ V_{ub}  \cdot 10^3$	3.62±0.14	3.82±0.56	<1
$\epsilon_K \cdot 10^3$	1.96±0.20	2.23±0.01	1.4 ←
BR(B $\rightarrow \tau \nu$ )· 10 <sup>4</sup>	0.82±0.08	1.67±0.30	-2.7 ←──

## Status for B $\rightarrow \tau \nu$ before ICHEP 2012



## Status for B $\rightarrow \tau \nu$ after ICHEP 2012



## Unitarity Triangle analysis in the SM:

obtained excluding the given constraint from the fit

		<u> </u>	
Observables	Measurement	Prediction	Pull (#σ)
sin2β	0.665 ± 0.024	0.757 ± 0.045	~ 1.7
γ	71.1 ± 7.6	68.6 ± 3.3	<1
α	91.1 ± 6.7	87.4 ± 3.6	< 1
[V <sub>ub</sub> ] · 10 <sup>3</sup>	3.82 ± 0.56	3.60 ± 0.14	< 1
[V <sub>ub</sub> ] • <b>10</b> <sup>3</sup> (incl)	4.40 ± 0.31	-	~ 2.2
V <sub>ub</sub>   · 10 <sup>3</sup> (excl)	3.28 ± 0.30	_	~ 1.1
[V <sub>cb</sub> ] · 10 <sup>3</sup>	41.0 ± 1.0	42.8 ± 0.79	~ 1.3
Bĸ	$0.730 \pm 0.30$	0.866 ± 0.086	< 1
BR(B $\rightarrow \tau \nu$ )	0.99 ± 0.25	0.826 ± 0.077	< 1
$BR(B \rightarrow \tau v)(old)$	1.67 ± 0.30	-	~ 2.6

#### From a closer look

UTfit

From the UTA (excluding its exp. constraint)

	Prediction	Measurement	Pull
sin2β	0.81±0.05	0.680±0.023	2.4 ←──
γ	68°±3°	76°±11°	<1
α	88°±4°	91°±6°	<1
V <sub>cb</sub>   · 10 <sup>3</sup>	42.3±0.9	41.0±1.0	<b>&lt;1</b>
V <sub>ub</sub>   · 10 <sup>3</sup>	3.62±0.14	3.82±0.56	<1
ε <sub>K</sub> · 10³	1.96±0.20	2.23±0.01	1.4 ←
BR(B $\rightarrow \tau \nu$ )· 10 <sup>4</sup>	0.82±0.08	1.67±0.30	-2.7 ←
Observables	Measurement	Prediction P	Pull (#σ)
sin2β	$0.665 \pm 0.024$	0.757 ± 0.045	~ 1.7
γ	71.1 ± 7.6	68.6 ± 3.3	< 1
α	91.1 ± 6.7	87.4 ± 3.6	< 1
V <sub>ub</sub>   · 10 <sup>3</sup>	3.82 ± 0.56	3.60 ± 0.14	< 1
$ V_{ub}  \cdot 10^3$ (incl)	4.40 ± 0.31	_	~ 2.2
V <sub>ub</sub>   • 10 <sup>3</sup> (excl)	3.28 ± 0.30	_	~ 1.1
[V <sub>cb</sub> ] · 10 <sup>3</sup>	41.0 ± 1.0	42.8 ± 0.79	~ 1.3 🔸
Вк	$0.730 \pm 0.30$	0.866 ± 0.086	< 1
BR(B $\rightarrow \tau v$ )	0.99 ± 0.25	0.826 ± 0.077	< 1
$BR(B \to \tau v)(old)$	1.67 ± 0.30	-	~ 2.6

## $B \rightarrow D^{(*)} \tau \nu$ from BaBar and SM

$$\mathcal{R}(D)_{\mathrm{exp}} = 0.440 \pm 0.072$$
  $\mathcal{R}(D^*)_{\mathrm{exp}} = 0.332 \pm 0.030$   $2.7\sigma$   $2.7\sigma$   $\mathcal{R}(D)_{\mathrm{SM}} = 0.297 \pm 0.017$   $\mathcal{R}(D^*)_{\mathrm{SM}} = 0.252 \pm 0.003$ 

SM expectations in S. Fajfer, J. Kamenik, I. Nisandzic, PRD 85, 094025 (2012).

## $B \rightarrow D^{(*)} \tau \nu$ from Belle

A. Bozek's averages (KEK-FF 2013):

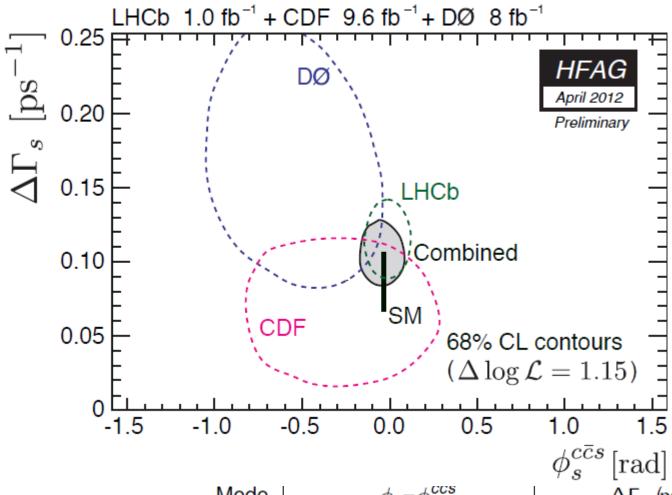
(naive averages for inclusive and exclusive hadronic tags)

$$R(D) = 0.430 \pm 0.091$$
  
 $R(D^*) = 0.405 \pm 0.047$ 

Deviation from SM

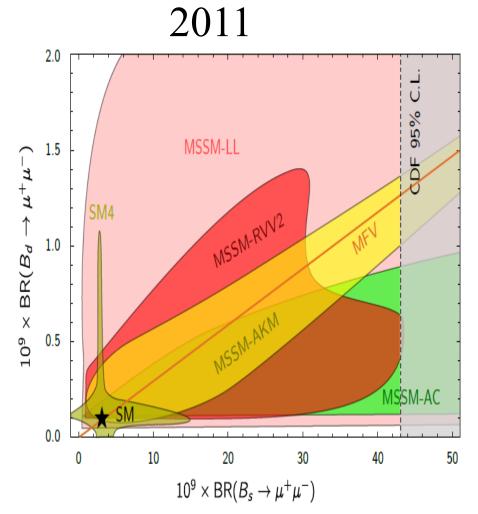
Correlation btw R(D) and R(D\*) neglected conservatively.

### LHCb and CPV in the B<sub>s</sub> decays



Ref.	Mode	$\phi_{\mathcal{S}} = \phi_{\mathcal{S}}^{ccs}$	$\Delta\Gamma_s \text{ (ps}^{-1)}$
CDF Note 10778 (2012)	$J/\psi \phi$	L 2	$0.068 \pm 0.026 \pm 0.007$
DØ, PRD D85 032006 (2012	) $J/\psi \phi$	$-0.55^{+0.38}_{-0.36}$	$0.163^{+0.065}_{-0.064}$
LHCb-CONF-2012-002	$J\!/\!\psi\phi$	$-0.001 \pm 0.101 \pm 0.027$	$0.116 \pm 0.018 \pm 0.006$
LHCb, arXiv:1204.5675		$-0.019^{+0.173+0.004}_{-0.174-0.003}$	_
Combined [HFAG'2012]		$-0.044^{+0.090}_{-0.085}$	$+0.105 \pm 0.015$

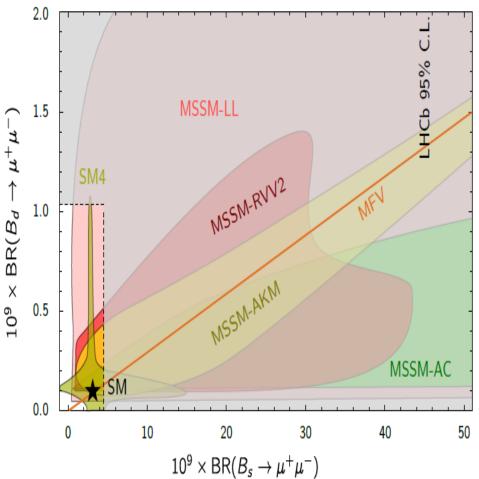
David Straub: arXiv:1205.6094



### 2012

ATLAS, CMS and **LHCb** results combined:

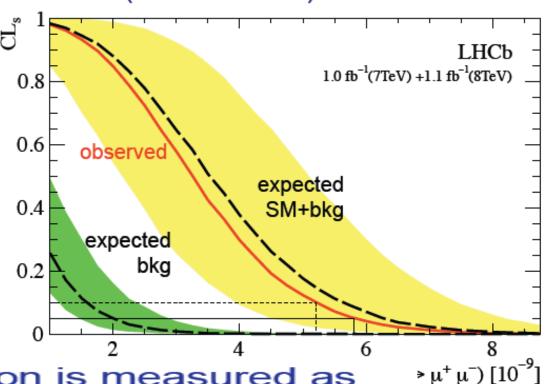
BPH-12-009, ATLAS-CONF-2012-061, LHCb-CONF-2012-017





### Results for $B_s \rightarrow \mu^+\mu^-$ : Limits and significance

- Evaluate compatibility with background only and background+signal hypotheses (CLs method)
  - 2011+2012:
     bkg only p-value:
     5 x 10<sup>-4</sup>
     (corresponds to 3.5σ)
  - 2012 alone
     bkg only p-value:
     9 x 10<sup>-4</sup>
     (corresponds to 3.3 σ)



The branching fraction is measured as

$$BR(B_s \rightarrow \mu^+ \mu^-) = (3.2^{+1.5}_{-1.2}) \times 10^{-9}$$

This is the first evidence of the decay B<sub>s</sub>→ μ<sup>+</sup>μ<sup>-</sup>!



### DIRECT CPV IN $D^0 \rightarrow \pi^+\pi^-, K^+K^-$

**2011:** LHCb, 620 pb<sup>-1</sup> first evidence (3.5  $\sigma$ ) of CPV in charm

$$\Delta A_{CP} = A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-) = (-0.82 \pm 0.21 \pm 0.11)\%$$

**2012**: fom CDF, 9.6 fb<sup>-1</sup>, + LHCb + BELLE

$$\Delta A_{CP} \equiv A_{CP} \left( K^+ K^- \right) - A_{CP} \left( \pi^+ \pi^- \right) = (-0.74 \pm 0.15)\%$$

This result demands an enhancement of the suppressed CKM amplitudes of the SM of a factor approx. 5 – 10 Isidori, Kamenik, Ligeti, Perez 2011

But the charm quark is **TOO HEAVY** to apply the ChPT, while, at the same time, it

is **TOO LIGHT** to trust the Heavy Quark Effective approach : **HENCE IT IS NOT** 

**IMPOSSIBLE** THAT THE **SM** IS ONCE AGAIN FINDING A WAYOUT TO

**SURVIVE!** Golden, Grinstein 1989; Brod, Kagan, Zupan 2011

ON THE OTHER IT REMAINS POSSIBLE THAT NEW PHYSICS IS SHOWING UP... Giudice,

Isidori, Paradisi 2012; Barbieri, Buttazzo, Sala e Straub 2012

### POSSIBLE SURPRISES FROM THE KAON TOO → NA62 ?

### **Experimental update including latest LHCb results**

$$\Delta A_{CP} \equiv A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-)$$
$$= -0.00656 \pm 0.00154.$$

HILLER, HOCHBERG, NIR

$$\Delta A_{CP}^{\rm SUSY} \sim 0.006 \; \frac{\mathcal{I}m(\delta_{LR})}{0.001} \; \frac{1 \; {\rm TeV}}{\tilde{m}}$$

TYPICAL RESULT IN SUSY MODELS WITH FLAVOR SYMMETRIES AND ACCOUNTING FOR  $M_H = 125 \text{ GeV} \rightarrow \Delta_{CP} \sim 0.001$  but there could be some accidental enhancement of O(1)

#### Ten Years Ago → Today L.Lellouch ICHEP 2002 UTA Lattice inputs 2012 Hadronic parameter [hep-ph/0211359] [www.utfit.org] $\hat{\mathbf{B}}_{K}$ 0.86(15) [17%] 0.75(2)[3%] $f_{Bs}$ 238(31) MeV [13%] 233(10) MeV [4%] [1.5%]

On the Lattice side:

**TARANTINO ICHEP2012** 

 $f_{Bs}/f_{B}$ [6%] 1.20(2) 1.24(7) Â<sub>Bs</sub> 1.34(12) [9%] 1.33(6) [5%]

1.00(3) [3%]  $B_{Bs}/B_{B}$ 1.05(7)

[7%] (quenched,  $\mu_1 > m_s/2,...$ )  $F_{D*}(1)$ 0.91(3) [3%] [2%] 0.92(2)

[20%] [11%]

 $\mathsf{F}_{\centerdot}^{\mathsf{B} o \pi}$ The last 10 years teach us that Lattice QCD has made important progresses (quenched->unquenched, higher computational power, better algorithms) More recently further improvements are being realized: simulations at the physical point, discretization effects well under control (in the light and heavy sectors),  $N_f=2+1+1$ , ...

### **Expected Progress**

Now 8 rulexch & Vch exil EXPECTATIONS DEUSACD COOL

### **SUSY GUTS**

• UV COMPLETION OF THE SM TO STABILIZE THE ELW. SCALE:

LOW-ENERGY SUSY TREND OF
UNIFICATION OF THE
SM GAUGE
COUPLINGS AT HIGH
SCALE:

**GUTs** 

### **GUT-RELATED SUSY SOFT BREAKING TERMS**

$$\begin{split} m_Q^2 &= m_{\tilde{e^c}}^2 = m_{\tilde{u^c}}^2 = m_{10}^2 \\ m_{\tilde{d^c}}^2 &= m_L^2 = m_{\overline{5}}^2 \\ A_{ij}^e &= A_{ji}^d \,. \end{split}$$

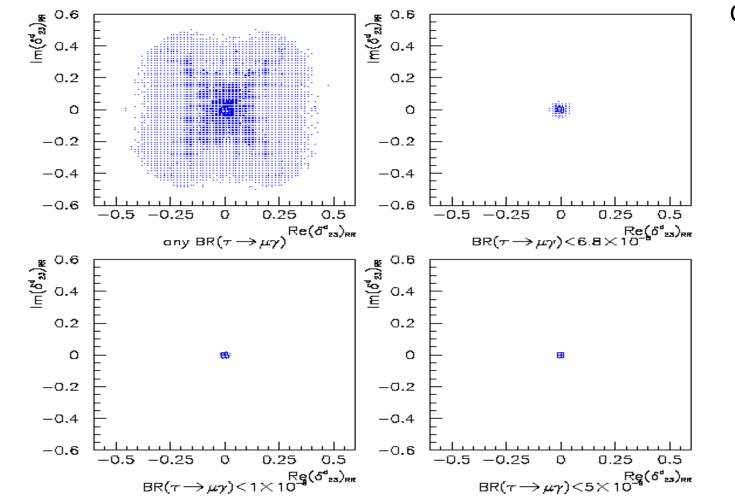
SU(5) RELATIONS

	Relations at weak-scale	Relationss at $M_{\rm GUT}$
(1)	$(\delta^u_{ij})_{\mathrm{RR}}~\approx~(m^2_{e^c}/m^2_{u^c})~(\delta^l_{ij})_{\mathrm{RR}}$	$m_{u^c_0}^2 = m_{e^c_0}^2$
(2)	$(\delta_{ij}^q)_{ m LL} \approx (m_{e^c}^2/m_Q^2) (\delta_{ij}^l)_{ m RR}$	$m_{Q_0}^2 = m_{e^c_0}^2$
(3)	$(\delta^d_{ij})_{\mathrm{RR}}~pprox~(m_L^2/m_{d^c}^2)~(\delta^l_{ij})_{\mathrm{LL}}$	$m_{d^c_0}^2 = m_{L_0}^2$
(4)	$(\delta_{ij}^d)_{ m LR} \approx (m_{L_{avg}}^2/m_{Q_{avg}}^2) (m_b/m_{ au}) (\delta_{ij}^l)_{ m LR}^{\star}$	$A^e_{ij_0} = A^d_{ji_0}$

# FCNC HADRON-LEPTON CONNECTION IN SUSYGUT

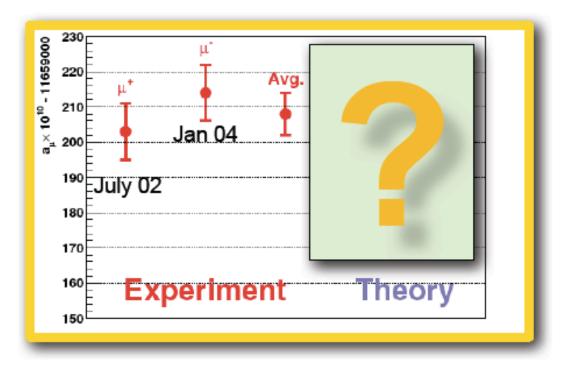
Ciuchini, A.M., Silvestrini, Vempati, Vives PRL general analysis Ciuchini, A.M., Paradisi, Silvestrini, Vempati, Vives

# Bounds on the hadronic $(\delta_{23})_{RR}$ as modified by the inclusion of the LFV correlated bound



**CMPSVV** 

#### The muon g-2: the experimental result



- **Today:**  $a_{\mu}^{EXP} = (116592089 \pm 54_{stat} \pm 33_{sys})x10^{-11}[0.5ppm].$
- Future: new muon g-2 experiments proposed at:
  - Fermilab (E989), aiming at 0.14ppm →
  - J-PARC aiming at 0.1 ppm

Sep 2012: CD0 approval! Data in 2016?

See B. Lee Roberts & T. Mibe @ Tau2012, September 2012

Are theorists ready for this (amazing) precision? No(t yet)

#### The muon g-2: SM vs. Experiment

# Adding up all contributions, we get the following SM predictions and comparisons with the measured value:

$$a_{\mu}^{EXP}$$
 = 116592089 (63) x 10<sup>-11</sup>

E821 – Final Report: PRD73 (2006) 072 with latest value of  $\lambda = \mu_{\mu}/\mu_{p}$  from CODATA'06

$a_{\mu}^{\scriptscriptstyle \mathrm{SM}} \times 10^{11}$	$\Delta a_{\mu} = a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}}$	σ
116 591 794 (66)	$295~(91)\times 10^{-11}$	3.2 [1]
116 591 814 (57)	$275~(85)\times 10^{-11}$	3.2 [2]
116 591 840 (58)	$249~(86)\times 10^{-11}$	2.9 [3]

with the "conservative"  $a_{\mu}^{HHO}(IbI) = 116 (39) \times 10^{-11}$  and the LO hadronic from:

- [1] Jegerlehner & Nyffeler, Phys. Rept. 477 (2009) 1
- [2] Davier et al, EPJ C71 (2011) 1515 (includes BaBar & KLOE10 2π)
- [3] Hagiwara et al, JPG38 (2011) 085003 (includes BaBar & KLOE10  $2\pi$ )

Note that the th. error is now about the same as the exp. one

### THE EDM CHALLENGE

FOR ANY NEW PHYSICS AT THE TEV SCALE WITH NEW SOURCES OF CP VIOLATION → NEED FOR FINE-TUNING TO PASS THE EDM TESTS OR SOME DYNAMICS TO SUPPRESS THE CPV IN FLAVOR CONSERVING EDMS

$$|d_{\rm n}| < 2.9 \times 10^{-26} e \text{ cm } (90\%\text{C.L.}),$$
  
 $|d_{\rm Tl}| < 9.0 \times 10^{-25} e \text{ cm } (90\%\text{C.L.}),$   
 $|d_{\rm Hg}| < 3.1 \times 10^{-29} e \text{ cm } (95\%\text{C.L.}).$ 

# Some thoughts on the "flavor path" to TeV New Physics

- Out of the 3 traditional theoretical shortcomings of the SM: i) lack of true unification; ii) gauge hierarchy; iii) no explanation for the fermion masses and mixings (flavor question within the SM), this latter issue is the one with the least progress in the last decades (we still completely lack a flavor theory unfortunately the (very) good knowledge of the CKM structure has not helped us much in this direction
- Today question: with all the existing constraints, how can it be that NP shows up only in very specific "corners" that we have not experimentally probed yet? The lack of a flavor theory tells us that what we consider unlikely "coincidences" may be just a fruit of such ignorance (think of finding  $\rho = 1$  without knowing the ELW gauge theory)
- In my view, in this moment of relevance of the "virtuality" as a gate to access NP, the flavor path remains imporatnt: SLOW DECOUPLING OF NEW PHYSICS IN VIRTUAL EFFECTS W.R.T. PHYSICAL PRODUCTS

# A FUTURE FOR FLAVOR PHYSICS IN OUR SEARCH BEYOND THE SM?

- COMPLEMENTARITY between direct and indirect searches for New Physics is the key-word
- Twofold meaning of such complementarity:
- i) synergy in "reconstructing" the "fundamental theory" staying behind the signatures of NP;
- ii) coverage of complementary areas of the NP parameter space (ex.: multi-TeV SUSY physics)

SLOWER DECOUPLING OF NEW PHYSICS IN VIRTUAL EFFECTS W.R.T. PHYSICAL EFFECTS → FCNC SENSITIVITY TO NEW PARTICLE MASSES IN THE TENS OF TEV

# **SOME FINAL THOUGHTS** ... (in particular dedicated to the young researchers present here)

"A special search at Dubna was carried out by E. Okonov and his group. They did not find a single  $K_L \rightarrow \pi^+ \pi^-$  event among 600 decays into charged particles [12] (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the Lab. The group was unlucky."

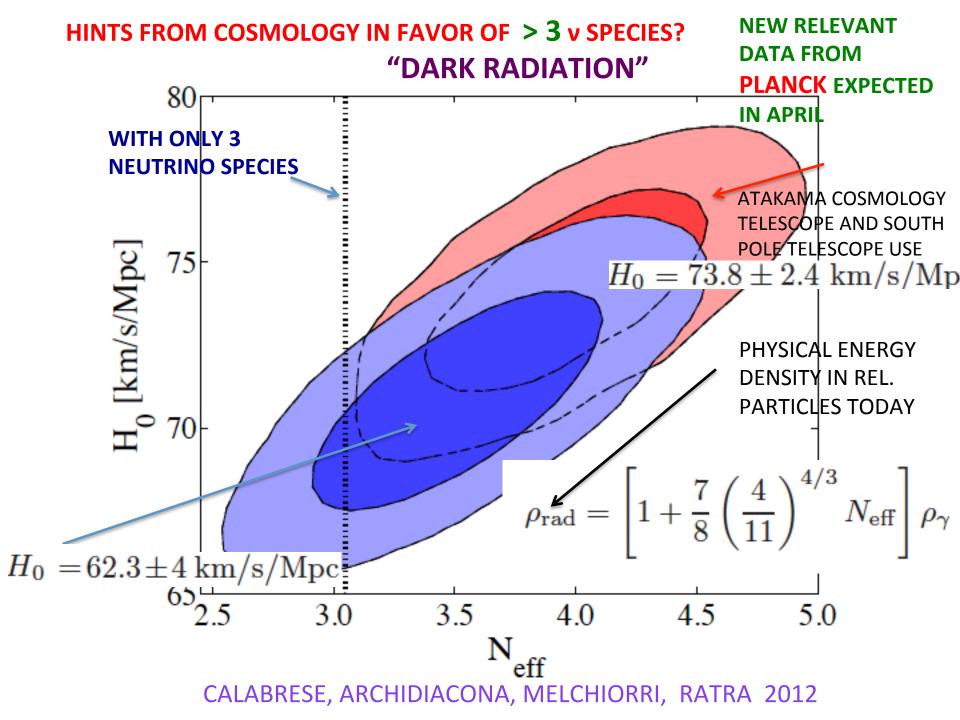
-Lev Okun, "The Vacuum as Seen from Moscow"

1964: BF= 2 x 10<sup>-3</sup> Christenson, Cronin, Fitch, Turlay BNL '64

Early '80s ... "neutrinos should have a mass < few eV; this would be ridiculously small even compared to the lightest fermion mass — that of the electron — neutrinos have to be massless and a symmetry should guarantee it" ....

I'm convinced that FLAVOR PHYSICS CAN STILL RESERVE IMPORTANT SURPRISES...

# BACKUP SLIDES



# Limit on the SUM of the v masses from COSMOLOGY

- WMAP 7yr
- SDSS III 8th data release
- Hubble space telescope H

R. De Putter et al, arXiv: 1201.1909 [astro-ph.CO]

 $\Sigma \, \text{m} < 0.26 \, \text{eV} \, (95 \% \, \text{CL})$ 

Conservative bias

 $\Sigma \, \text{m} < 0.36 \, \text{eV} \, (95 \% \, \text{CL})$ 

Bounds presented at ICHEP 2012

- WMAP 7yr
- Observable Hubble parameter data (OHD)
- $H_0$  (in correlation with  $\sigma_8$ )

 $\Sigma m < 0.24 \text{ eV } (68 \% CL)$ 

M. Moresco, et al., arXiv:1201.6658 [astro-ph.CO]

Future:  $\sum m <$ 

 $\Sigma$  m < 0.08 eV

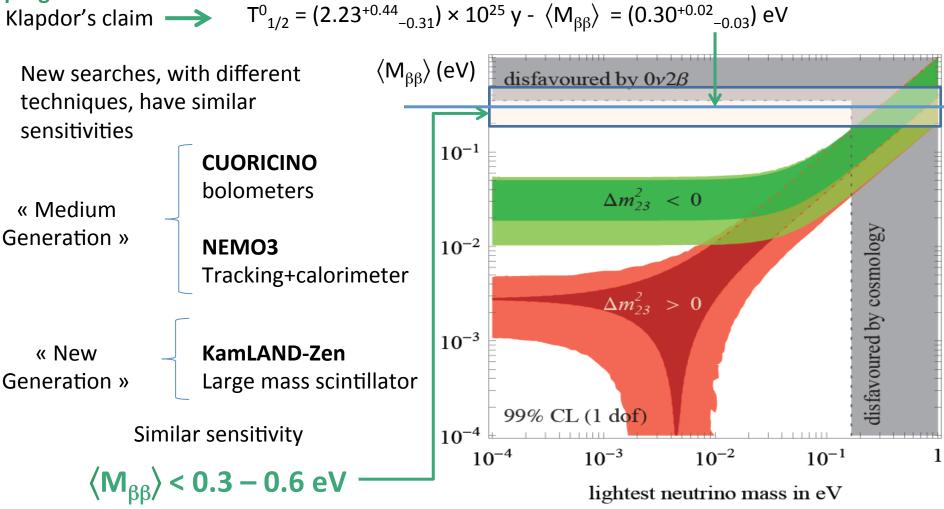
### **Double beta decay: status**

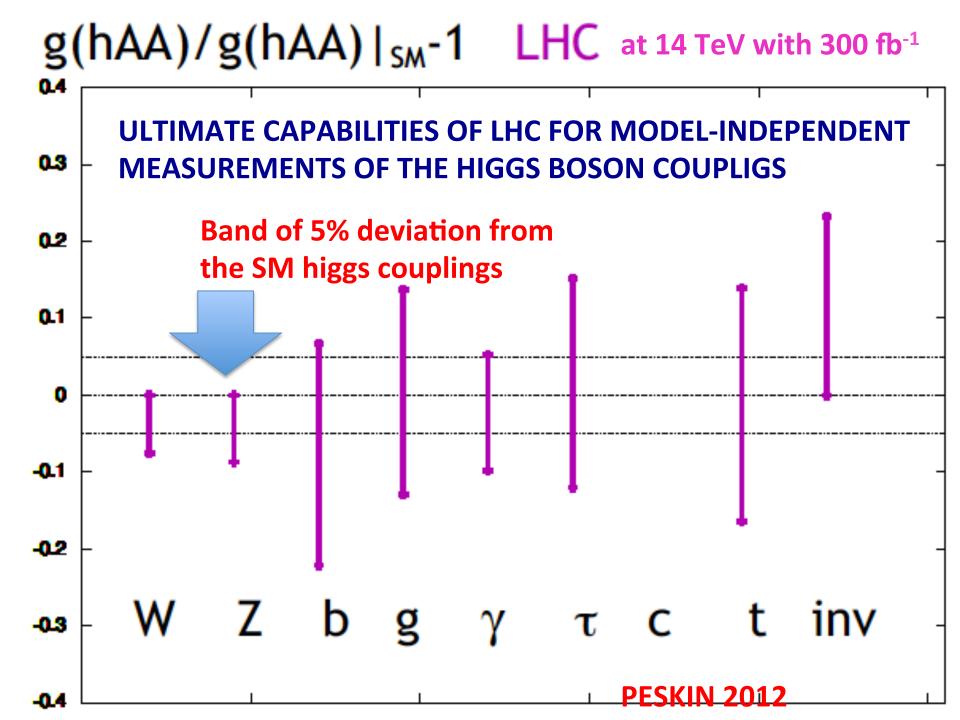
**GIULIANI IFAE2012** 

In 1998, when neutrino flavour oscillations were discovered, the « old-generation » **Heidelberg-Moscow** experiment (<sup>76</sup>Ge, Ge diodes) was leading in terms of sensitivity.

Today, it is still the most sensitive experiment in 0v-DBD  $\longrightarrow$  Difficult subject, slow

#### progresses





### LC at $\sqrt{s} = 250 \text{ GeV}$ : a HIGGS FACTORY

- Expected O(10<sup>5</sup>) Higgs bosons for ~ 250 fb<sup>-1</sup>
- Accuracies on Higgs couplings for M<sub>H</sub> = 125 GeV (on individual couplings and not only on products of production cross section × BR)

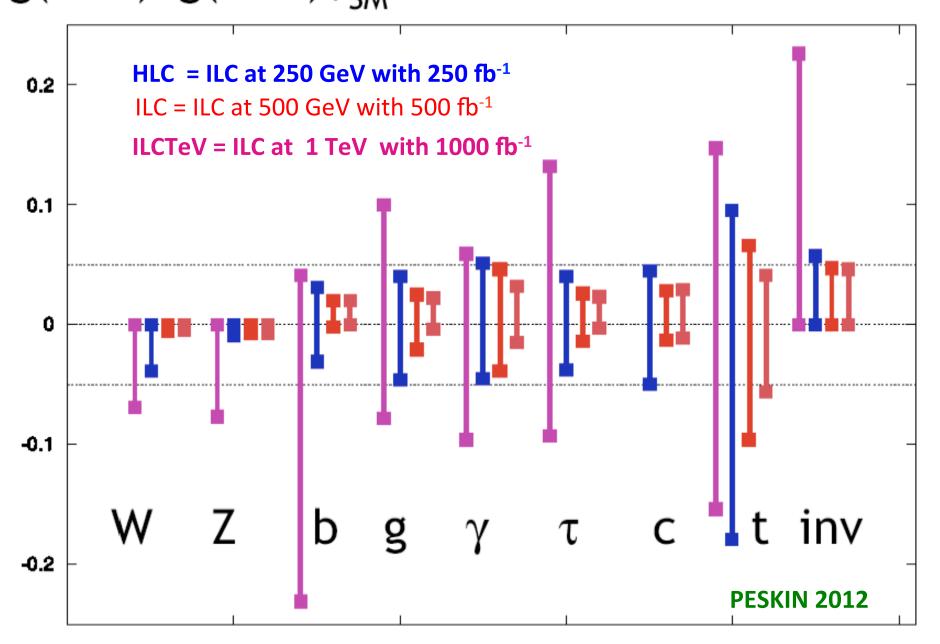
g / BR	$g_{HWW}$	$g_{HZZ}$	$g_{Hbb}$	$g_{Hcc}$	$g_{H au au}$	$g_{Htt}$	9ннн	$BR(\gamma\gamma)$	BR(gg)	BR(invis.)
Precision	1.4 %	1.4 %	1.4 %	2.0 %	2.5 %	15 %	40 %	15 %	5 %	0.5 %

Baer et al., ILC Detailed Baseline Design report 2012

PRECISION ON THE MEASUREMENT OF  $M_H$ : 0.03%

**Probing additional non-SM-like Higgs bosons**: the 125 GeV Higgs could be the second lightest Higgs in the spectrum → lighter Higgs (maybe below the LEP limit for a SM-like Higgs) with reduced couplings to gauge bosons

## g(hAA)/g(hAA)|<sub>SM</sub>-1 LHC/ILC1/ILC/ILCTeV



## e<sup>+</sup>e<sup>-</sup> Collider Summary

Accelerator	LHC	HL-LHC	ILC (250)	ILC	LEP3	TLEP
→Physical	300fb <sup>-1</sup> /exp	3000fb <sup>-1</sup>	250 fb <sup>-1</sup>	(250+350+1000)	240	240 +350
quantity $\downarrow$		/exp			4 IP	4 IP
Approx. date	2021	2030	2035	2045	2035	2035
N <sub>H</sub>	1.7 x 10 <sup>7</sup>	1.7 x 10 <sup>8</sup>	5 10⁴ZH	(10 <sup>5</sup> ZH)	4 10 <sup>5</sup> ZH	2 10 <sup>6</sup> ZH
				(1.4 10 <sup>5</sup> Hvv)		
m <sub>H</sub> (MeV)	100	50	35	35	26	7
$\Delta\Gamma_{\text{H}}/\Gamma_{\text{H}}$			10%	3%	4%	1.3%
$\Delta\Gamma_{\text{inv}}/\Gamma_{\text{H}}$	Indirect	Indirect	1.5%	1.0%	0.35%	0.15%
	(30%?)	(10% ?)				
$\Delta g_{H\gamma\gamma}/g_{H\gamma\gamma}$	6.5 - 5.1%	5.4 – 1.5%		5%	3.4%	1.4%
$\Delta g_{Hgg}/g_{Hgg}$	11 - 5.7%	7.5 - 2.7%	4.5%	2.5%	2.2%	0.7%
$\Delta g_{Hww}/g_{Hww}$	5.7 – 2.7%	4.5 – 1.0%	4.3%	1%	1.5%	0.25%
$\Delta g_{HZZ}/g_{HZZ}$	5.7 – 2.7%	4.5 – 1.0%	1.3%	1.5%	0.65%	0.2%
Δg <sub>ннн</sub> /g <sub>ннн</sub>		< 30%		~30%		
		(2 exp.)				
	20	-10			4.40/	70/
$\Delta g_{H\mu\mu}/g_{H\mu\mu}$	<30	<10			14%	7%

### **HOW MUCH PRECISION IS NEEDED?**

(references in arXiv:1208.5152)
M. Peskin, Theoretical Summary Lecture for Higgs Hunting 2012 Examples:

Supersymmetry:

$$g(\tau)/SM = 1 + 10\% \left(\frac{400 \text{ GeV}}{m_A}\right)^2$$

$$g(b)/SM = g(\tau)/SM + (1-3)\%$$

Little Higgs:

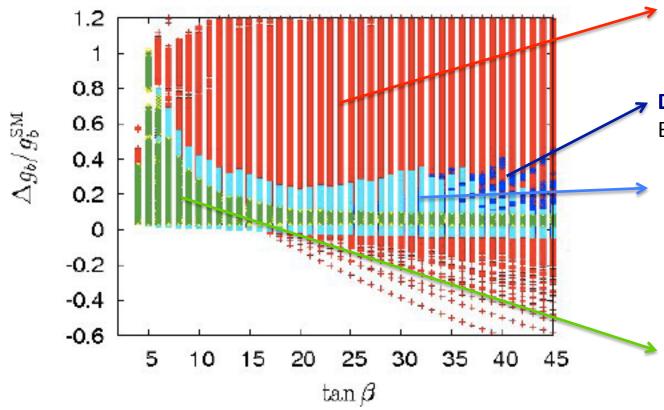
$$g(g)/SM = 1 + (5 - 9)\%$$

$$g(\gamma)/SM = 1 + (5-6)\%$$

Composite Higgs:

$$g(f)/SM = 1 + (3-9)\% \cdot \left(\frac{1 \text{ TeV}}{f}\right)^2$$

roughly 3 TeV in new particle masses for the most sensitive deviations.



**RED**: several Higgses are discovered at LHC

**DARKBLUE**: excluded by BR (b  $\rightarrow$ sy) constraint

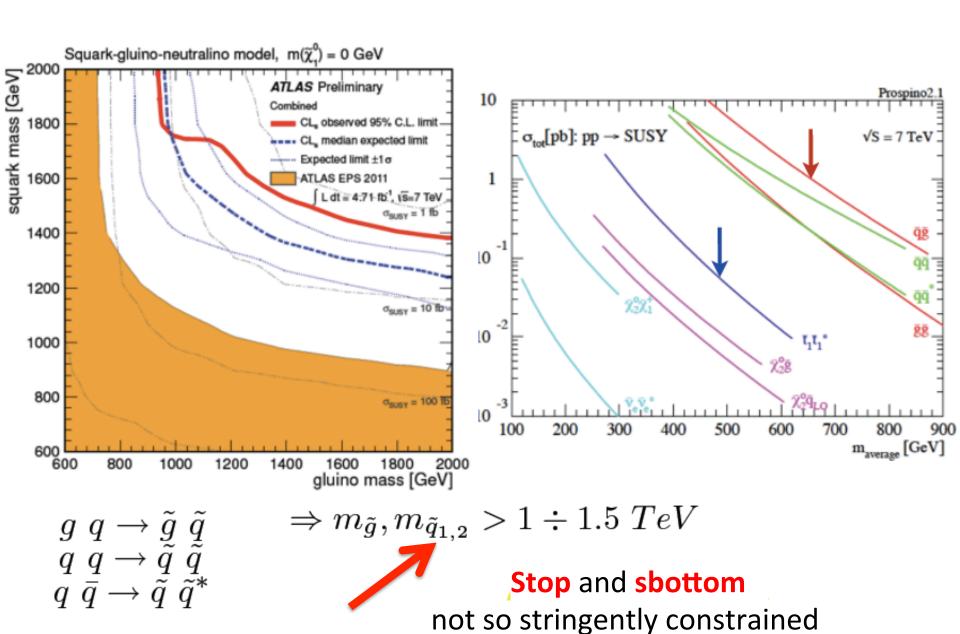
LIGHTBLUE: at least one stop has mass < 1 TeV

**GREEN**: both top squarks are heavier than 1.5 TeV

	$\Delta hVV$	$\Delta h ar t t$	$\Delta hbb$
Mixed-in Singlet	6%	6%	6%
Composite Higgs	8%	tens of $\%$	tens of $\%$
Minimal Supersymmetry	< 1%	3%	$10\%^a, 100\%^b$
LHC $14 \mathrm{TeV},3\mathrm{ab}^{-1}$	8%	10%	15%

GUPTA, RZEHAK, WELLS 2012

### IS LOW-ENERGY SUSY STILL ALIVE?

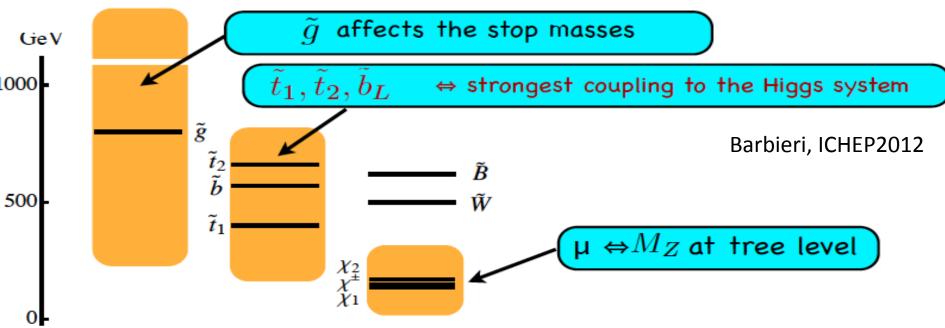


### **NATURAL SUSY**

### LOW-ENERGY SUSY to cope with the gauge hierarchy

problem: only the SUSY particles involved in the cancellation of the quadratic div. to the Higgs mass have to remain "light"

"s-particles at their naturalness limit"



orange areas indicative and dependent on how the Higgs boson gets its mass  $ilde{B}, ilde{W}$  not much constrained but expected below  $m_{ ilde{q}}$ 



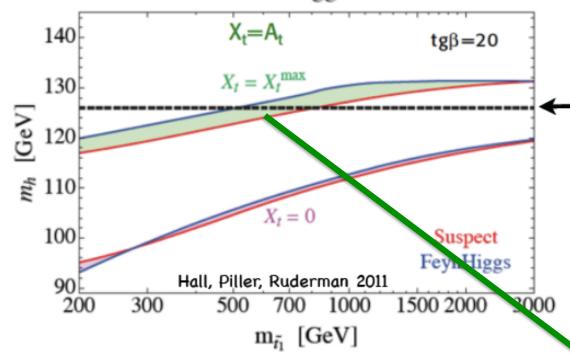
# COPING WITH A HIGGS MASS OF 125 GEV?

the two players to raise the Higgs mass

$$m_h^2 \approx m_Z^2 \cos^2 2\beta + \frac{3}{(4\pi)^2} \frac{m_t^4}{v^2} \left[ \ln \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$



#### MSSM Higgs Mass



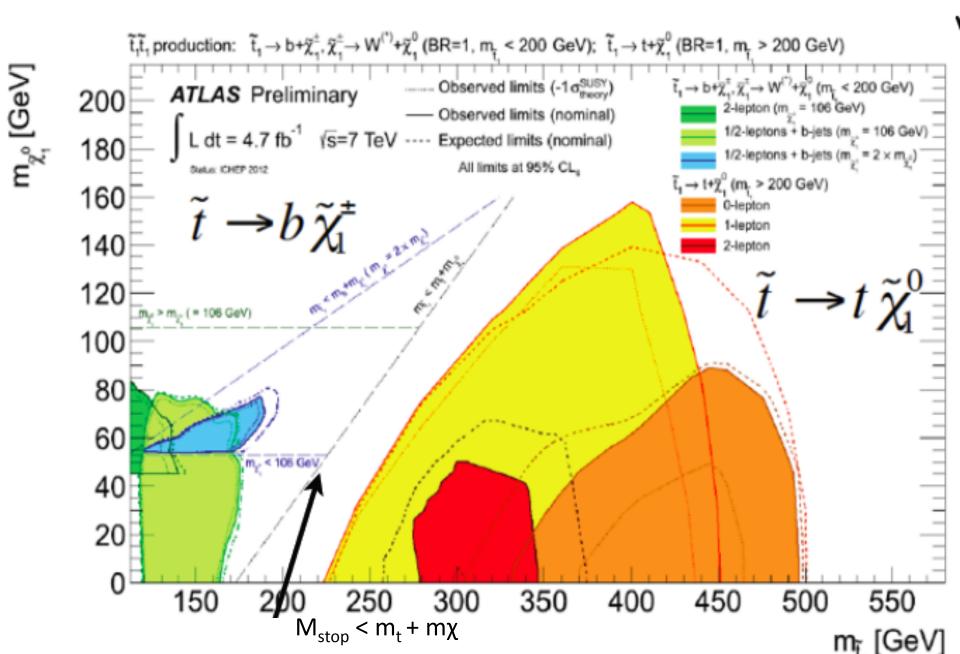
POSSIBLE TO HAVE A LIGHT STOP IF ONE MOVES FROM THE MSSM TO THE

### **NMSSM**

WITH ONE ADDITIONAL SINGLET

Possible for the MSSM to have a light Higgs of mass=125 GeV, but need for **not so light stop** 

### Hunting for a light s-top



SM 6 NN 10+

FORWARD-BACKWARD TOP ASY

Observable	Values	Experiment
$\mathcal{A}_{FB}^t$	$0.19 \pm 0.065$	DØ Collaboration [1]
	$0.158 \pm 0.074$	CDF Collaboration [2]
	$0.176 \pm 0.05$	Combined
$\mathcal{A}_{FB}^{t,low}$	$0.078 \pm 0.048$	DØ Collaboration [1]
10.75	$-0.022 \pm 0.043$	CDF Collaboration [2]
	$0.023 \pm 0.032$	Combined
$\mathcal{A}_{FB}^{t,high}$	$0.115 \pm 0.060$	DØ Collaboration [1]
100	$0.266 \pm 0.062$	CDF Collaboration [2]
	$0.188 \pm 0.043$	Combined
$\sigma_{tar{t}}^{Tevatron}$	8.18 <sup>+0.98</sup> <sub>-0.87</sub> pb	DØ Collaboration [8]
$\sigma^{LHC}_{l^{\pm}l^{\pm}}$	< 1 fb	ATLAS & CMS Collaborations [9]

Table 1: Measured values of various observables used in our analysis; combined here mea weighted averages.

V. Ahrens, A. Ferroglia, M. Neubert, B. D. Pecjak and L. L. Yang, JHEP 1009, 097 (2010) [arxiv:1003.5827 [hep-ph]]. Atwood, Gupta, AS, arXiv1301.2250

Berger et al 1101.5625

Aguilar-Saavedra, Perez-Victoria, 1104.1385 Degrande et al 1104.1798