

# BBN constraints on MeV-scale dark sectors: Sterile decays.

based on

arXiv:1712.03972

[Marco Hufnagel](#), Kai Schmidt-Hoberg, Sebastian Wild

Wednesday, May 23, 2018

# Big Bang Nucleosynthesis

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- Formation of light nuclei in the early phase of the universe

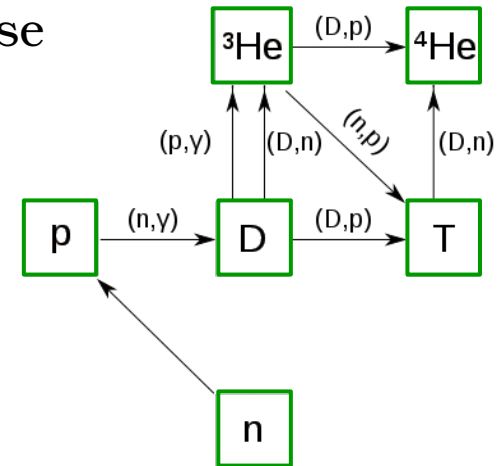
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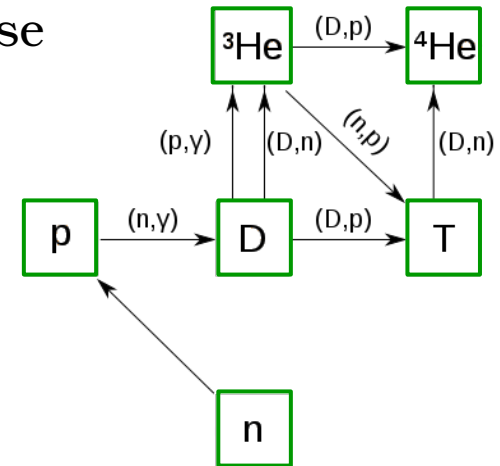


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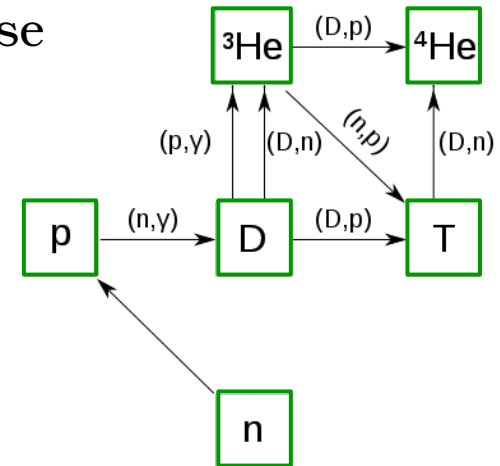
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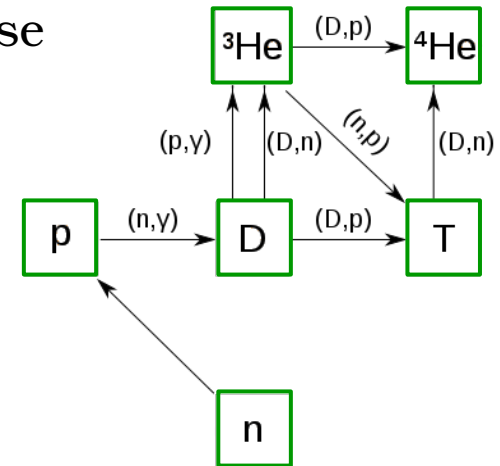
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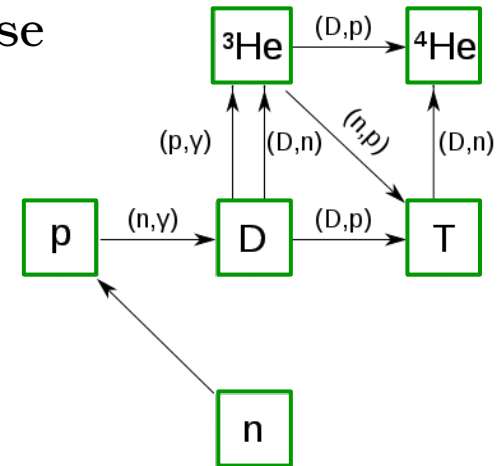
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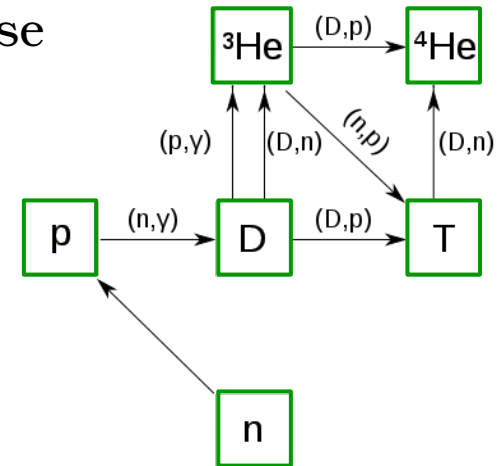
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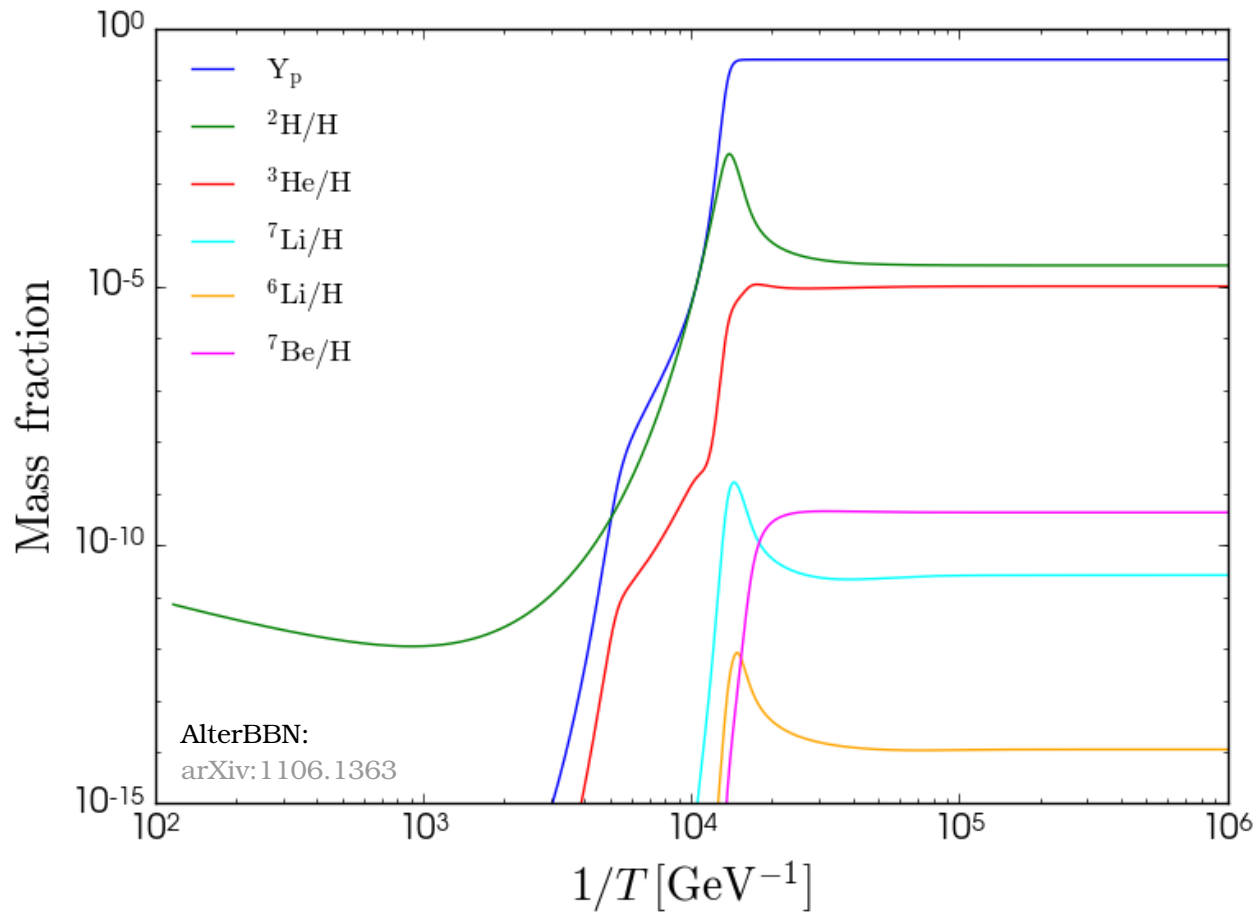
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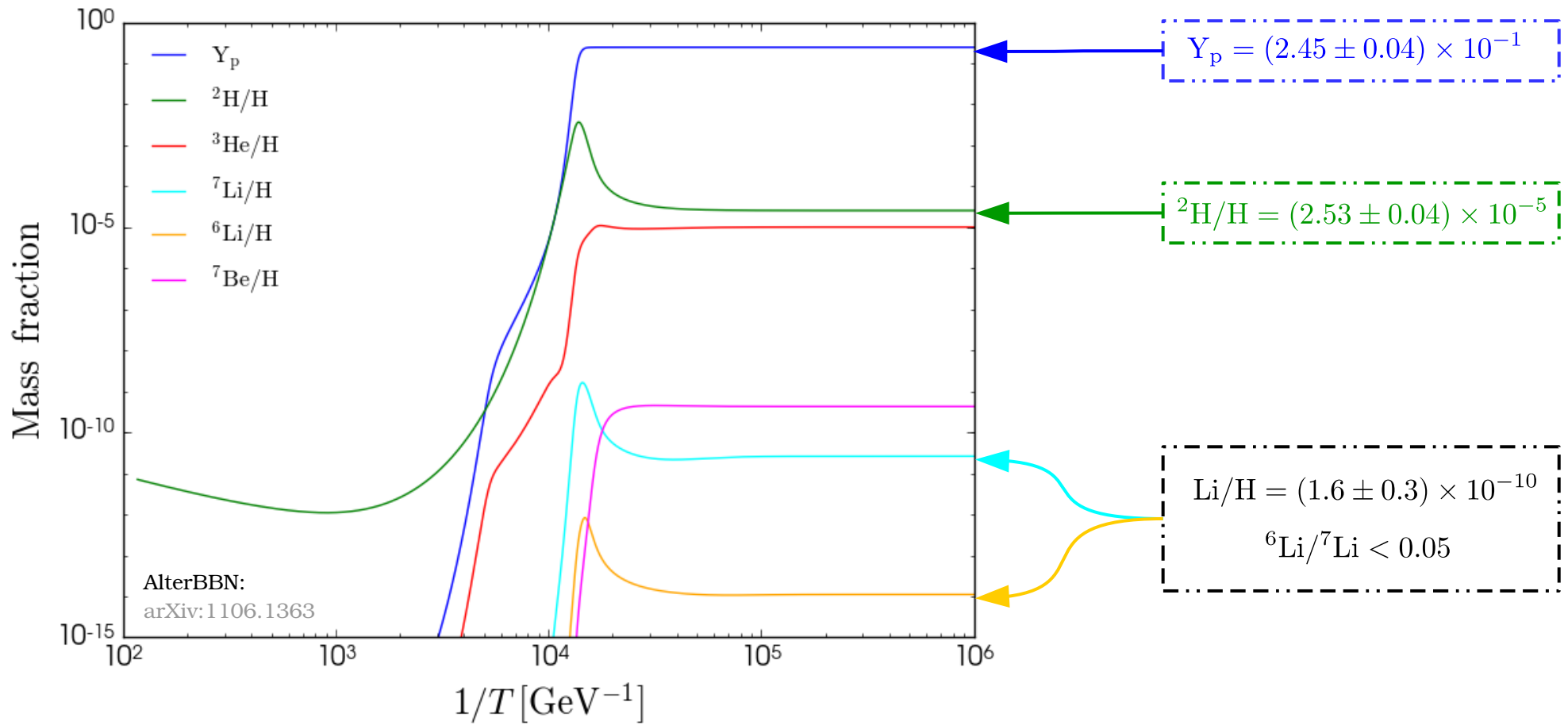
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# Evolution of the abundances during BBN

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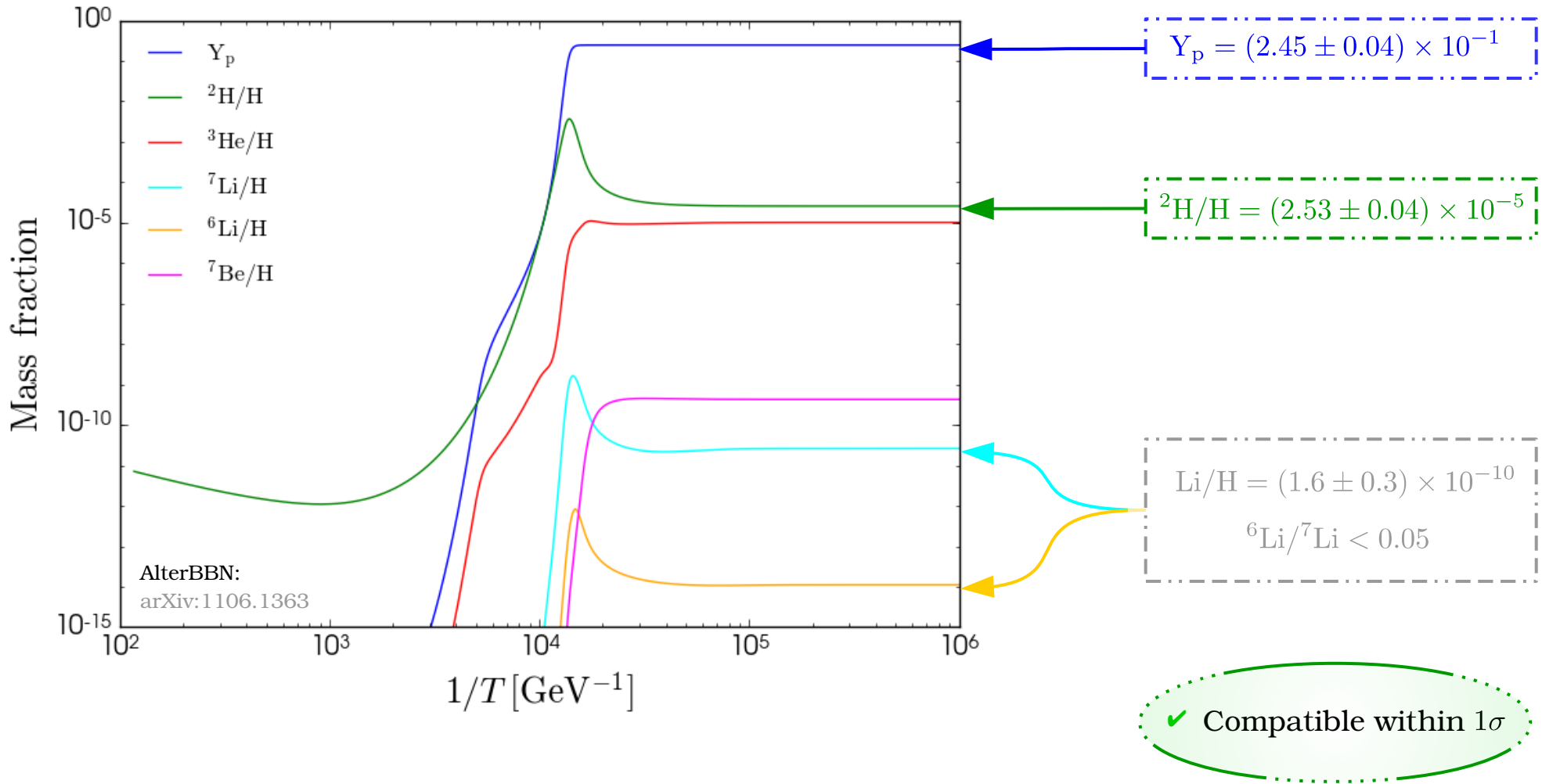
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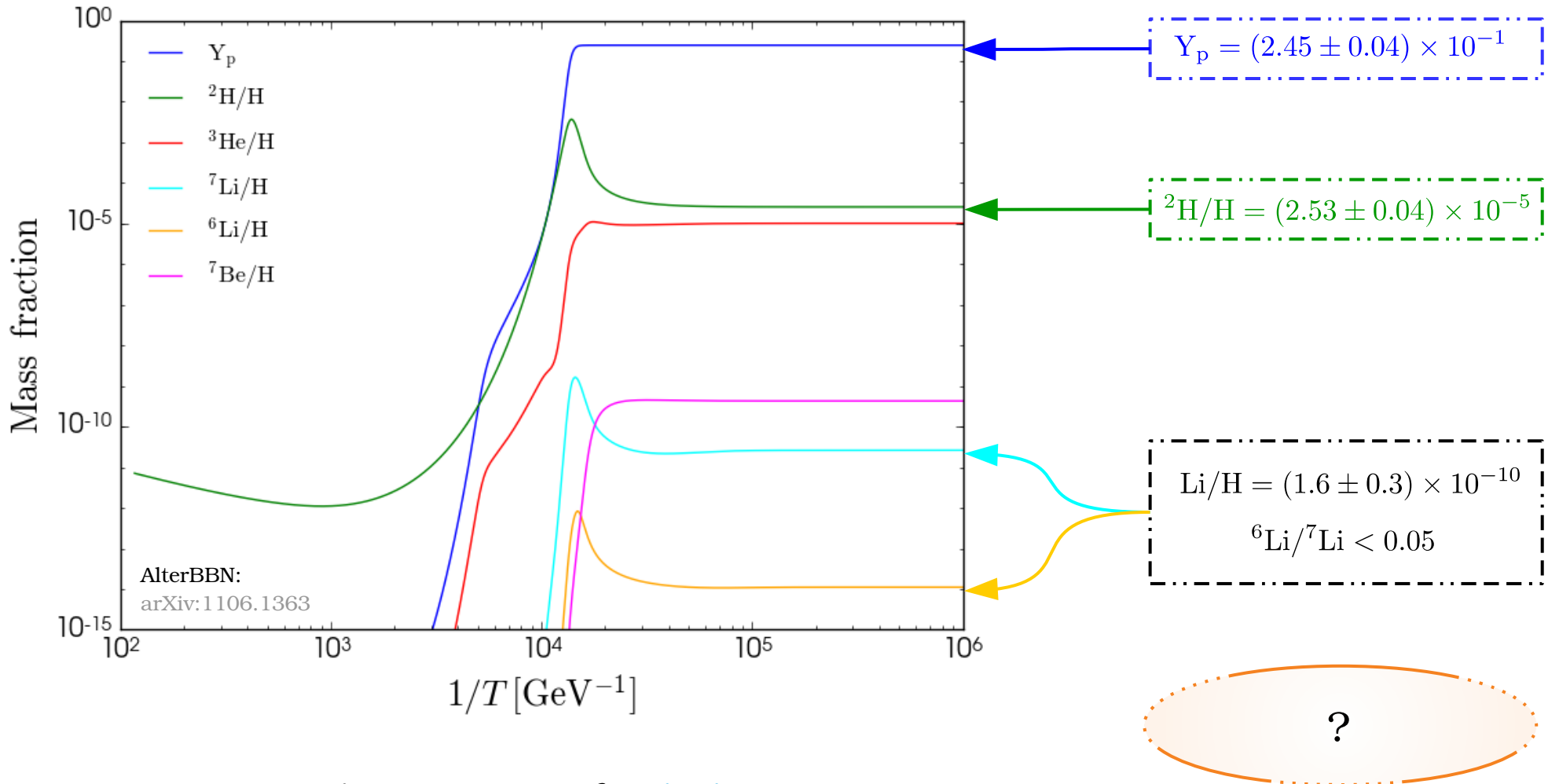
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However: In the presence of a [dark sector](#):

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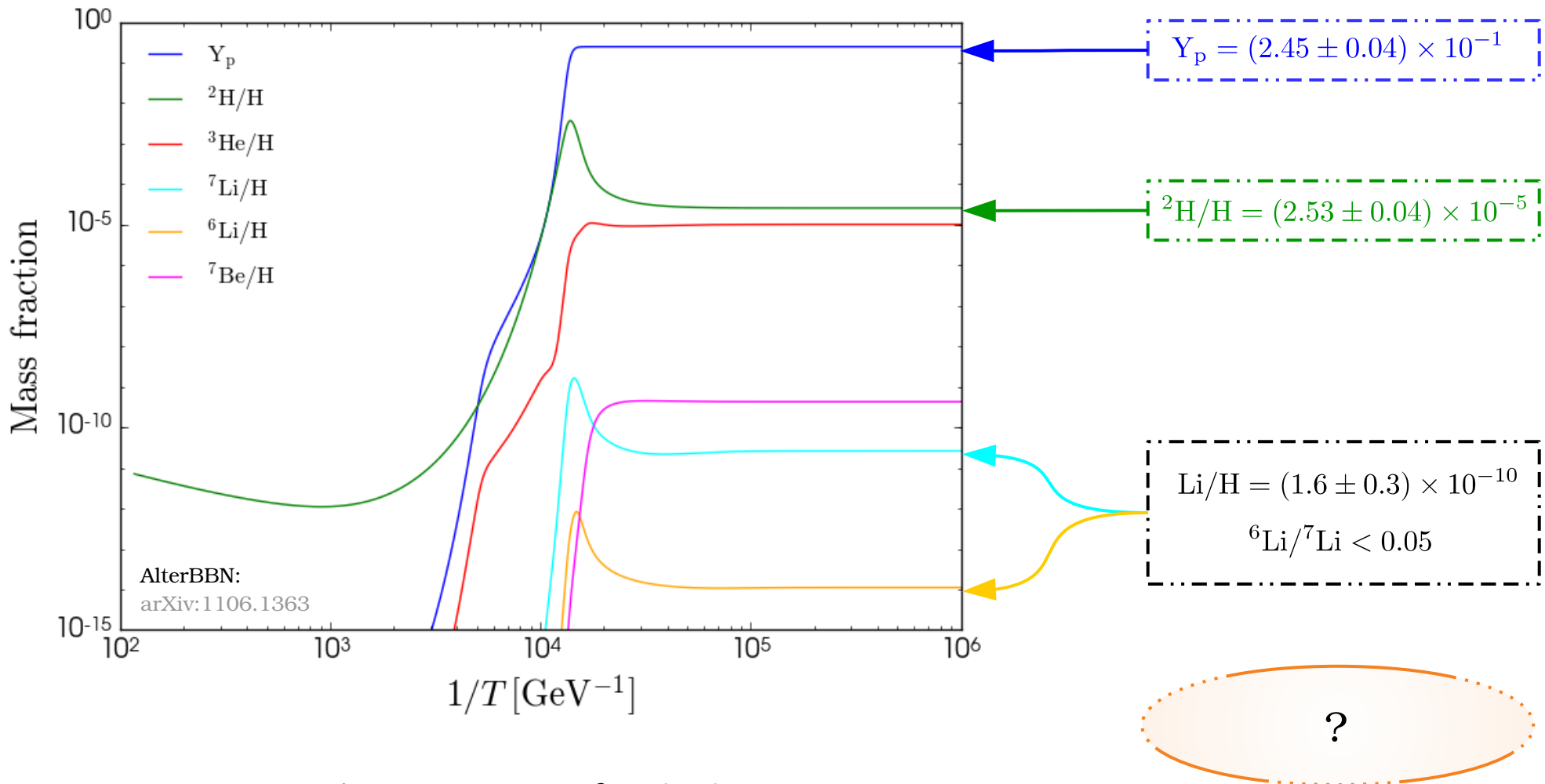
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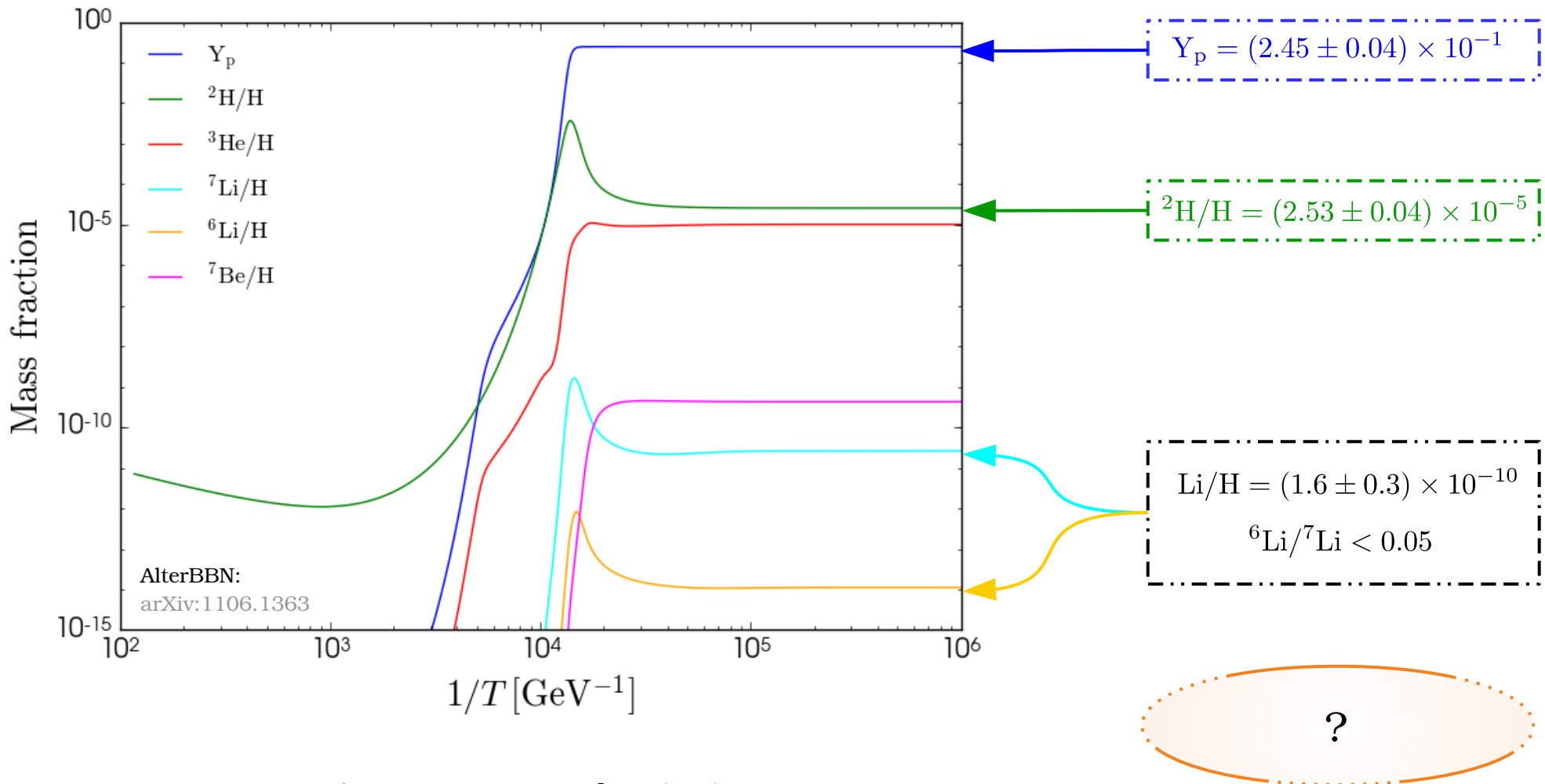
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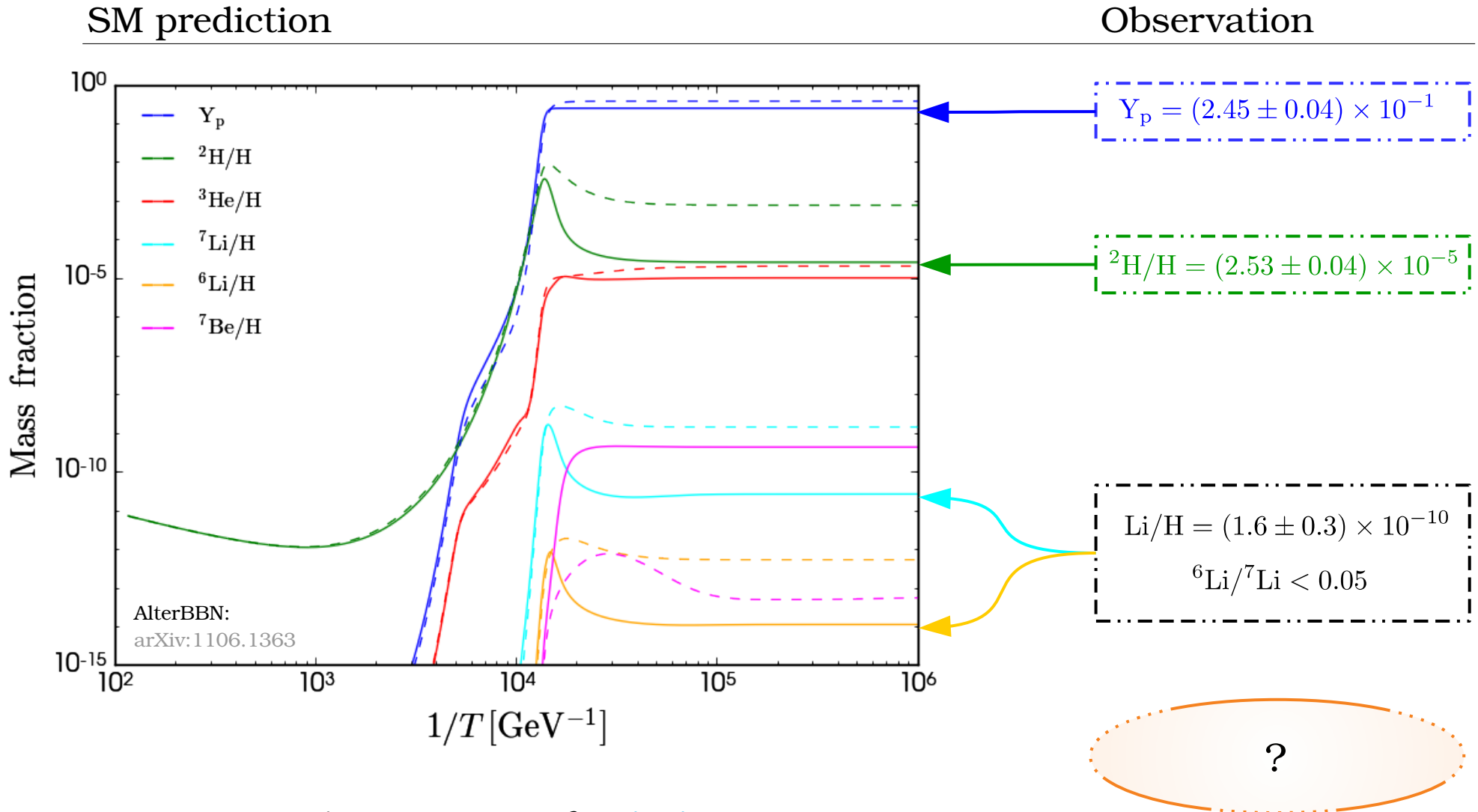
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$m_X \ll \text{MeV}$	$0.01\text{MeV} \lesssim m_X \lesssim 10\text{MeV}$	$m_X \sim 10 - 100\text{MeV}$



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# Setup and Assumptions

Particle content:

Dark Matter	$\chi, \bar{\chi}$	$m_\chi \sim \mathcal{O}(\text{GeV})$
Mediator	$\phi$	$m_\phi \sim \text{MeV}$
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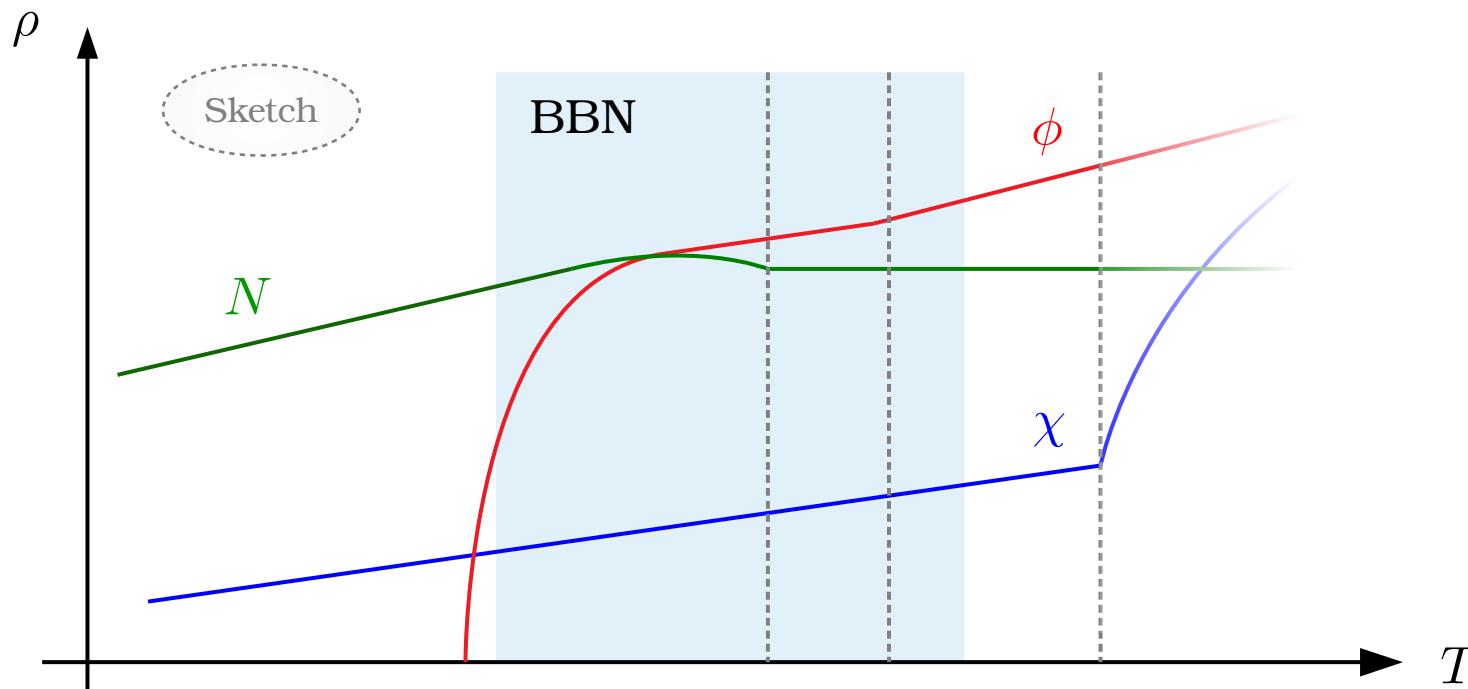
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# Thermal evolution of the dark sector

Boltzmann equation for the mediator  $\phi$  :

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Dilution



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$$\frac{\partial f_\phi}{\partial t} = \underbrace{H p \frac{\partial f_\phi}{\partial p}}_{\text{Dilution}} - \underbrace{\frac{1}{\tau_\phi} \frac{m_\phi}{E} f_\phi}_{\text{Decay}}$$

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$$\frac{\partial f_\phi}{\partial t} = \underbrace{Hp \frac{\partial f_\phi}{\partial p}}_{\text{Dilution}} - \underbrace{\frac{1}{\tau_\phi} \frac{m_\phi}{E} f_\phi}_{\text{Decay}}$$

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$$f_\phi(p, t) = \left[ \exp \left( \frac{\sqrt{m_\phi^2 + p^2 (R_{\text{cd}}/R)^2}}{T_D(t_{\text{cd}})} \right) + 1 \right]^{-1} \exp \left( -\frac{t - t_{\text{cd}}}{\tau_\phi} \left\langle \frac{1}{\gamma} \right\rangle \right)$$

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Entropy conservation:

$$\frac{s_D(T_D)}{s_{\text{SM}}(T)} = \frac{s_D(T_D(T_{\text{cd}}))}{s_{\text{SM}}(T_{\text{cd}})} \quad \Rightarrow \quad T_D = T_D(T)$$

Boltzmann equation for the 'dark neutrino'  $N$  :

$$\frac{d\rho_N}{dt} = \underbrace{-4H\rho_N}_{\text{Dilution}} + \underbrace{\frac{1}{\tau_\phi} \frac{m_\phi}{E} n_\phi}_{\text{Decay}}$$

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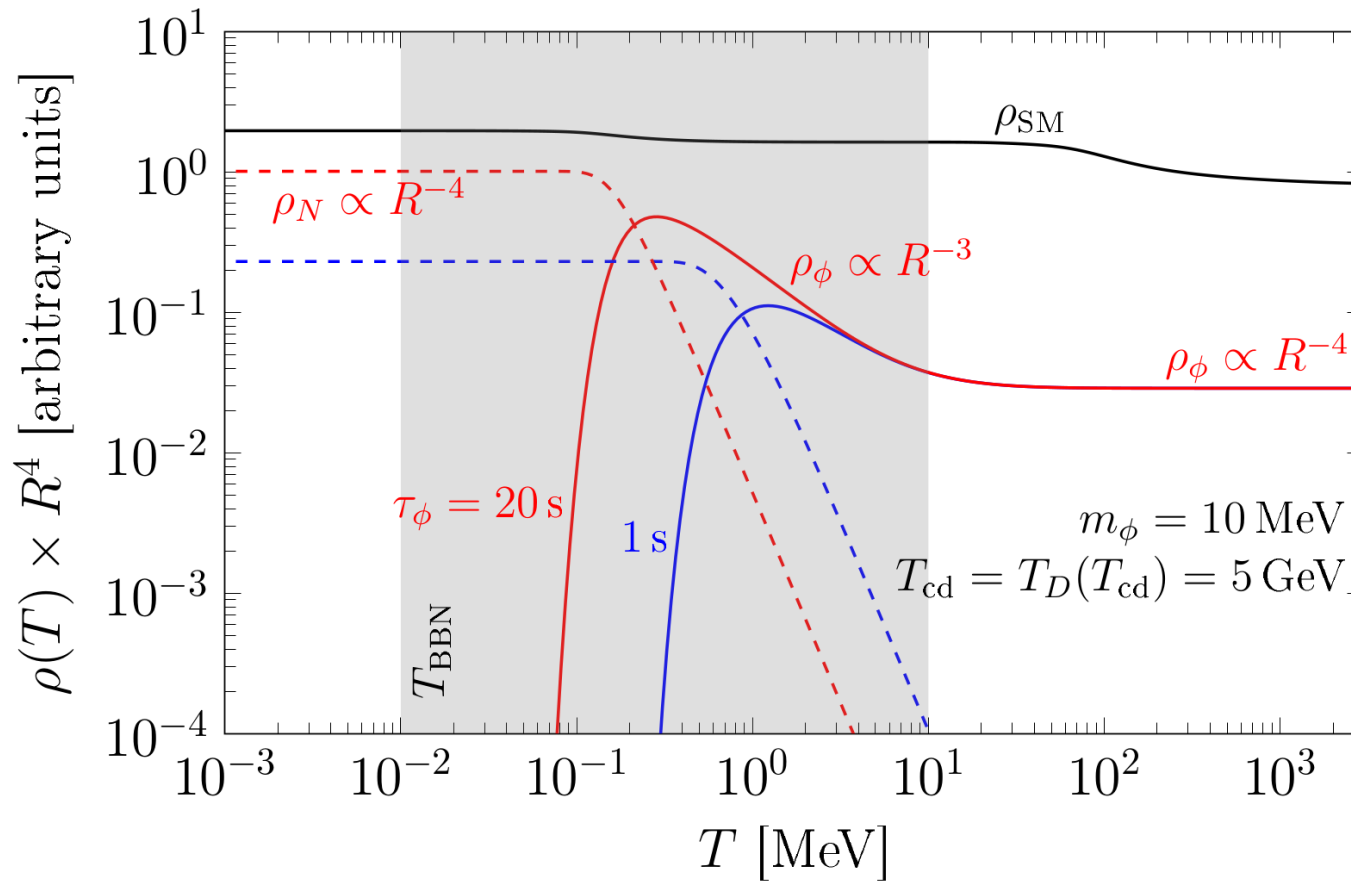
Initial condition:

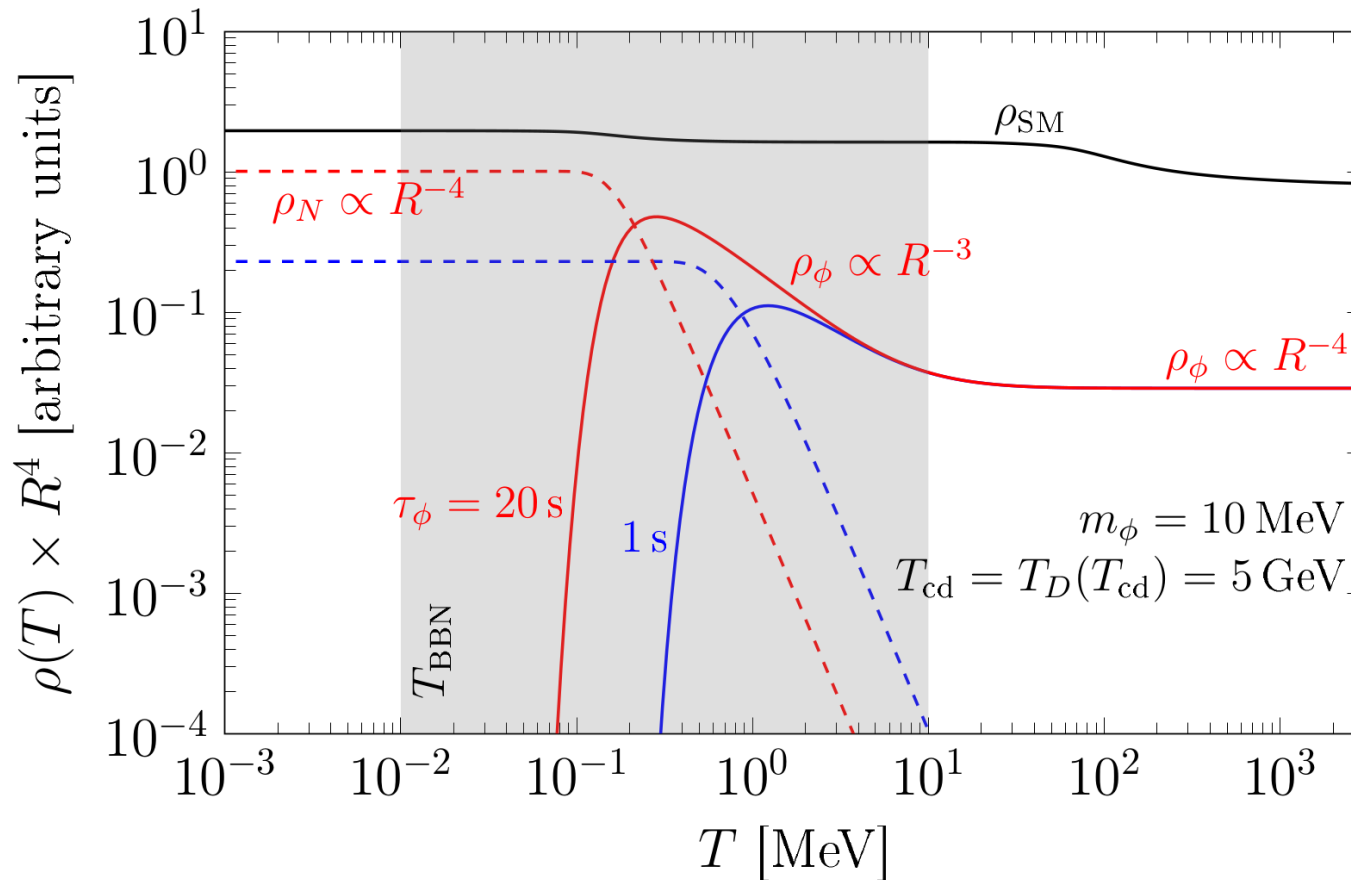
$$\rho_N(t = t_{\text{cd}}) \simeq 0$$

Solution:

$$\rho_N(t) = R(t)^4 \int_{t_{\text{cd}}}^t \frac{1}{R(\lambda)^4} \frac{m_\phi n_\phi(\lambda)}{\tau_\phi} dt$$

# Thermal evolution of the dark sector



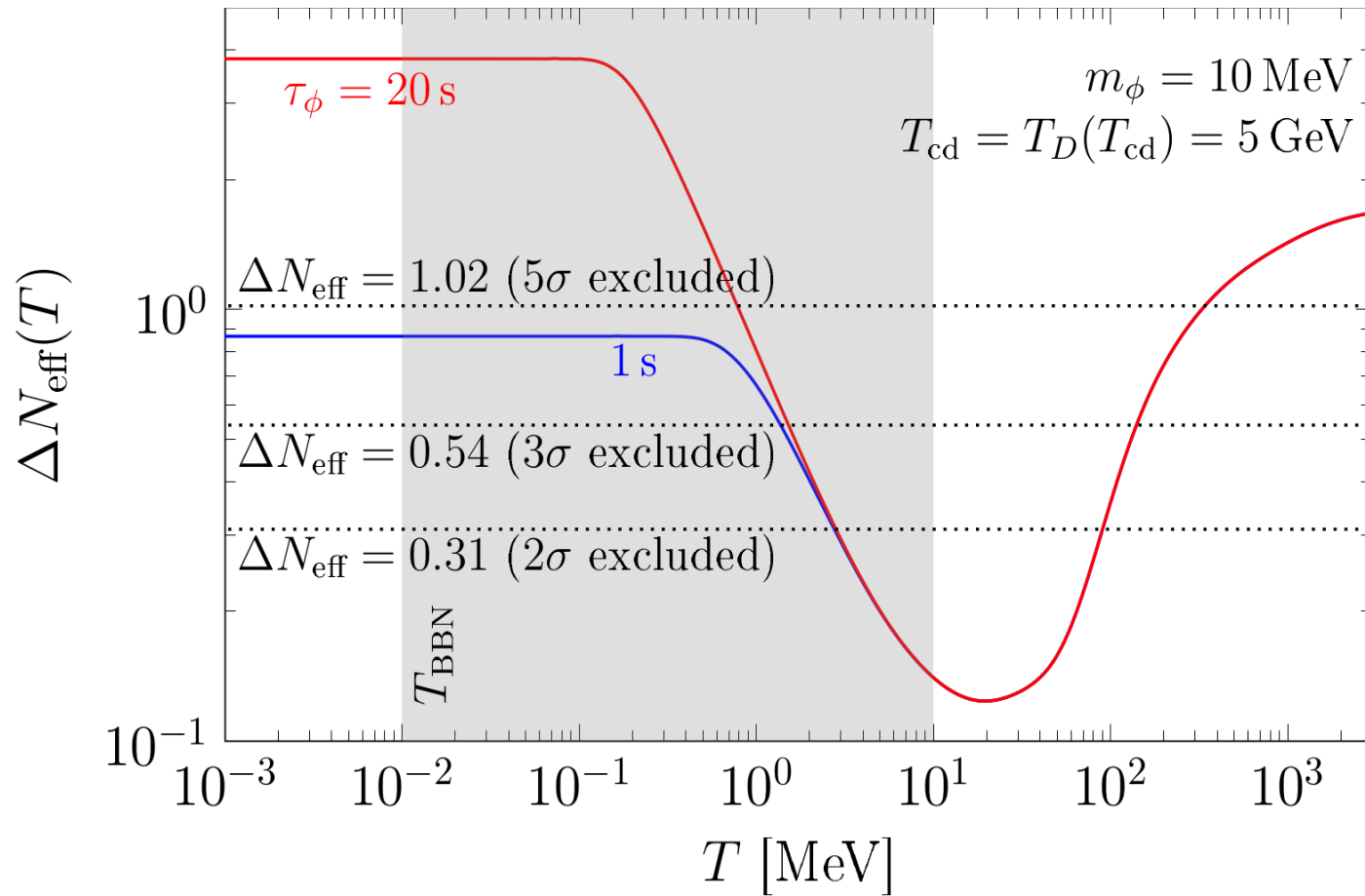


**Question:** Can the thermal evolution be quantified by

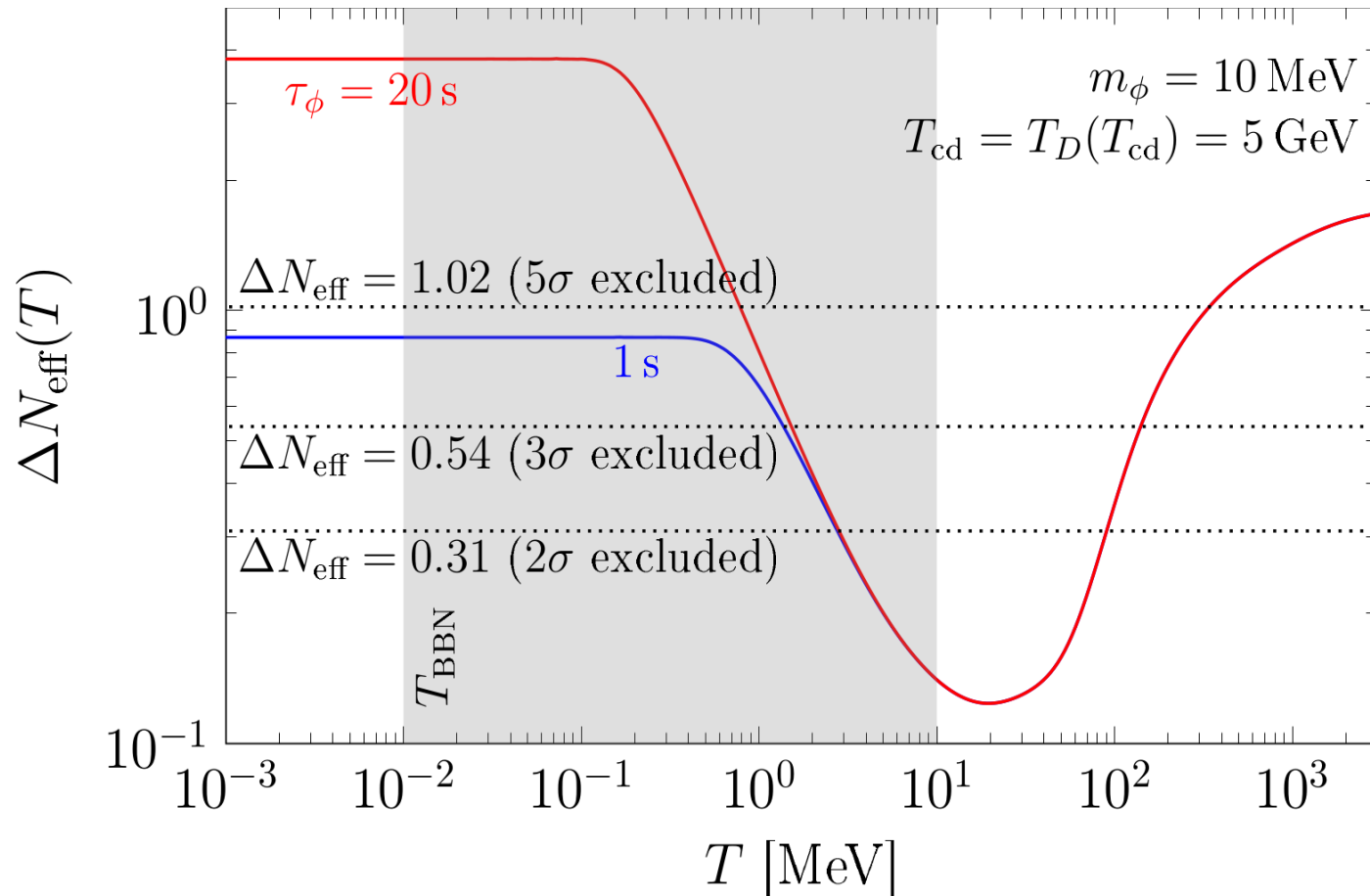
$$\Delta N_{\text{eff}}(T) = \frac{\rho_D(T)}{\rho_\nu(T)}$$



# Thermal evolution of the dark sector







The limit cannot be expressed in terms of  $\Delta N_{\text{eff}}$

→ A dedicated analysis is needed

# Calculation of the bounds

→ Energy densities

$$\rho_D = \rho_\phi + \rho_N$$

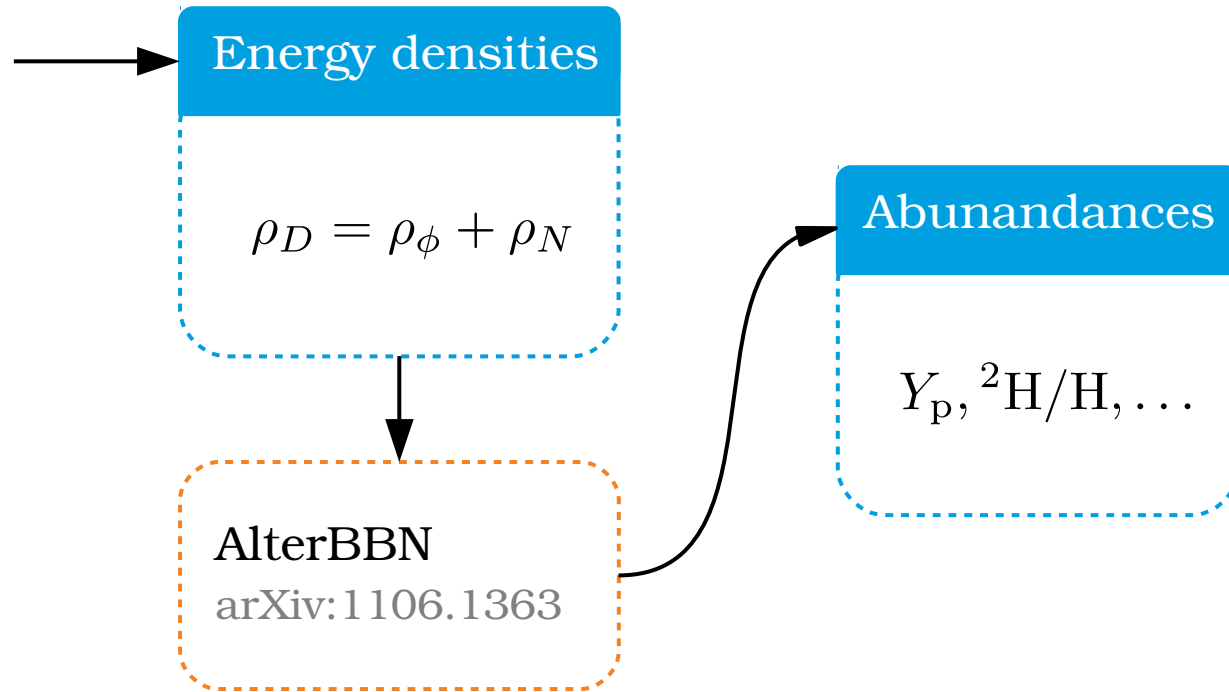
# Calculation of the bounds

Energy densities

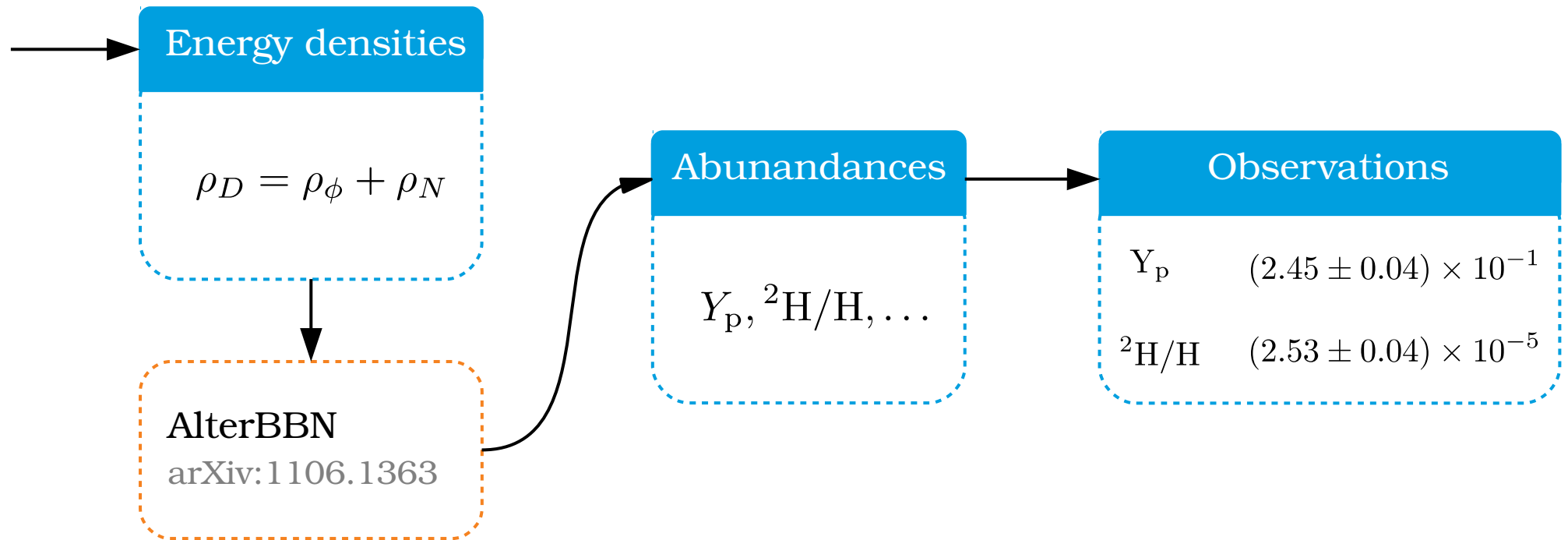
$$\rho_D = \rho_\phi + \rho_N$$

AlterBBN  
arXiv:1106.1363

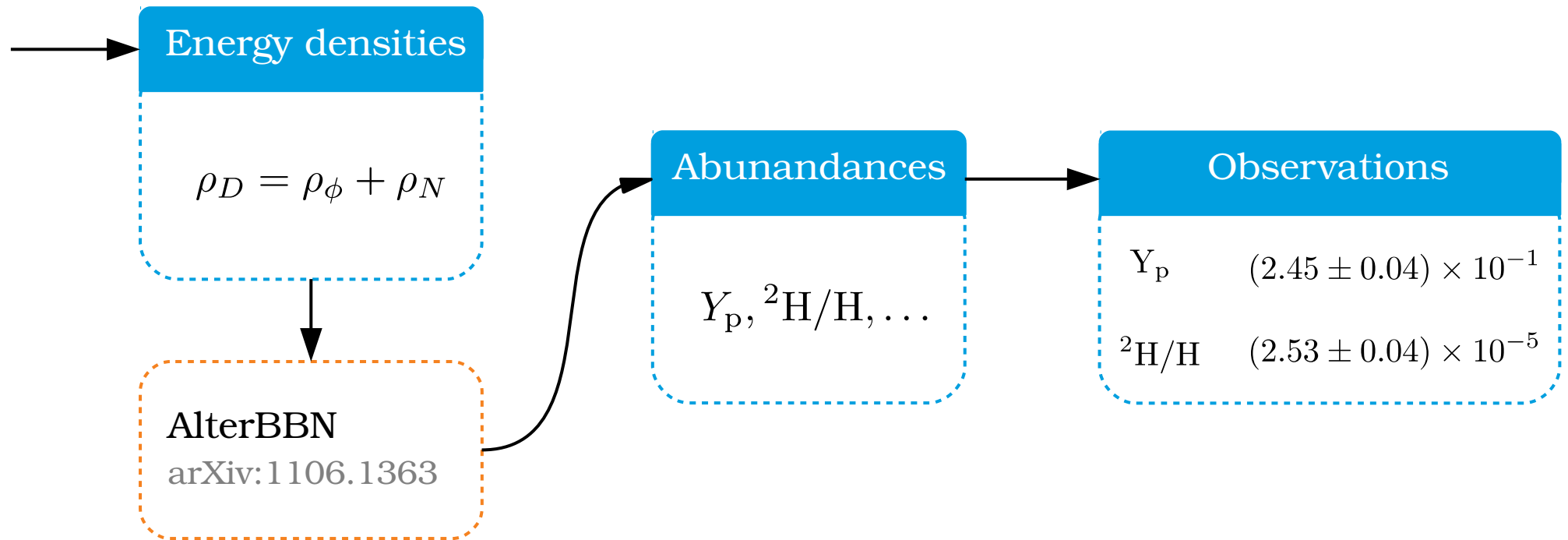
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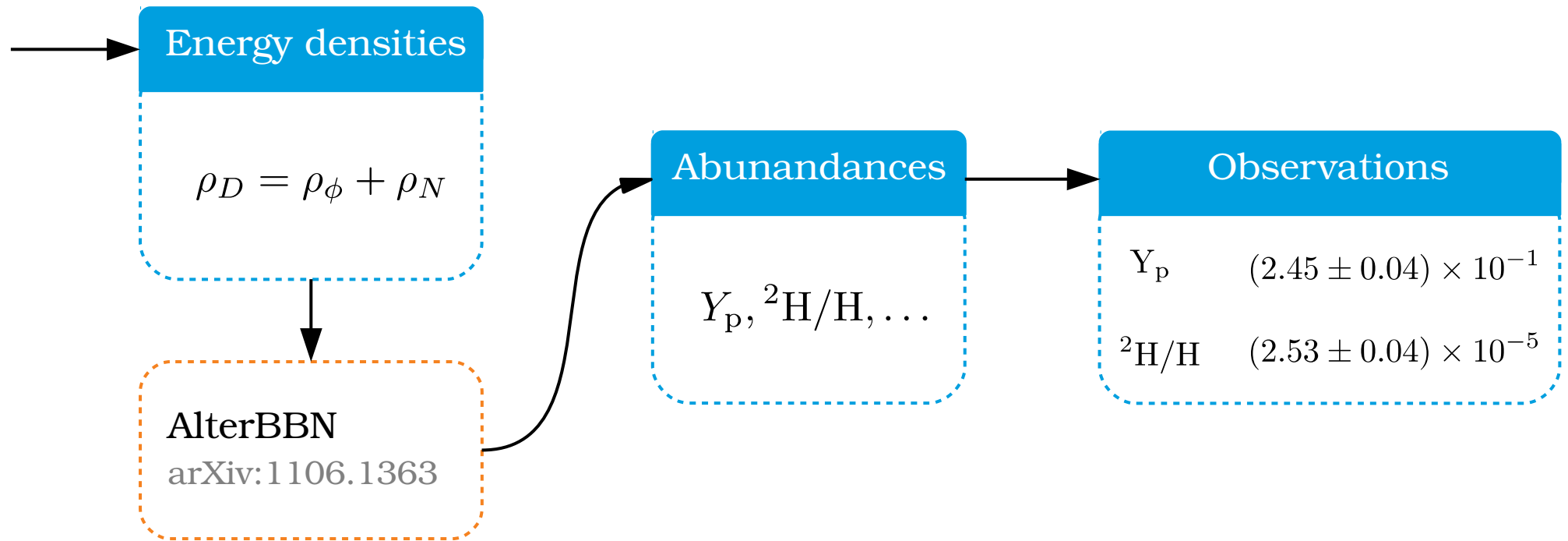


Parameters of the calculation:

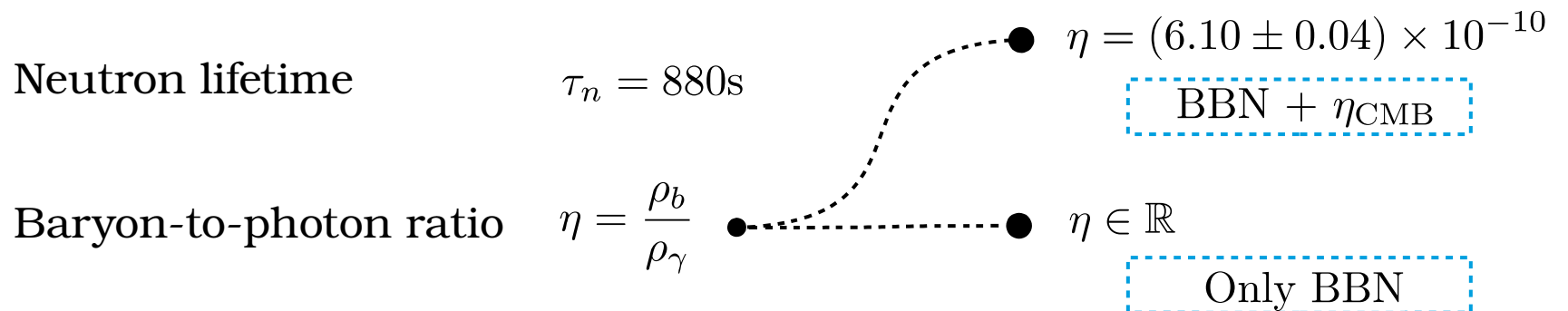
Neutron lifetime  $\tau_n = 880\text{s}$

Baryon-to-photon ratio  $\eta = \frac{\rho_b}{\rho_\gamma}$

# Calculation of the bounds



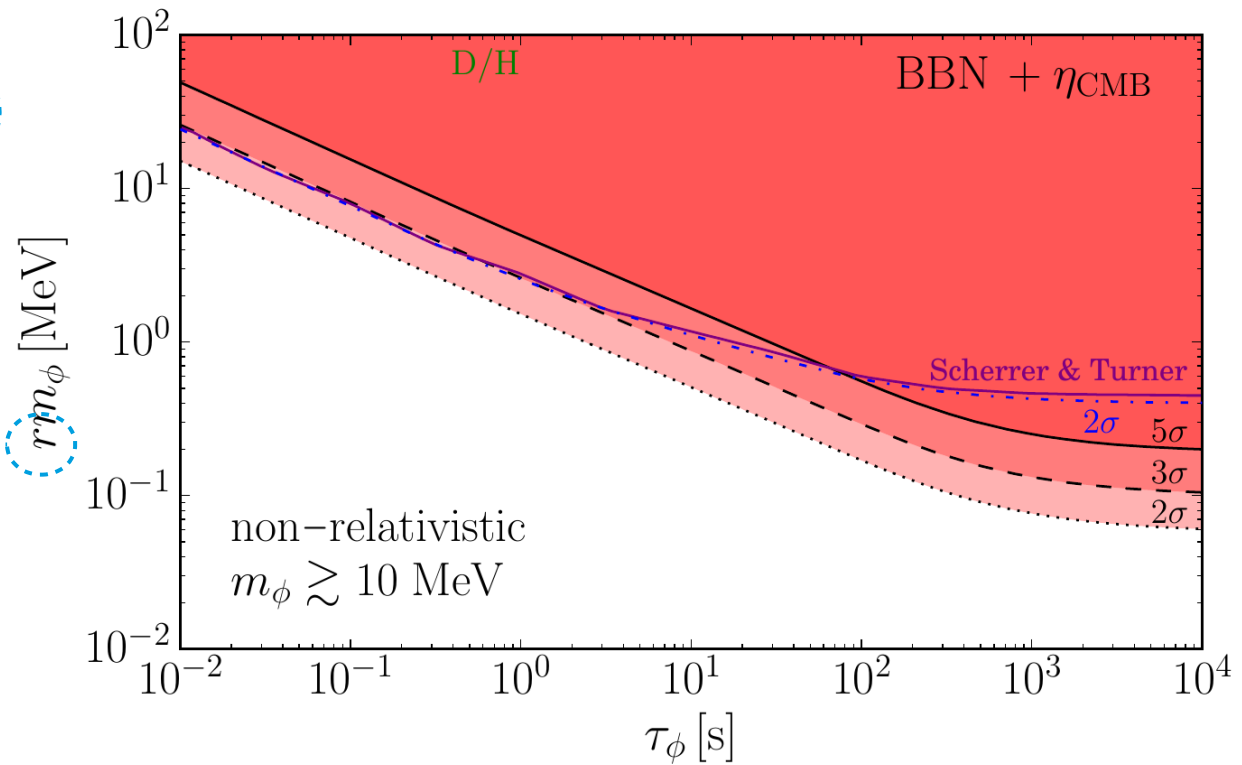
Parameters of the calculation:



# Resulting bounds from BBN

First check non-relativistic limit (Scherrer/Turner, 10.1086/166534):

$$r = \frac{n_\phi}{n_\gamma} \Big|_{T=10^9\text{K}}$$

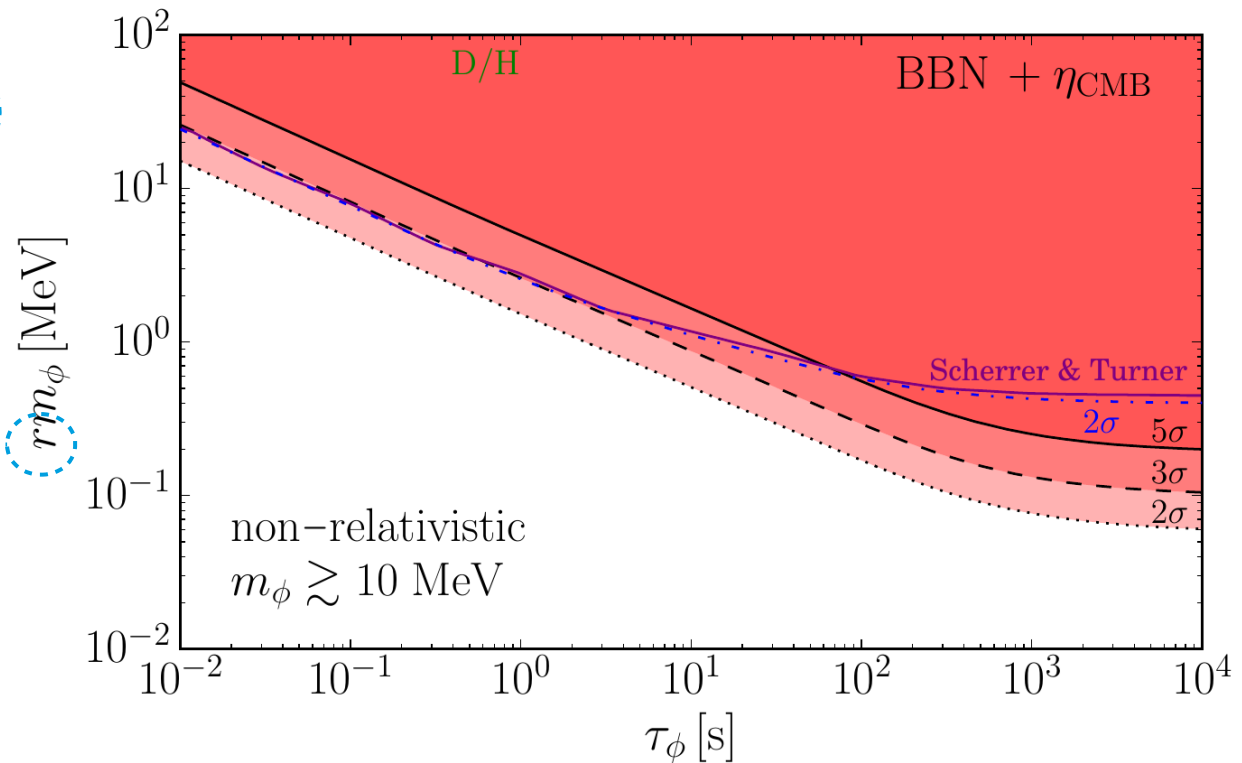




# Resulting bounds from BBN

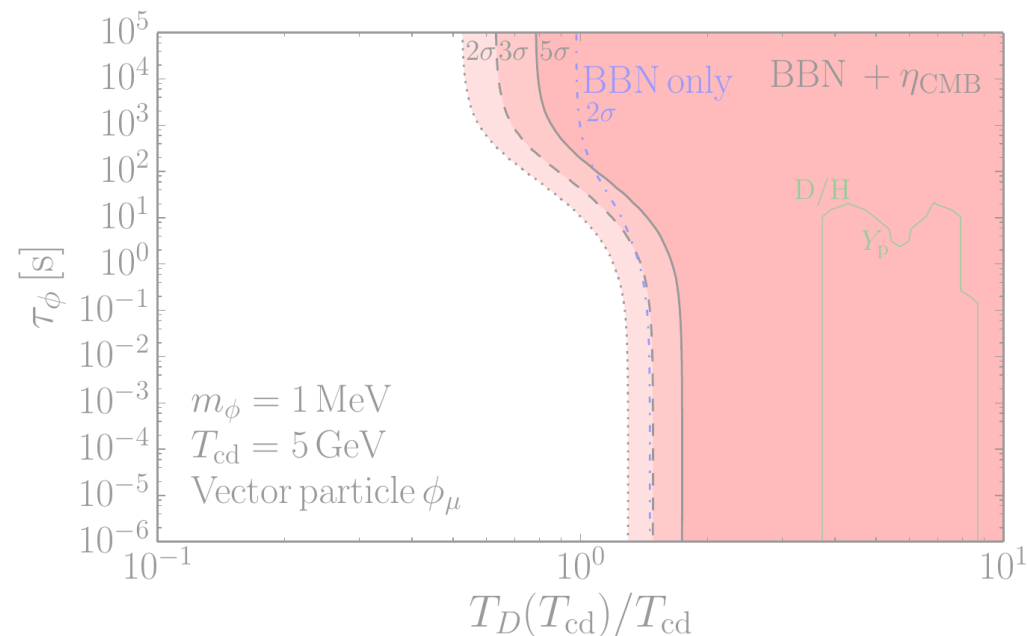
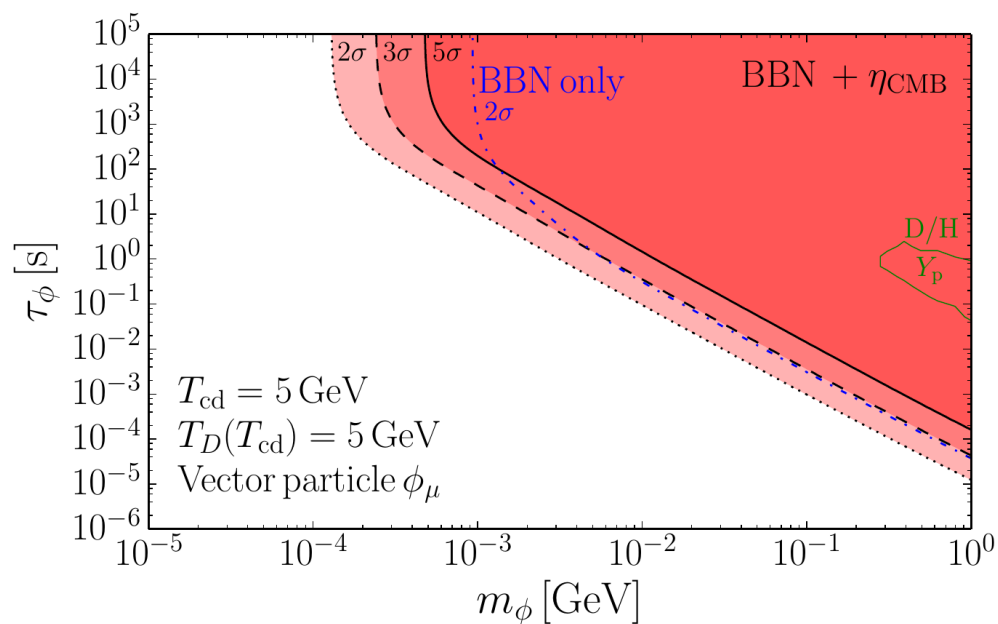
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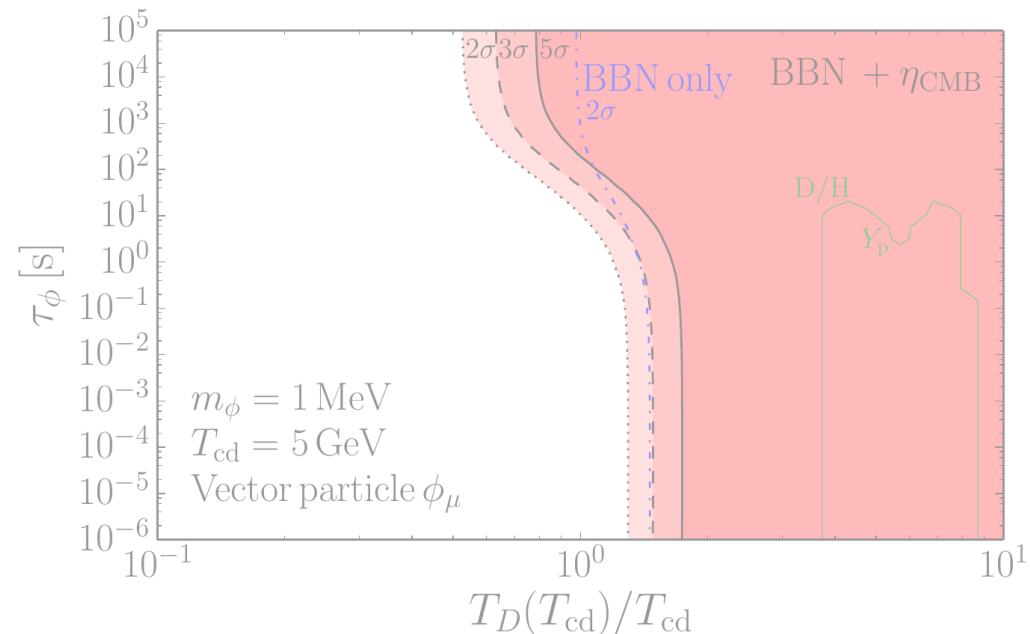
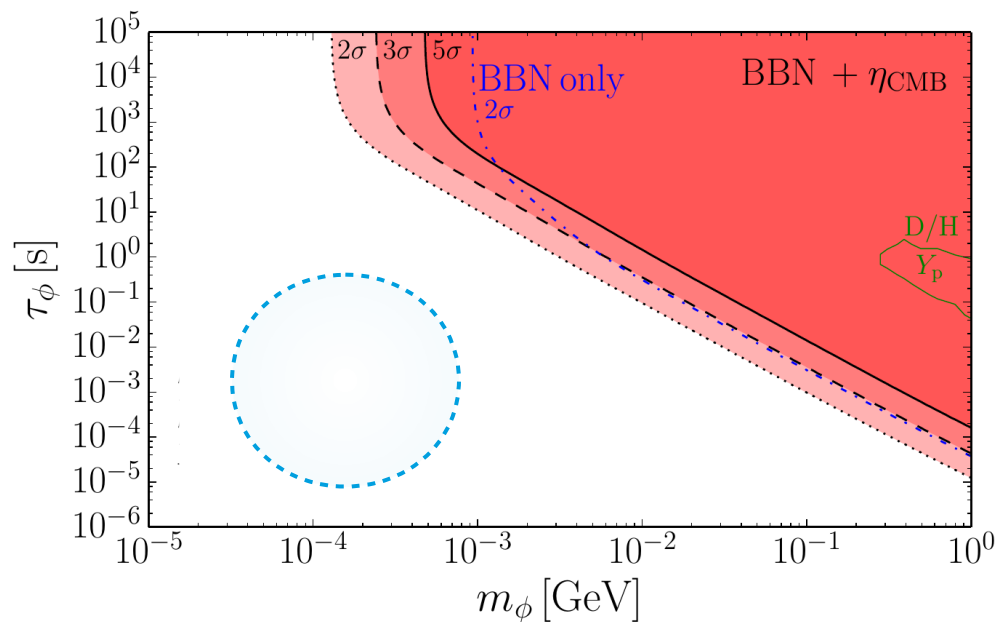
➔ Good agreement with the literature for  $m_\phi \gtrsim 10 \text{ MeV}$

# Resulting bounds from BBN (Vector mediator)



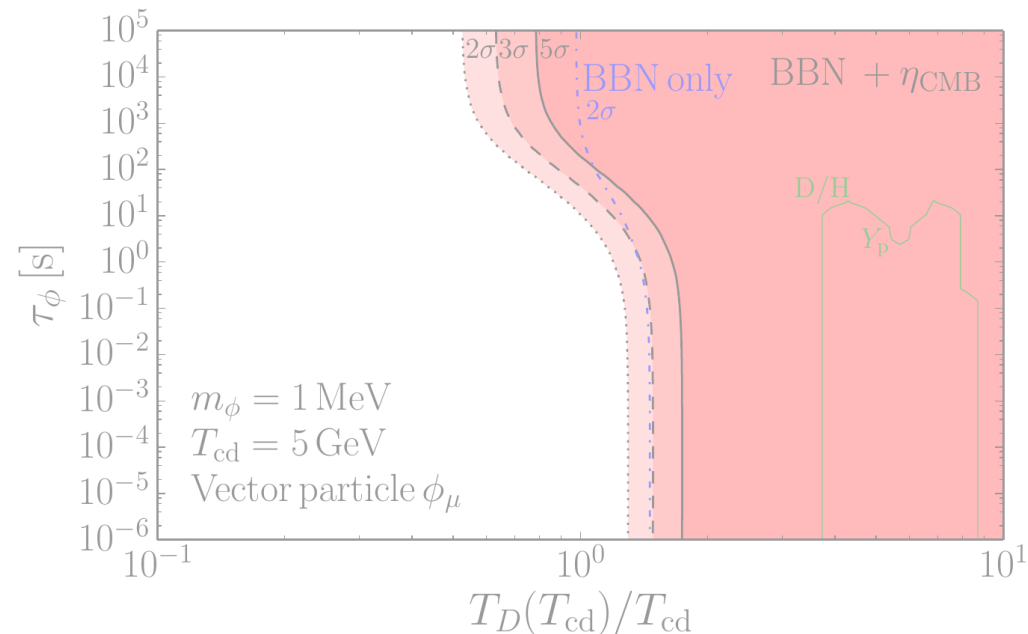
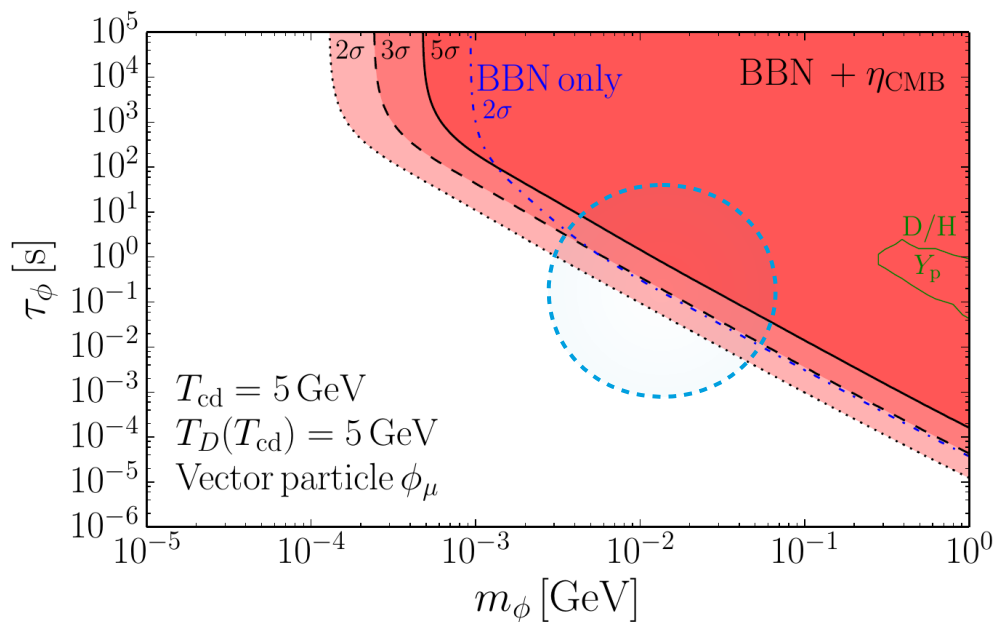
- For small  $m_\phi, \tau_\phi$ ,  $\phi$  is relativistic during decay:  $\Delta N_{\text{eff}} \sim 0.1 < 0.2$
- Diagonal exclusion line determined by  $T(t = \tau_\phi) \sim m_\phi$ 
  - Above,  $\phi$  is non-relativistic during decay:  $\rho_\phi \propto R^{-3} > R^{-4}$
- For large  $\tau_\phi$ ,  $\phi$  is stable during BBN
  - Bounds become independent of  $\tau_\phi$

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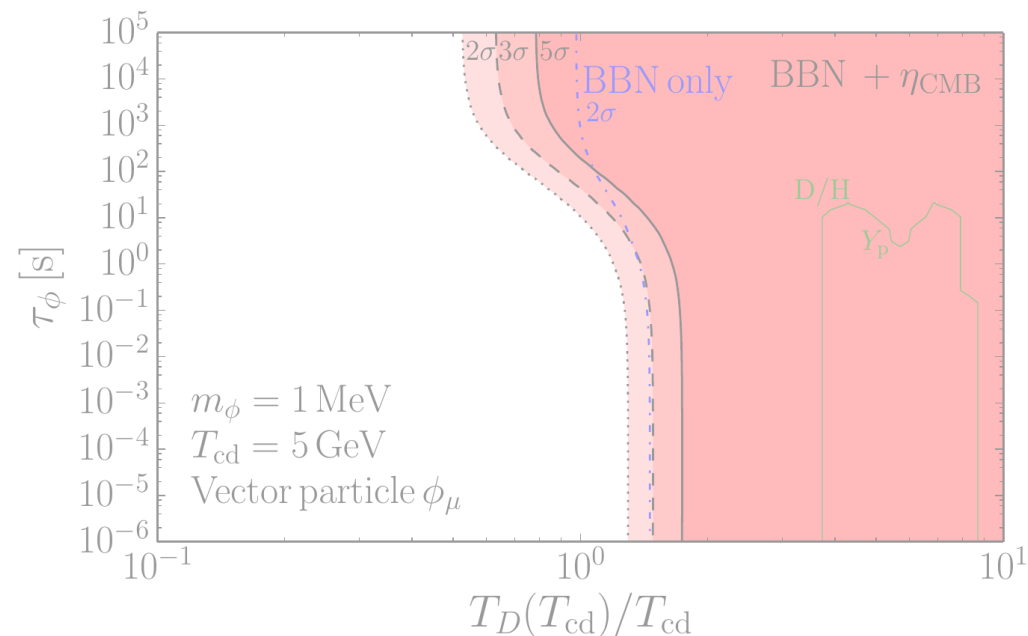
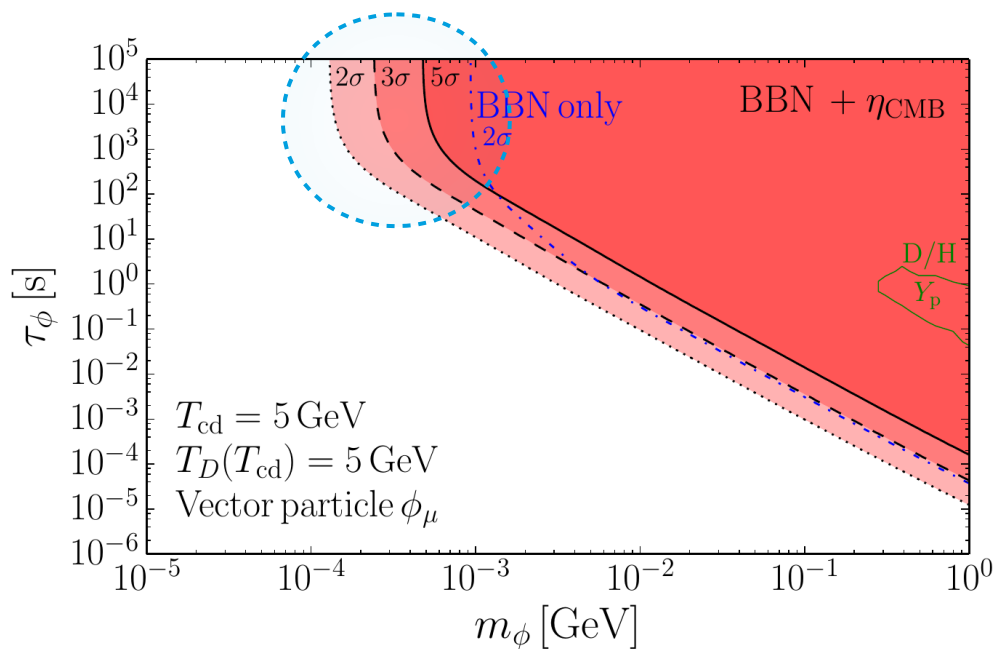
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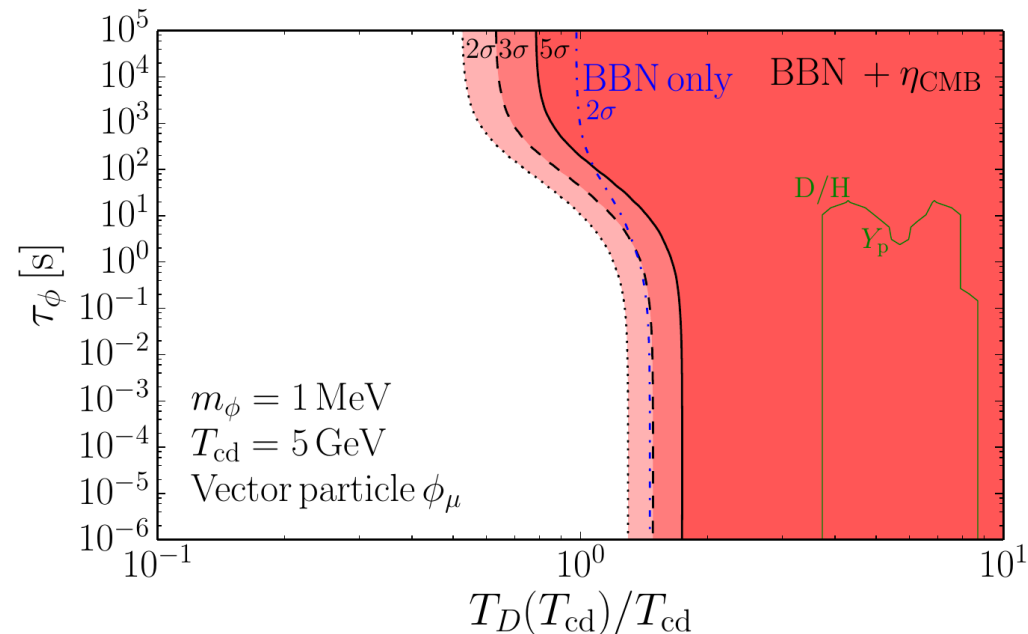
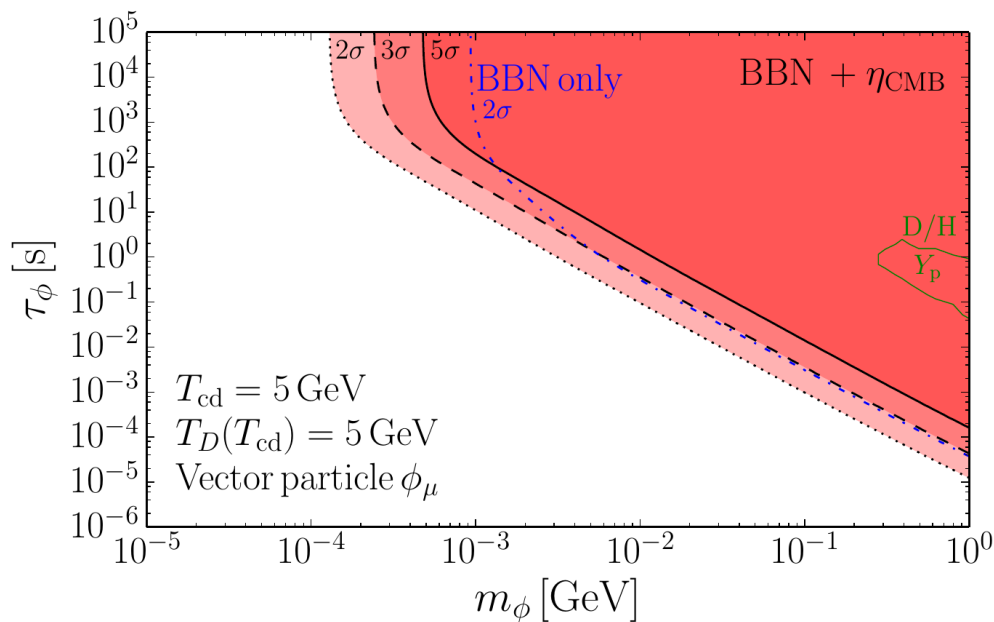
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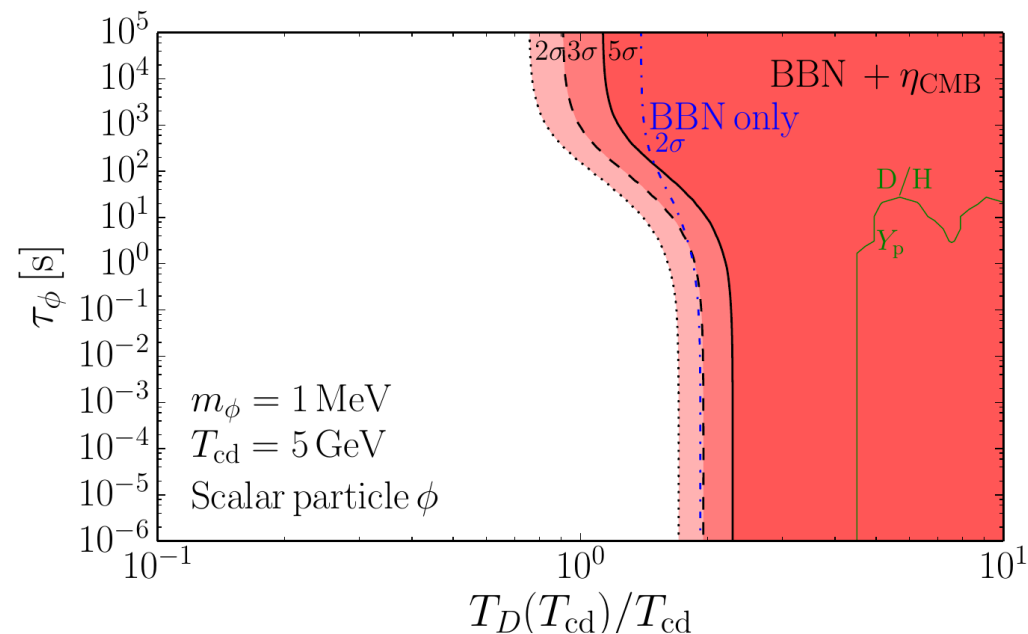
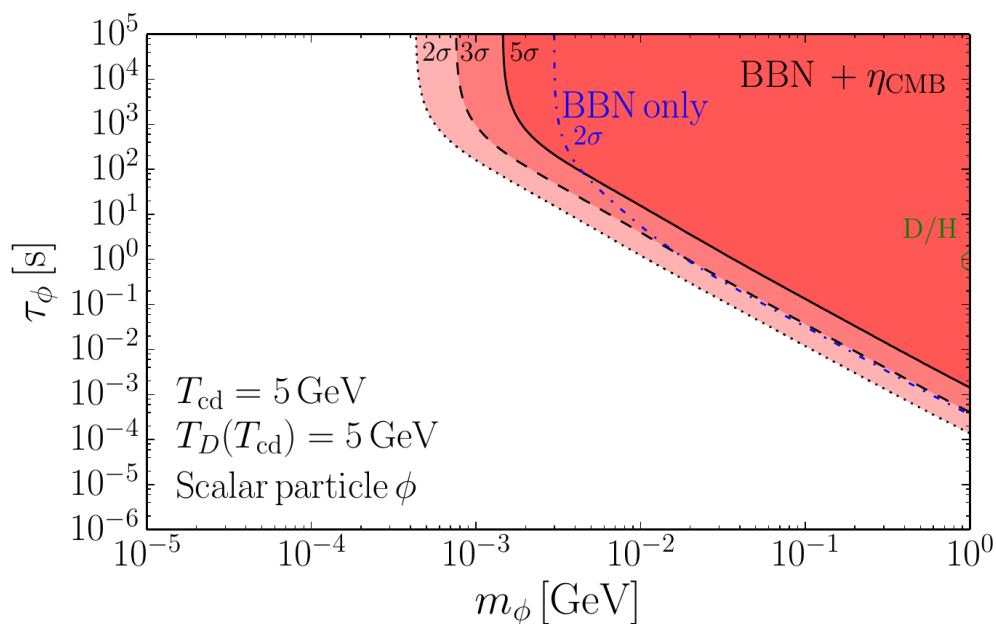
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# Resulting bounds from BBN (Scalar mediator)

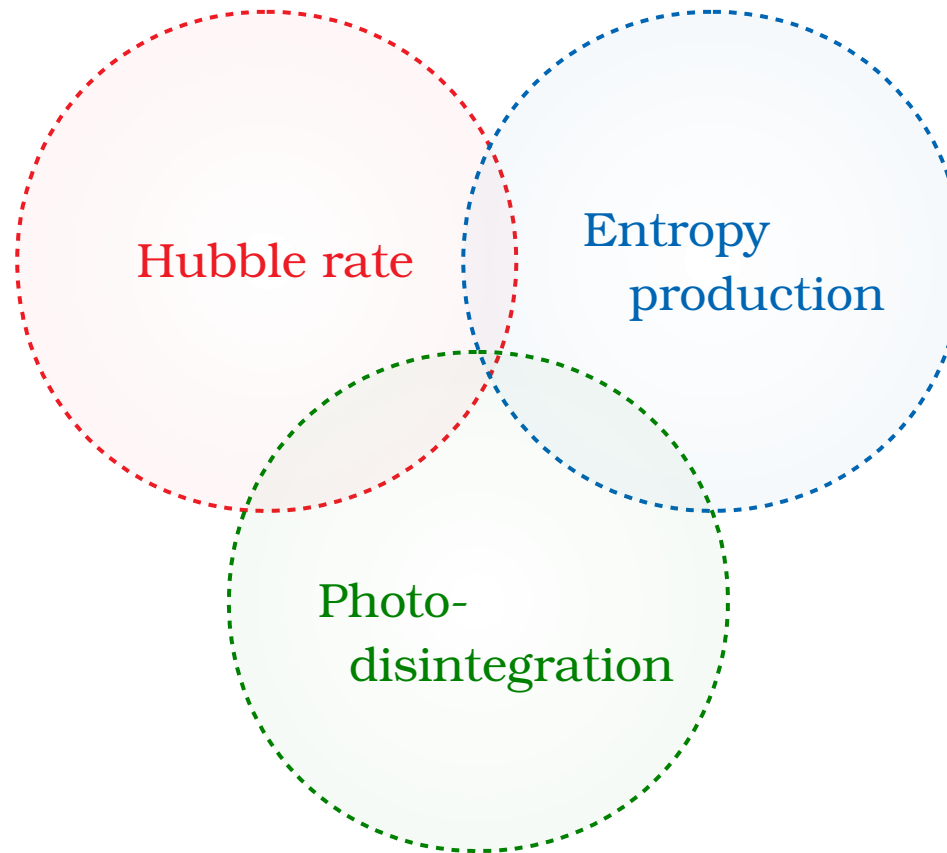


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  - Bounds become independent of  $\tau_\phi$

- Dark sectors with mediators decaying into electrons and/or photons



- Need to consider three different effects:





# Summary

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- Possibility to constraint dark sectors without Standard Model interactions
- New (almost) model-independent study of BBN bounds for particles in the MeV range decaying into light states

## Appetizer:

- Results can be applied to particular models, especially those with dark matter self-interactions

→ Strong bounds

Thank you for  
your attention!

# Backup Slides

# Models with self-interacting dark matter

Model Lagrangian:

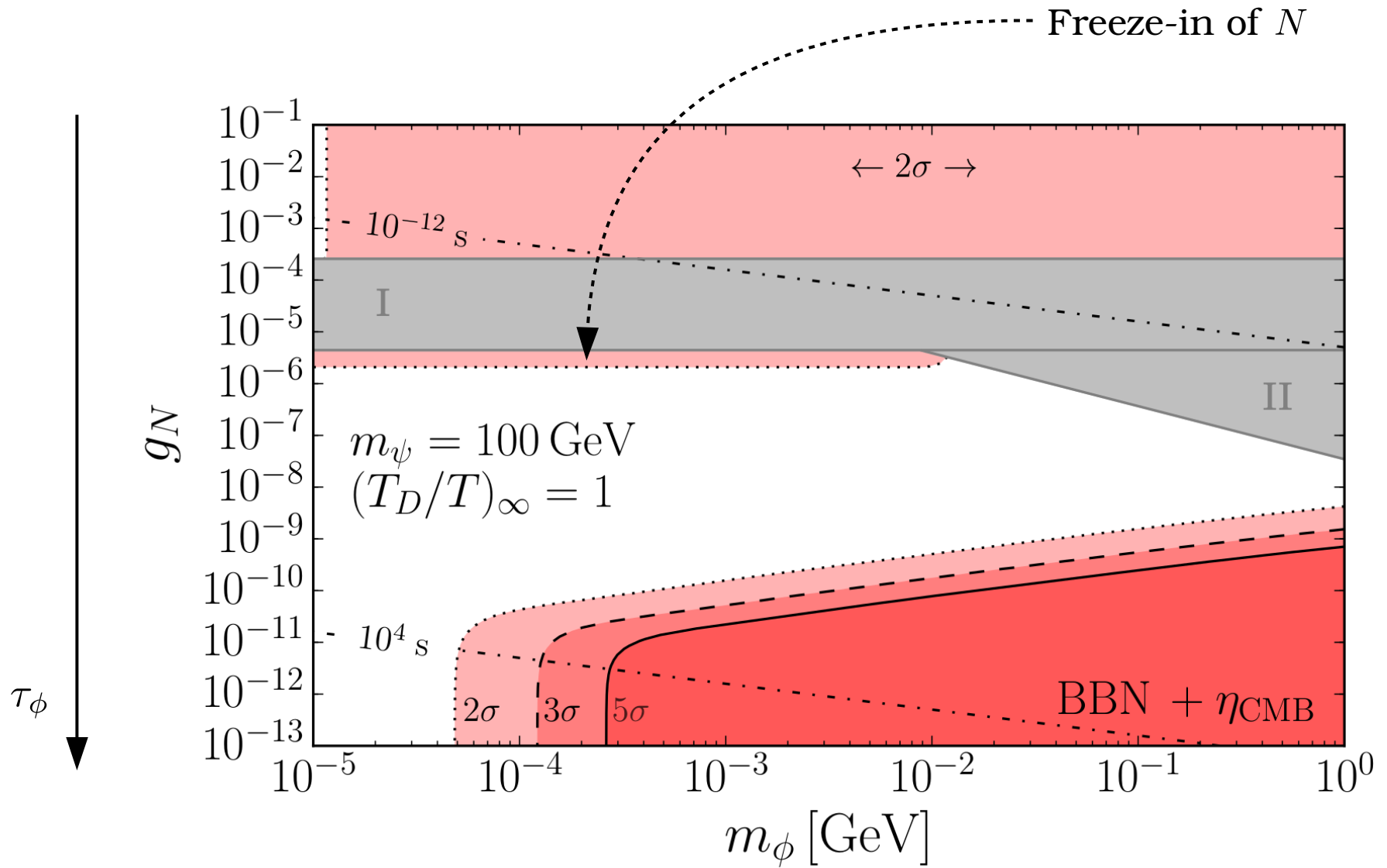
$$\mathcal{L} = g_\psi \bar{\psi} \psi \phi + g_N \bar{N} N \phi$$

Discriminate between two regimes:

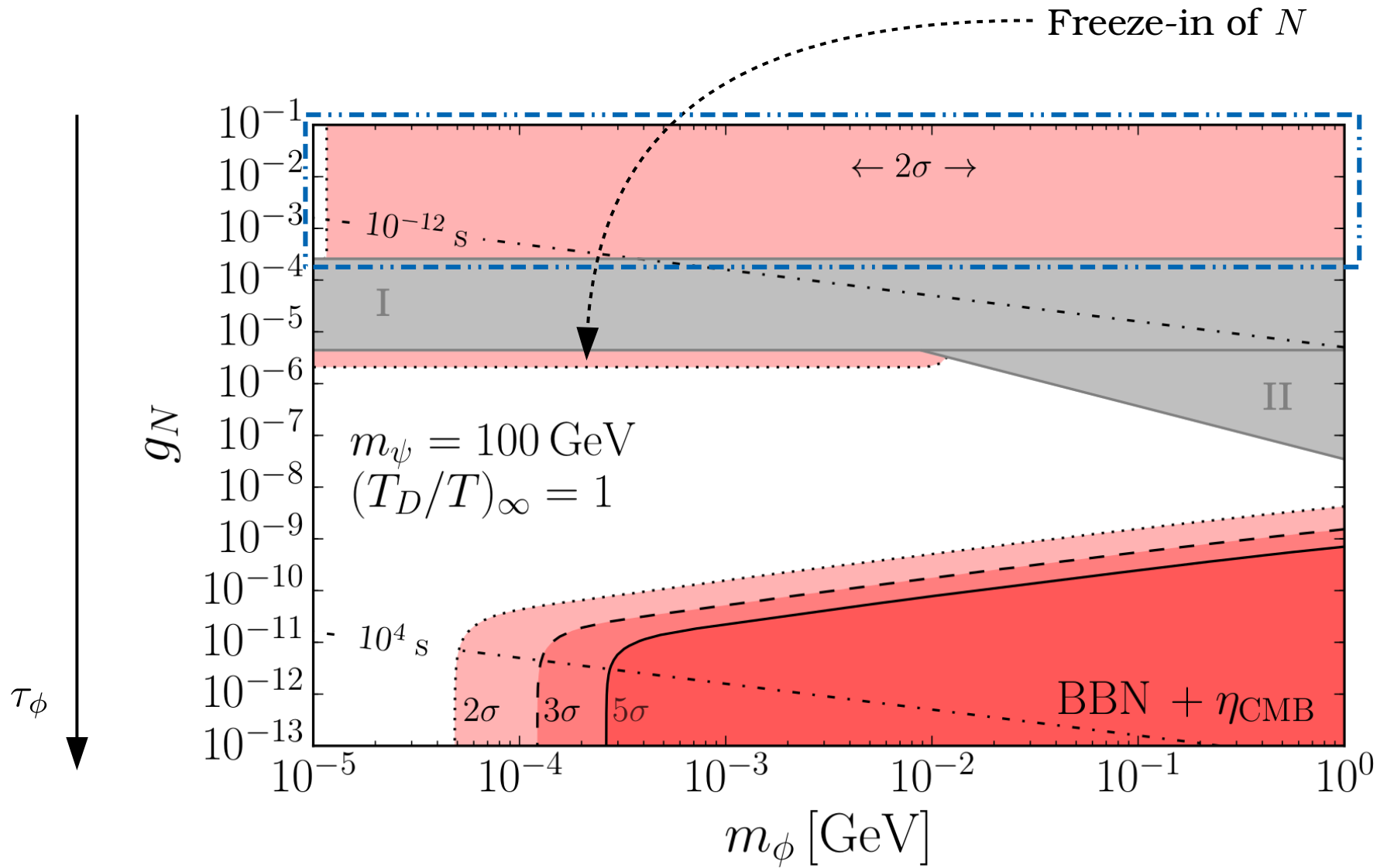
1. *Large coupling regime*
2. *Small coupling regime*

However: Two *intermediate regions* remain

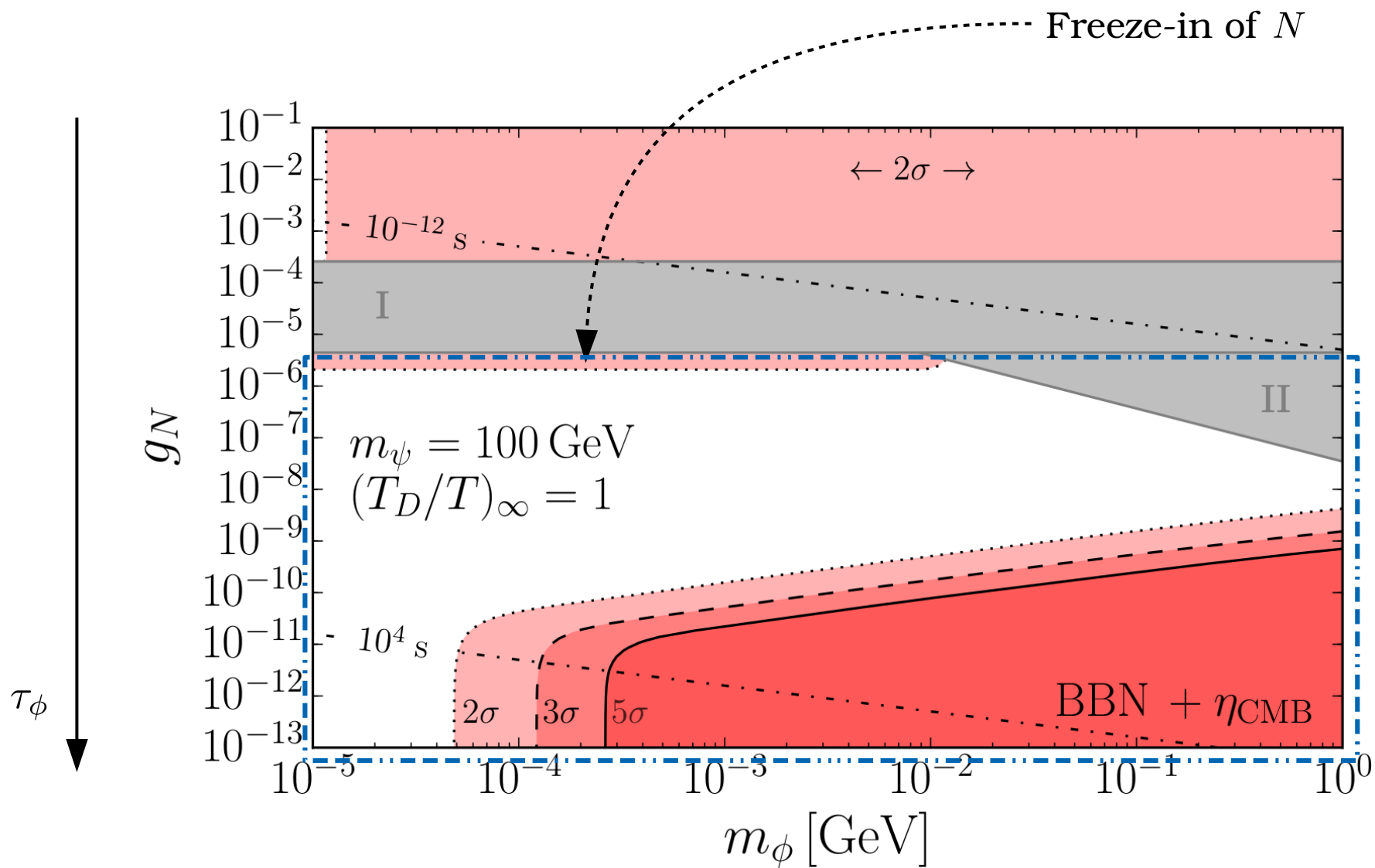
# Model-dependent constraints



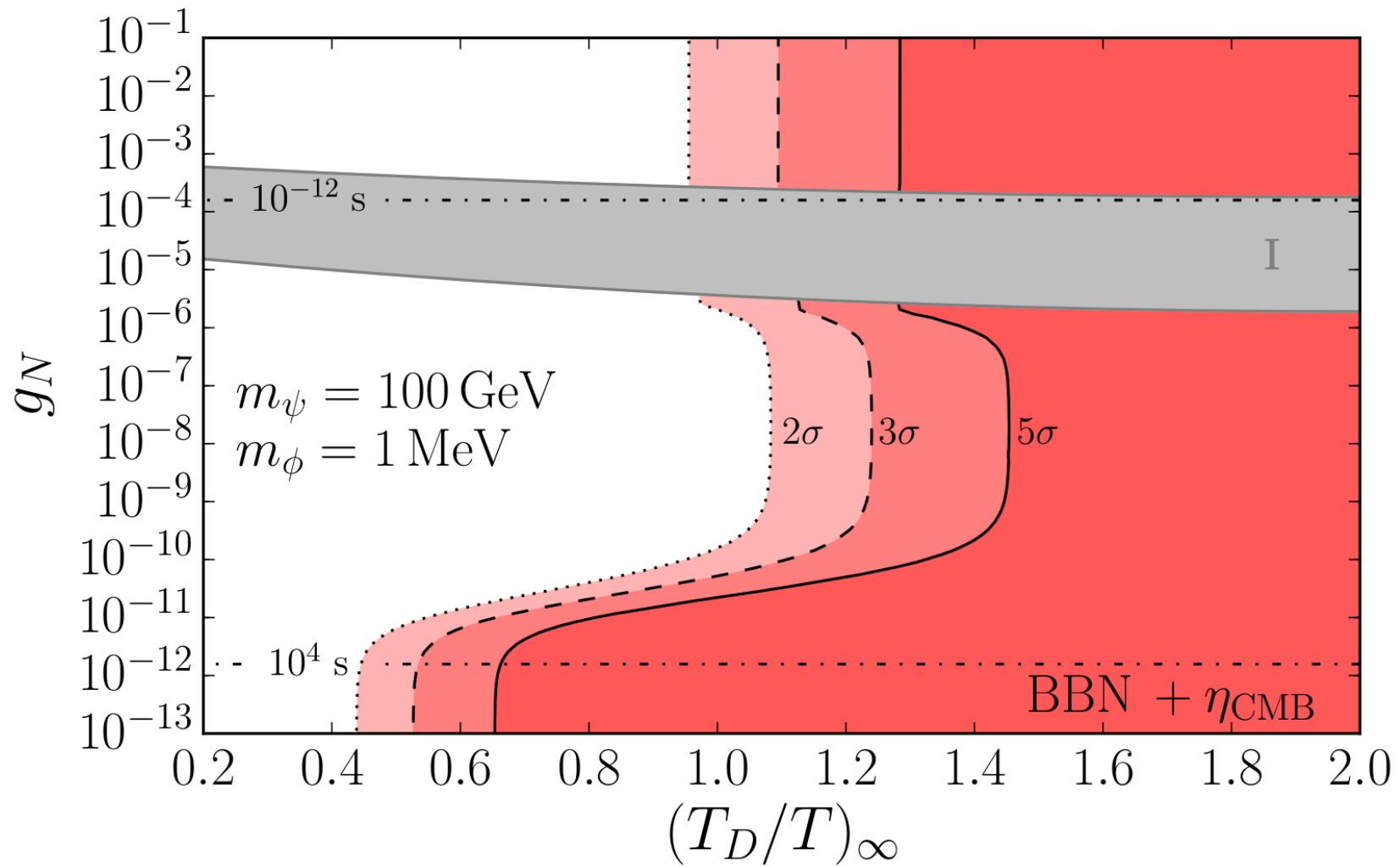
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# BBN and dark matter models with self-interactions

