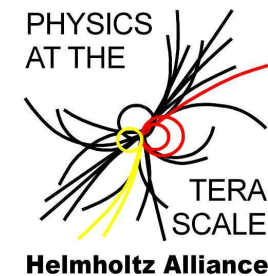


Electroweak and Bottom Quark Contributions to Higgs + Jet Production

Oliver Brein

Physikalisches Institut,
Universität Freiburg

e-mail: Oliver.Brein@physik.uni-freiburg.de



[see [arXiv:1003.XXXX](https://arxiv.org/abs/1003.XXXX) [hep-ph]]

outline :

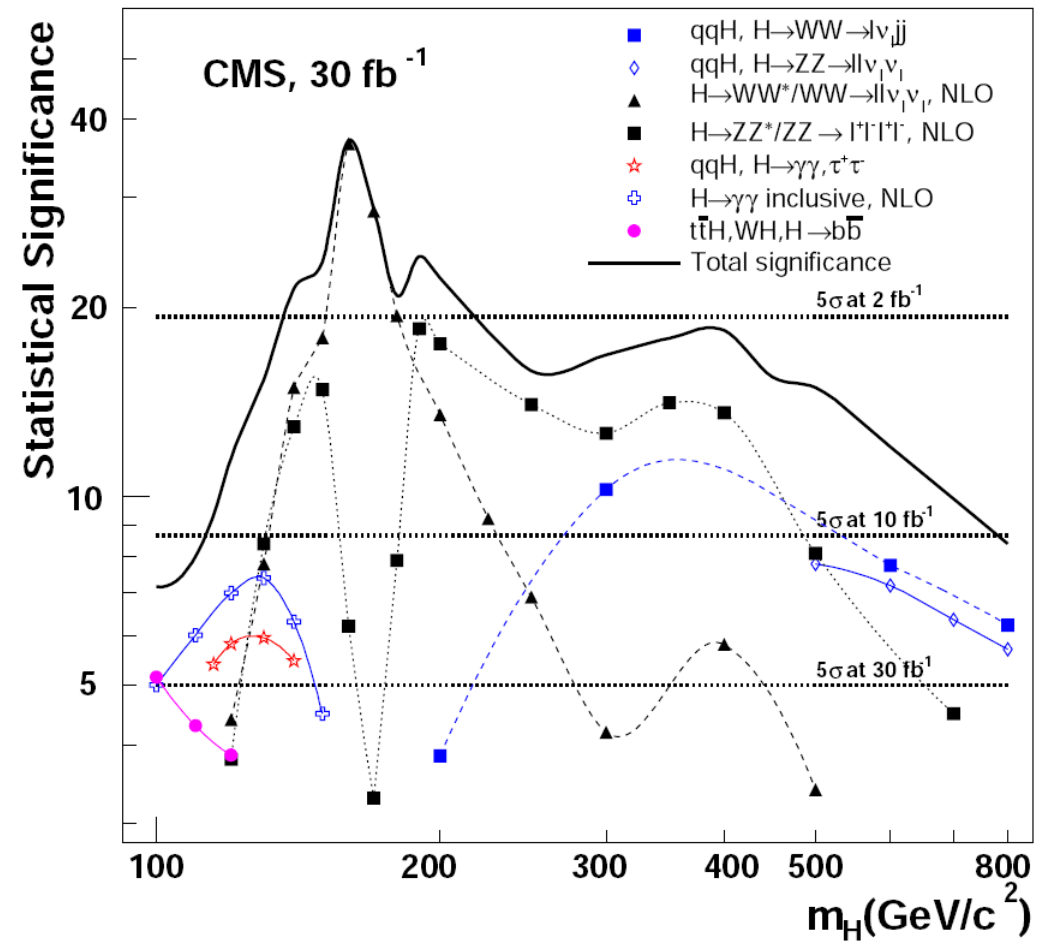
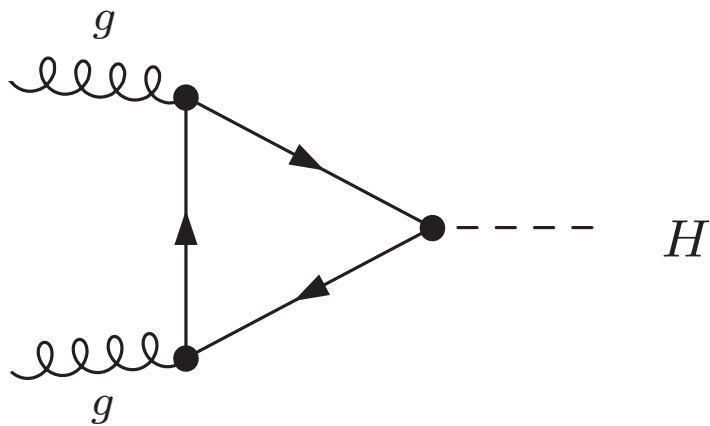
- Higgs + Jet in the Standard Model
- LO Contributions to Higgs + Jet
- Numerical Results

- Higgs + Jet in the Standard Model

• Higgs + Jet in the Standard Model

– Higgs production @ the LHC

SM Higgs production @ LHC mainly via gluon fusion:



Detection ($m_H \approx 100 - 140 \text{ GeV}$): mainly via the rare decay $H \rightarrow \gamma\gamma$.

– Higgs + Jet

suggestion: study Higgs events with a high- p_T hadronic jet

LO QCD $\mathcal{O}(\alpha_S^3\alpha)$: [van der Bij et al. '87; Baur, Glover '89]

NLO QCD $\mathcal{O}(\alpha_S^4\alpha)$: [de Florian, Grazzini, Kunszt '99]

+ NLL soft gluon threshold resummation: [de Florian, Kulesza, Vogelsang '05]

advantages:

* richer kinematical structure compared to inclusive Higgs production.

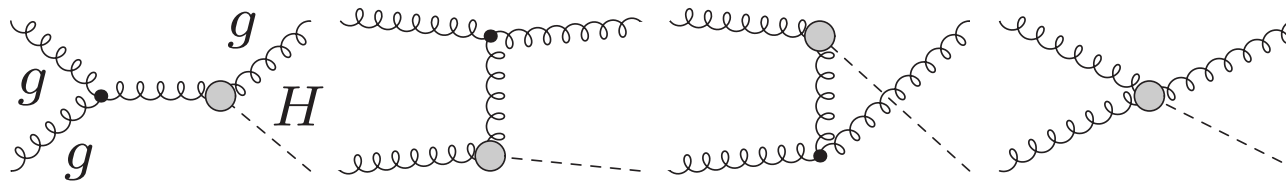
→ allows for refined cuts

→ better signal significance (S/\sqrt{B})

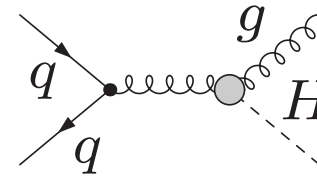
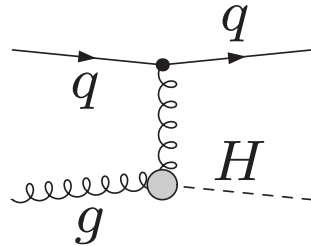
* background predictions e.g. for $H \rightarrow \gamma\gamma$ under better theoretical control

disadvantage:

* lower rate than inclusive Higgs production

SM H+jet, partonic processes ($\mathcal{O}(\alpha_s^3\alpha)$, mainly via top loops):

$$gg \rightarrow Hg \quad (\approx 60 - 75 \% \text{ of total rate})$$



$$qg \rightarrow Hq \quad (\approx 25 - 40 \%) \quad q\bar{q} \rightarrow Hg \quad (\text{rate small})$$

simulations: $pp \rightarrow H + \text{jet}, H \rightarrow \gamma\gamma$ [Abdullin et al. '98 & '02; Zmushko '02]

$pp \rightarrow H + \text{jet}, H \rightarrow \tau^+\tau^- \rightarrow l^+l^- \cancel{p}_T$ [Mellado et al. '05]

show: $H + \text{jet}$ production (e.g. with $p_{T,\text{jet}} \geq 30 \text{ GeV}$, $|\eta_{\text{jet}}| \leq 4.5$)
is a promising alternative (supplement)
to the inclusive SM Higgs production
for $m_H \approx 100 - 140 \text{ GeV}$.

available codes: SM:

- **Higgsjet** [de Florian, Grazzini, Kunszt '99]
NLO QCD cross section for $pp \rightarrow H + \text{jet}$ (large m_t approx.)
also: soft gluon resummation [de Florian, Kulesza, Vogelsang '05]
- **HqT** [Bozzi, Catani, de Florian, Grazzini '03 & '06]
 p_T -distribution for $pp \rightarrow H + X$ (large m_t approx.)
including resummation at $NLL + LO$ and $NNLL + NLO$ QCD accuracy
- **MC@NLO** [Frixione, Webber '02; Frixione, Nason, Webber '05]
contains $pp \rightarrow H + X$ event generation at NLO QCD accuracy
(large m_t approx.)
- **FEHiP** [Anastasiou, Melnikov, Petriello '05]
NNLO QCD differential cross section for $pp \rightarrow H + X$ (large m_t approx.)
- **HPro** [Anastasiou, Bucherer, Kunszt '09]
corrects large m_t approx. NNLO QCD differential predictions
by finite m_t & m_b terms from NLO QCD

NNLO QCD accuracy (large m_t approx.) $\propto 10\%$ (scale variation)

→ further improvements need to consider other 10%-ish effects

available codes: MSSM:

- **HJET 1.3** [OBr, Hollik '03; '07]
 LO QCD full MSSM (no approximations)
 & LO QCD SM (no approximations):

$$\sigma_{\text{hadronic}}^{\text{total}}, \frac{d\sigma_{\text{hadronic}}}{d\sqrt{\hat{s}}}, \frac{d\sigma_{\text{hadronic}}}{dp_{T,\text{jet}}}, \frac{d\sigma_{\text{hadronic}}}{d\eta_{\text{jet}}}, \frac{d^2\sigma_{\text{hadronic}}}{dp_{T,\text{jet}} d\eta_{\text{jet}}}, \dots$$

– Higgs + Jet: How to improve the prediction ?

- go beyond the large m_t approximation
in the NLO QCD prediction for the Higgs p_T distribution
- NNLO QCD corrections (in the large m_t approximation)
- consider other LO effects
 - * non-QCD: electroweak LO contributions
 - * QCD 5-flavour scheme: b quark parton process contributions

- LO Contributions to Higgs + Jet

• LO Contributions to Higgs + Jet

– Previous Study [Keung, Petriello '09]

SM Higgs p_T distribution with

1. finite quark mass effects (m_t, m_b) in one-loop QCD amplitude:

→ already included in [..., OBr, Hollik '03; '07]

comparison of approximations:

* large- m_t limit (no b in loops) → effective ggH vertex [SIZE]

* finite m_t (no b in loops) [SIZE]

* finite m_t and m_b [SIZE]

2. electroweak one-loop effects [SIZE]

→ 5-flavour PDFs used but b quark parton processes not considered.

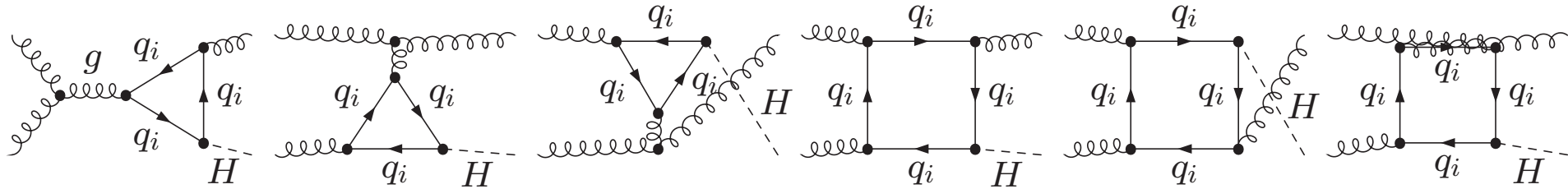
– Our Study [OBr '10]

SM Higgs p_T , η_{jet} (and double differential) distribution with

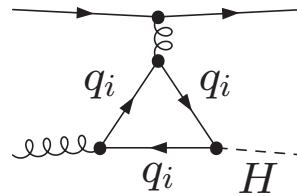
1. finite quark mass effects (m_t, m_b) in one-loop QCD amplitude:
2. electroweak one-loop effects
3. contributions from b -quark parton processes
 - * leading QCD and electroweak effects

– Gluon & Light Quark (u, d, s, c) QCD Contribution : $\mathcal{O}(\alpha_S^3\alpha)$

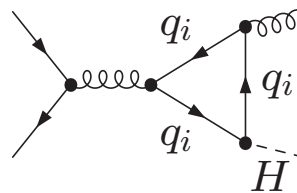
gluon fusion, $gg \rightarrow Hg$



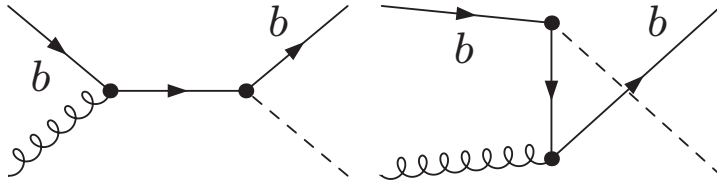
quark gluon scattering, $qg \rightarrow Hq$



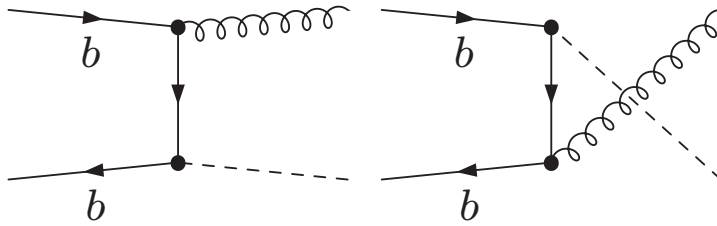
quark anti-quark annihilation, $q\bar{q} \rightarrow Hg$



– Bottom Quark QCD Contribution : $\mathcal{O}(\alpha_s\alpha)$
quark gluon scattering, $bg \rightarrow Hb$



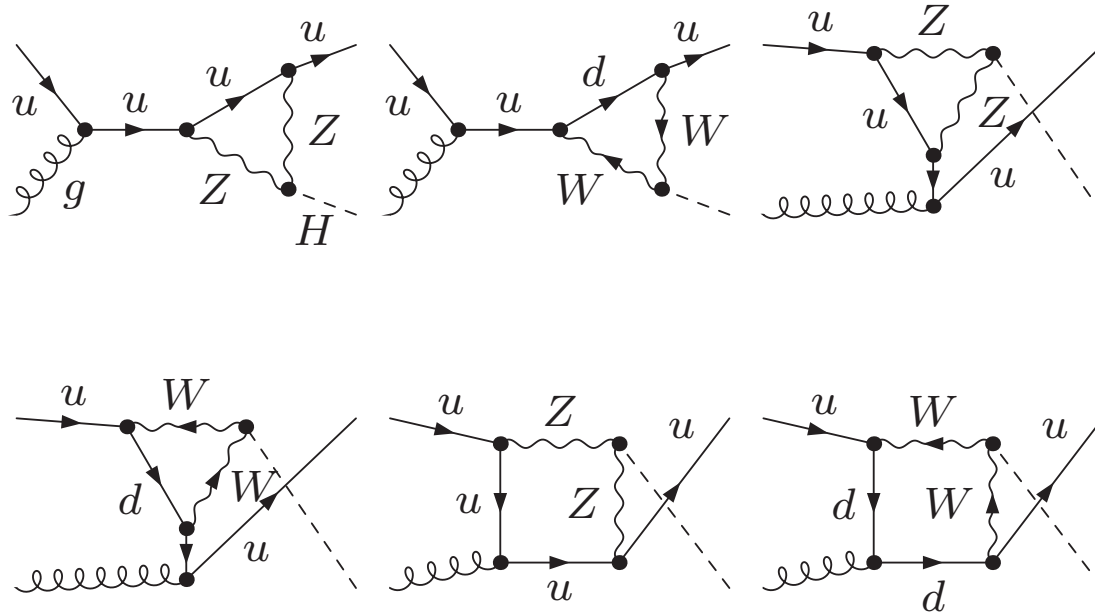
quark anti-quark annihilation, $b\bar{b} \rightarrow Hg$



– Light Quark (u, d, s, c) EW Contribution : $\mathcal{O}(\alpha_S \alpha^3)$

[Mrenna, Yuan '96; Keung, Petriello '09]

quark gluon scattering, $qg \rightarrow Hq$



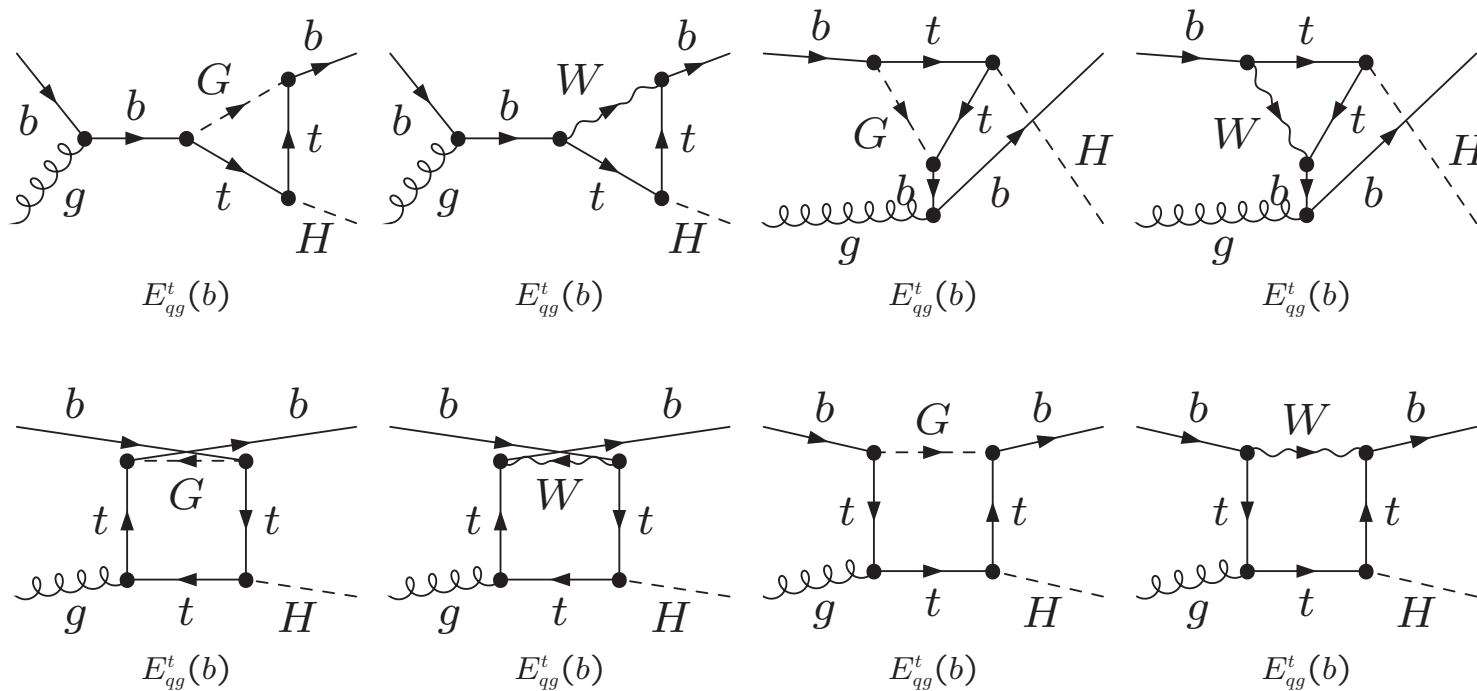
quark anti-quark annihilation, $q\bar{q} \rightarrow Hg$

crossed diagrams

[LO Contributions to Higgs + Jet]

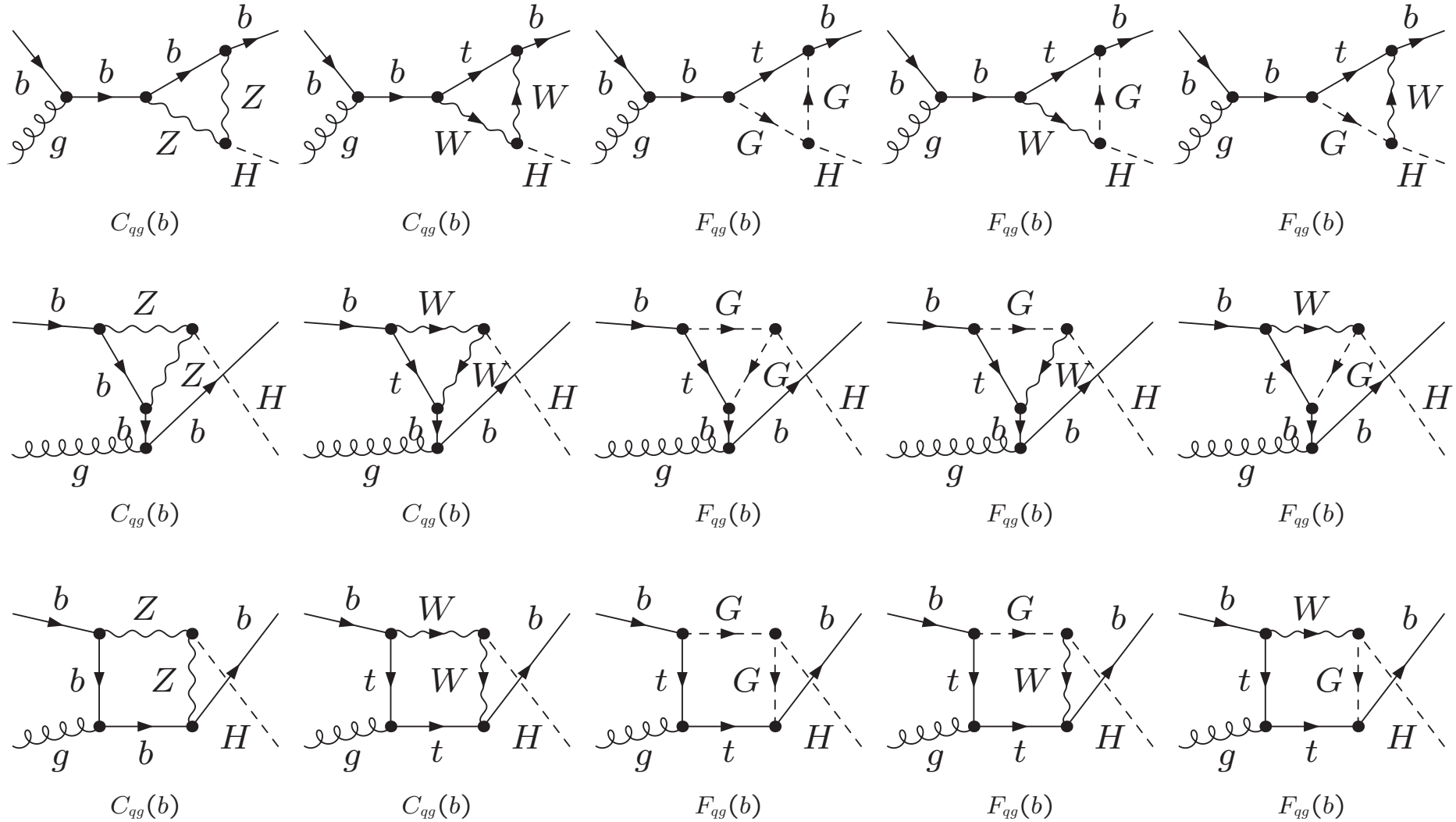
[Mrenna, Yuan '96]

– Bottom Quark EW Contribution : $\mathcal{O}(\alpha_S\alpha^3)$
 quark gluon scattering, $bg \rightarrow Hb$, $\mathcal{O}(\alpha_S\alpha^2\alpha_t)$



– Bottom Quark EW Contribution : $\mathcal{O}(\alpha_S\alpha^3)$

quark gluon scattering, $bg \rightarrow Hb$, $\mathcal{O}(\alpha_S\alpha^3)$ “non α_t ”



– Computational Approach

- respect the hierarchy of Yukawa couplings:

$$\alpha_q = y_q^2/4\pi = \frac{1}{4\pi}m_q^2/v^2 \quad (v = 246 \text{ GeV})$$

$$\rightarrow \alpha_t = 3.9 \cdot 10^{-2}, \quad \alpha_b = 2.3 \cdot 10^{-6} \quad \text{and} \quad \frac{\alpha_b}{\alpha_t} \approx \alpha^2(0) < \alpha_S^4(m_Z)$$

→ consider LO QCD and EW contributions to the full polynomial in $\sqrt{\alpha_t}$ and $\sqrt{\alpha_b}$ in the cross section predictions

- light quark (u, d, s, c) processes:

* full mass dependence in m_t, m_b

- bottom-quark processes:

* 5-flavour scheme:

- $m_b = 0$ to be consistent with parton model
- only b Yukawa coupling y_b retained non-zero

* for the tree-level amplitude: eff. Born approx. to NLO QCD corrections

- factorisation scale choice $\mu_F^{(b)} = m_H/4$
- NLO running m_b in b Yukawa coupling

scattering amplitudes

$$\mathcal{M}_{gg} = A_t g_S^3 y_t + A_b g_S^3 y_b,$$

$$\mathcal{M}_X(q) = B_X^t(q) g_S^3 y_t + B_X^b(q) g_S^3 y_b + C_X(q) g_S e^3,$$

$$\mathcal{M}_X(b) = D_X(b) g_S y_b + B_X^t(b) g_S^3 y_t + E_X^t(b) g_S e^2 y_t + (C_X(b) + F_X(b)) g_S e^3,$$

with $X \in \{qg, \bar{q}g, q\bar{q}\}$ and $q = u, d, s, c$.

squared matrix elements, for $m_b = 0$:

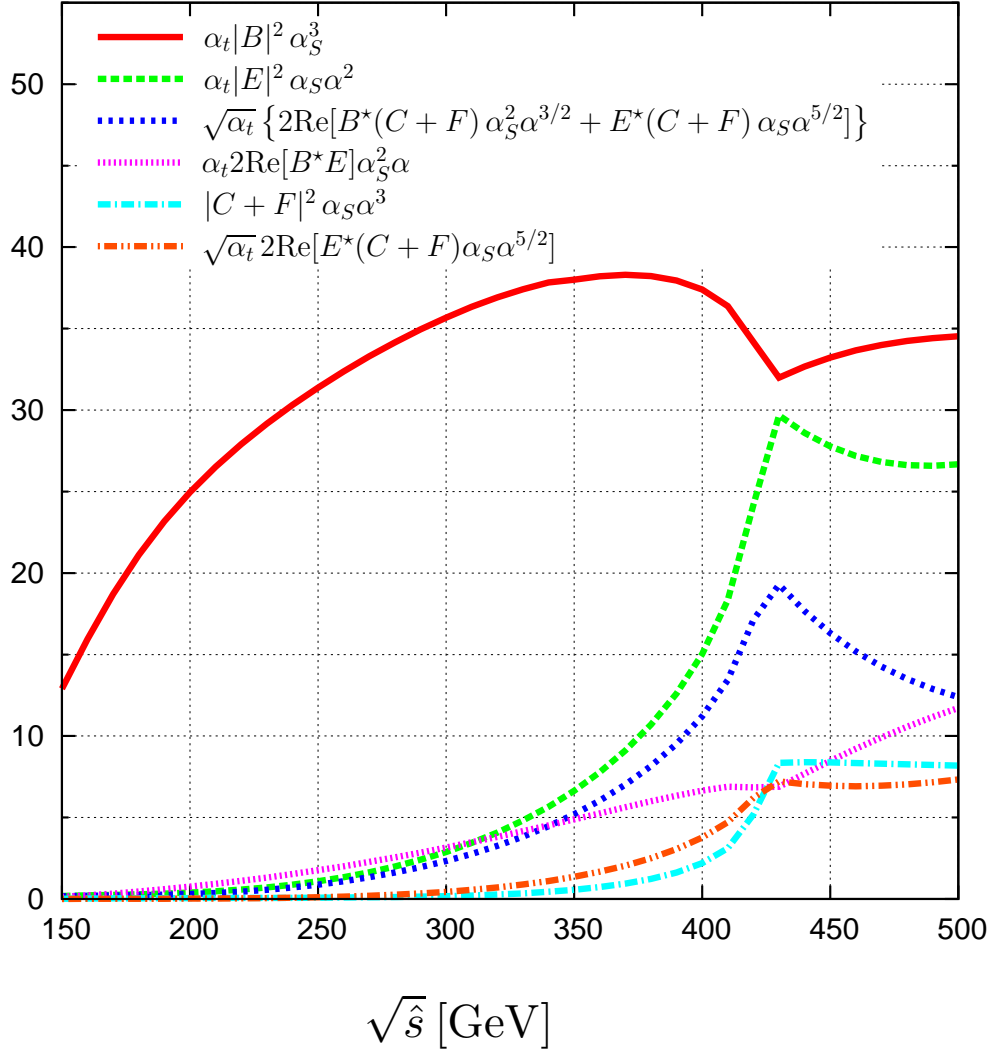
$$|\mathcal{M}_{gg}|^2 / (4\pi)^4 = \alpha_t |A_t|^2 \alpha_S^3 + \alpha_b |A_b|^2 \alpha_S^3 + \sqrt{\alpha_t \alpha_b} 2 \text{Re}[A_t^* A_b] \alpha_S^3,$$

squared matrix elements, for $m_b = 0$:

$$\begin{aligned}
|\mathcal{M}_X(q)|^2/(4\pi)^4 = & \\
& \alpha_t |B_X^t(q)|^2 \alpha_S^3 + \alpha_b |B_X^b(q)|^2 \alpha_S^3 \\
& + \sqrt{\alpha_t \alpha_b} \left\{ 2\text{Re} \left[(B_X^t(q))^* B_X^b(q) \right] \alpha_S^3 \right\} \\
& + \sqrt{\alpha_t} \left\{ 2\text{Re} \left[(B_X(q)^t)^* C_X(q) \right] \alpha_S^2 \alpha \sqrt{\alpha} \right\} \\
& + \sqrt{\alpha_b} \left\{ 2\text{Re} \left[(B_X(q)^b)^* C_X(q) \right] \alpha_S^2 \alpha \sqrt{\alpha} \right\} \\
& + |C_X(q)|^2 \alpha_S \alpha^3,
\end{aligned}$$

$$\begin{aligned}
|\mathcal{M}_X(b)|^2/(4\pi)^4 = & \\
& \alpha_t \left\{ |B_X^t(b)|^2 \alpha_S^3 + 2\text{Re} \left[(B_X^t(b))^* E_X^t(b) \right] \alpha_S^2 \alpha + |E_X^t(b)|^2 \alpha_S \alpha^2 \right\} \\
& + \alpha_b \left\{ |D_X(b)|^2 \alpha_S \right\} (4\pi)^{-2} \\
& + \sqrt{\alpha_t} \left\{ 2\text{Re} \left[(B_X^t(b))^* (C_X(b) + F_X(b)) \right] \alpha_S^2 \alpha \sqrt{\alpha} \right. \\
& \quad \left. + 2\text{Re} \left[(E_X^t(b))^* (C_X(b) + F_X(b)) \right] \alpha_S \alpha^2 \sqrt{\alpha} \right\} \\
& + |C_X(b) + F_X(b)|^2 \alpha_S \alpha^3.
\end{aligned}$$

[contribution to $|\mathcal{M}_{qg}(b)|^2/|\mathcal{M}_{qg}(b)|^2$ [%]



$$\mathcal{M}_{qg}(b) = D_{qg}(b)g_S y_b + B_{qg}^t(b)g_S^3 y_t + E_{qg}^t(b)g_S e^2 y_t + (C_{qg}(b) + F_{qg}(b))g_S e^3$$

$$|\mathcal{M}_{qg}(b)|^2/(4\pi)^4 = \alpha_b \left\{ |D_{qg}(b)|^2 \alpha_S \right\} (4\pi)^{-2} + \alpha_t \left\{ |B_{qg}^t(b)|^2 \alpha_S^3 + 2\text{Re} [B_{qg}^{*\,t}(b) E_{qg}^t(b)] \alpha_S^2 \alpha + |E_{qg}^t(b)|^2 \alpha_S \alpha^2 \right\} + \sqrt{\alpha_t} \left\{ 2\text{Re} [B_{qg}^{*\,t}(b) (C_{qg}(b) + F_{qg}(b))] \alpha_S^2 \alpha \sqrt{\alpha} + 2\text{Re} [E_{qg}^{*\,t}(b) (C_{qg}(b) + F_{qg}(b))] \alpha_S \alpha^2 \sqrt{\alpha} \right\} + |C_{qg}(b) + F_{qg}(b)|^2 \alpha_S \alpha^3.$$

- Numerical Results

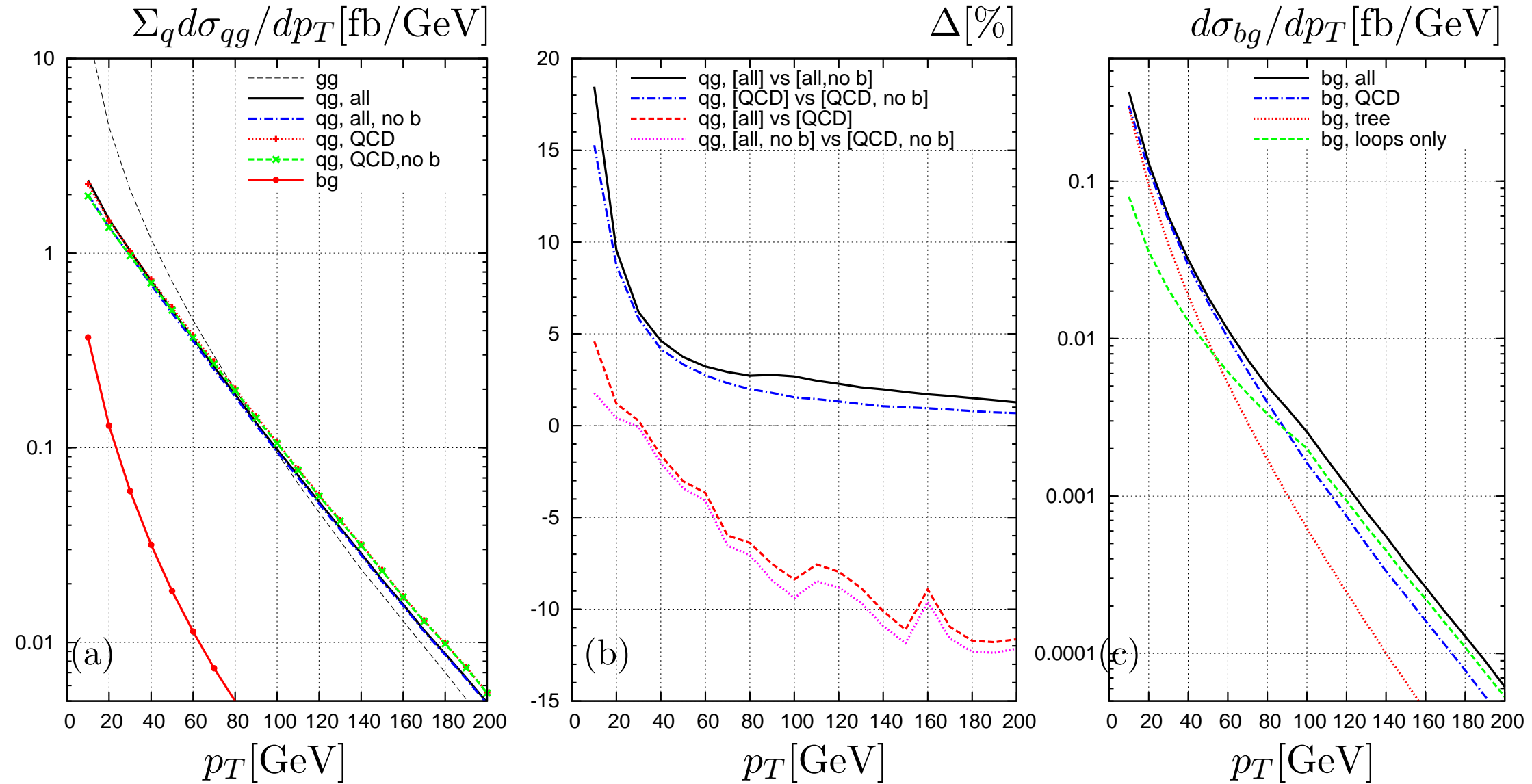
– Tevatron

differential hadronic cross sections for $\sqrt{S} = 1.96$ TeV

$$\frac{d\sigma(S, p_{T,\text{jet}})}{dp_{T,\text{jet}}}, \quad |\eta_{\text{jet}}| < 2.5$$

$$\frac{d\sigma(S, \eta_{\text{jet}})}{d\eta_{\text{jet}}}, \quad p_{T,\text{jet}} > 15 \text{ GeV}$$

$p_{T,\text{jet}}$ distribution : quark-gluon scattering ($m_H = 120$ GeV)

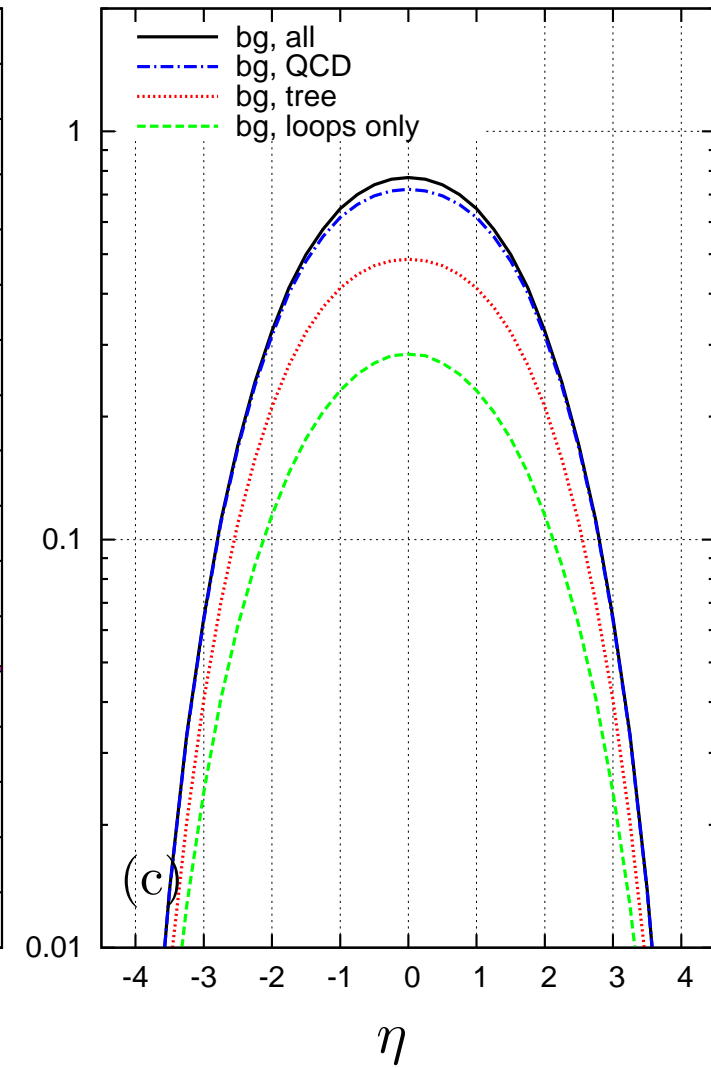
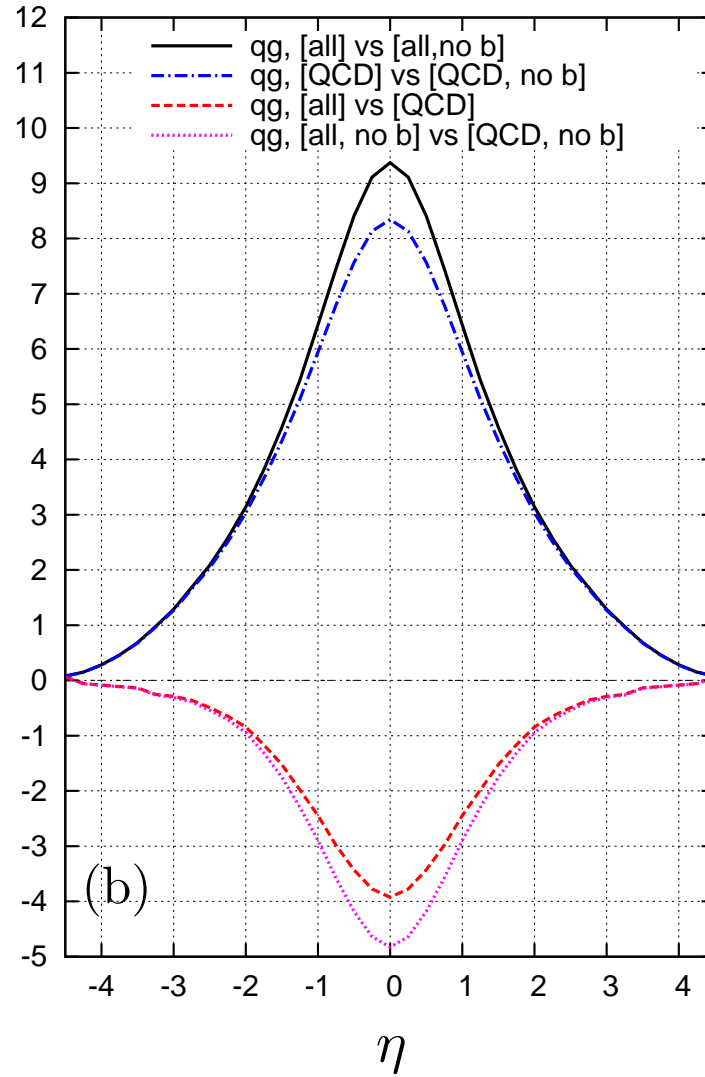
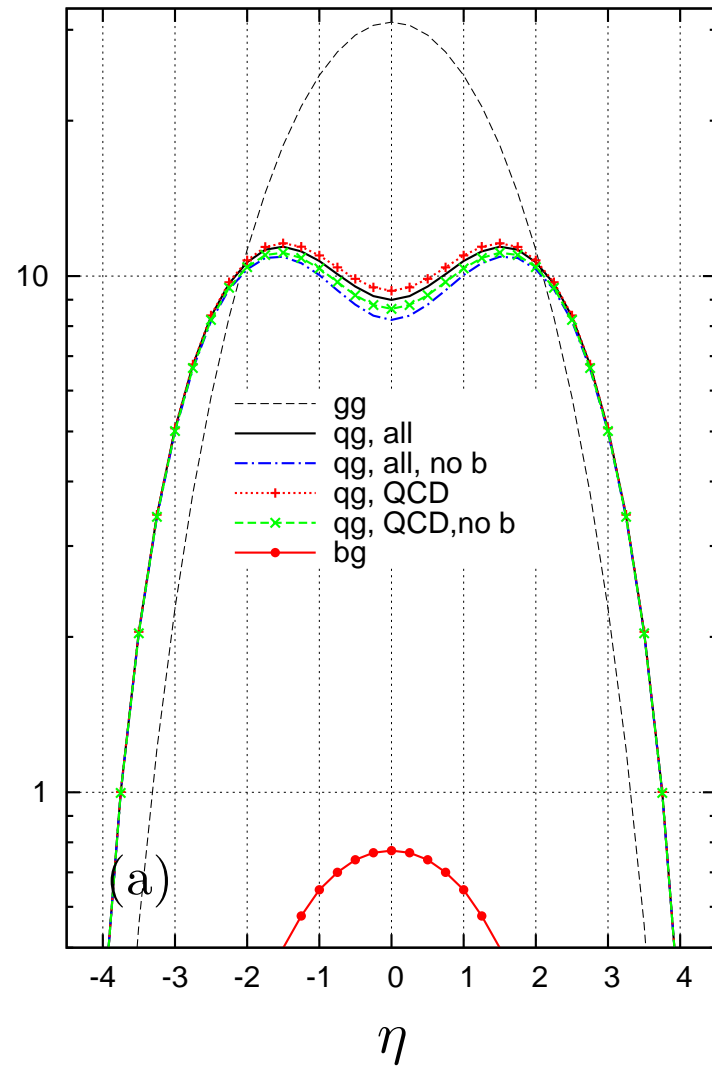


η_{jet} distribution : quark-gluon scattering ($m_H = 120 \text{ GeV}$)

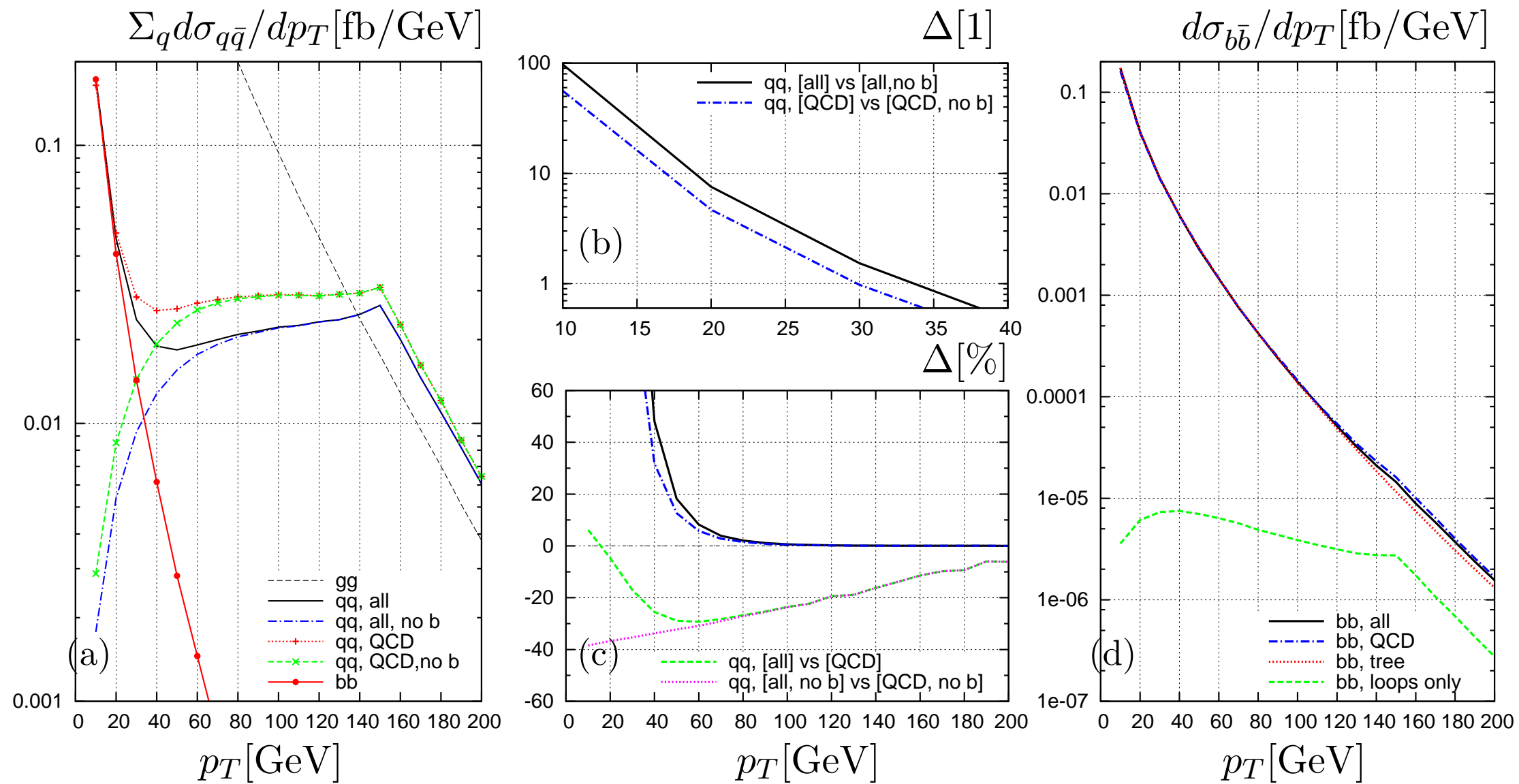
$\Sigma_q d\sigma_{qg}/d\eta [\text{fb}]$

$\Delta [\%]$

$d\sigma_{bg}/d\eta [\text{fb}]$

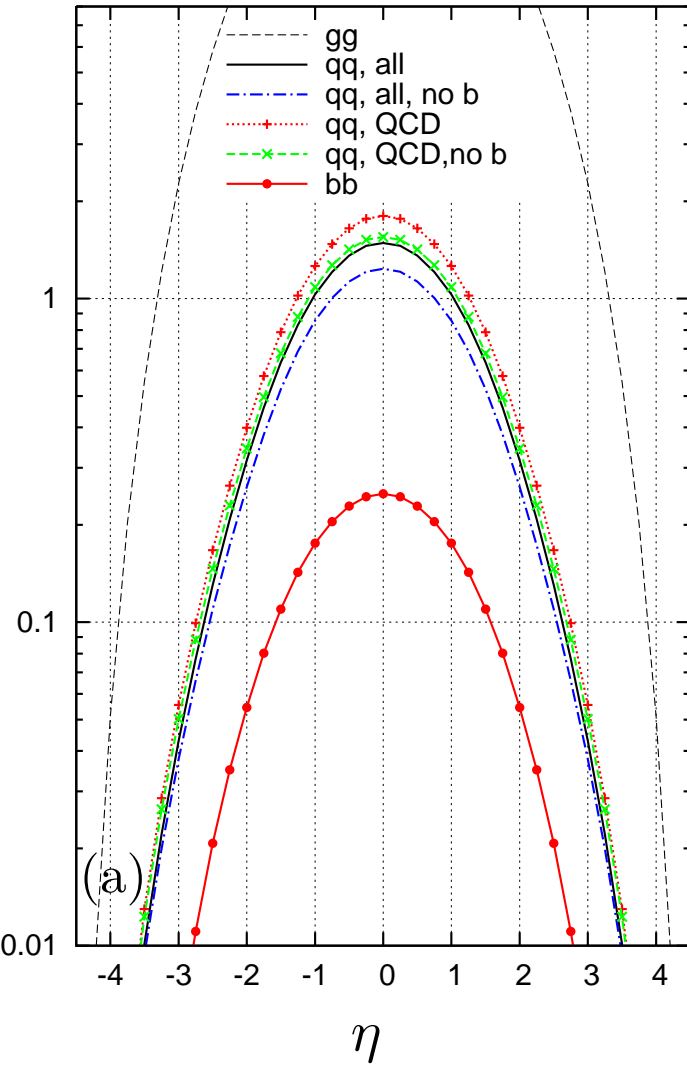


$p_{T,\text{jet}}$ distribution : $q\bar{q}$ annihilation ($m_H = 120$ GeV)

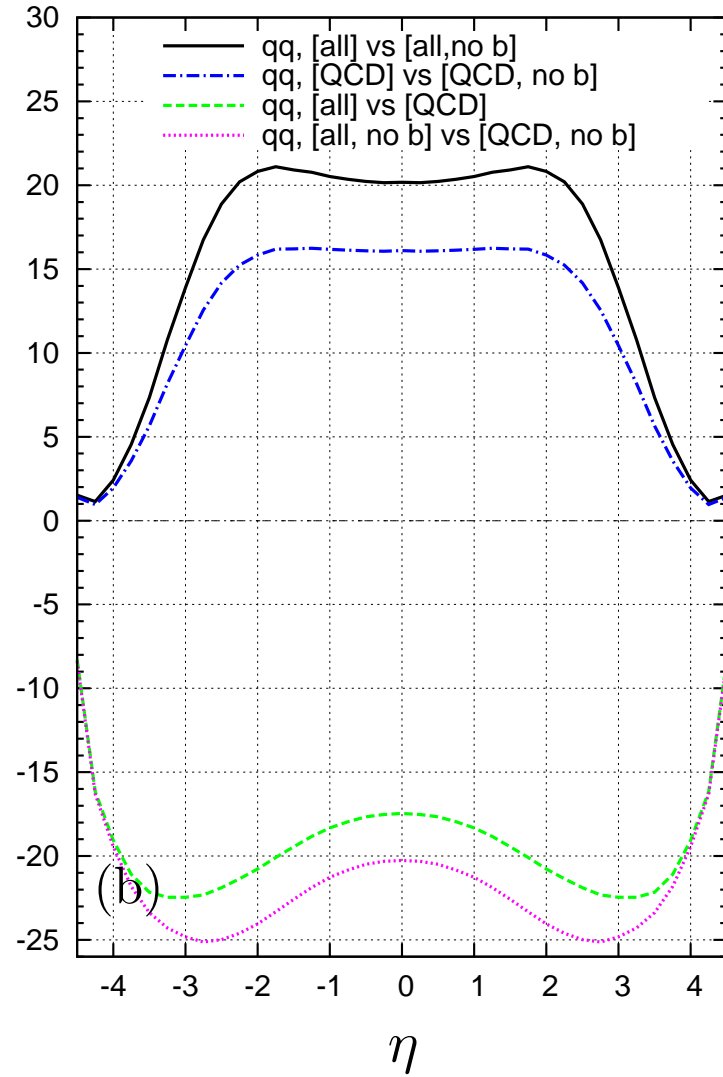


η_{jet} distribution : $q\bar{q}$ annihilation ($m_H = 120$ GeV)

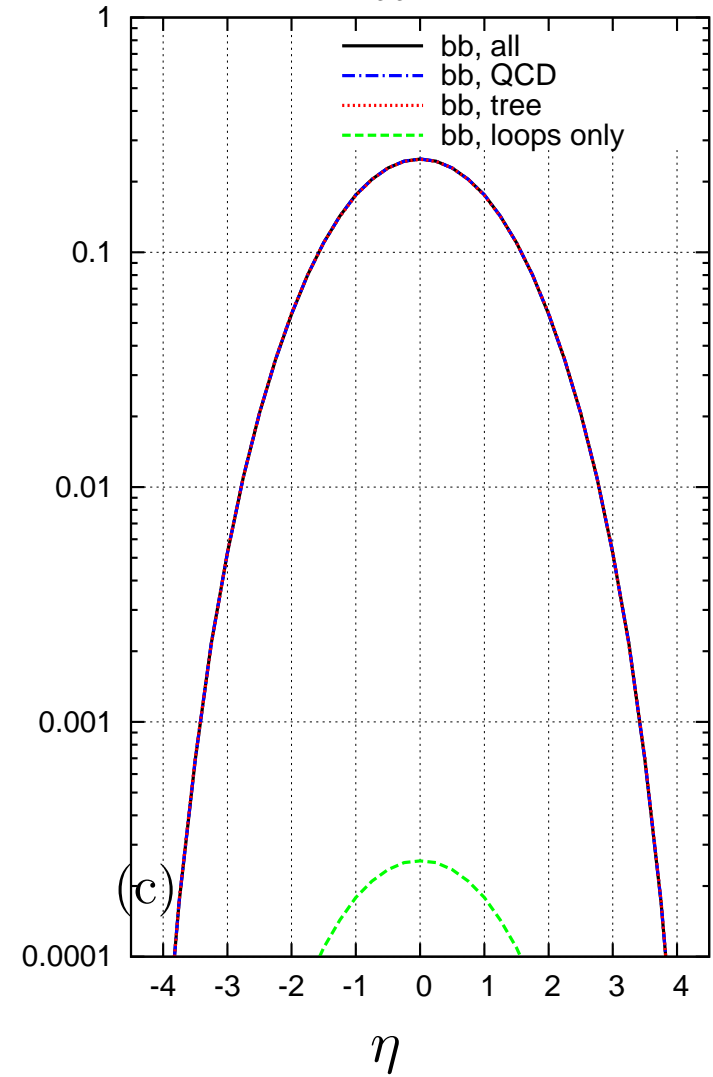
$\Sigma_q d\sigma_{q\bar{q}}/d\eta [\text{fb}]$



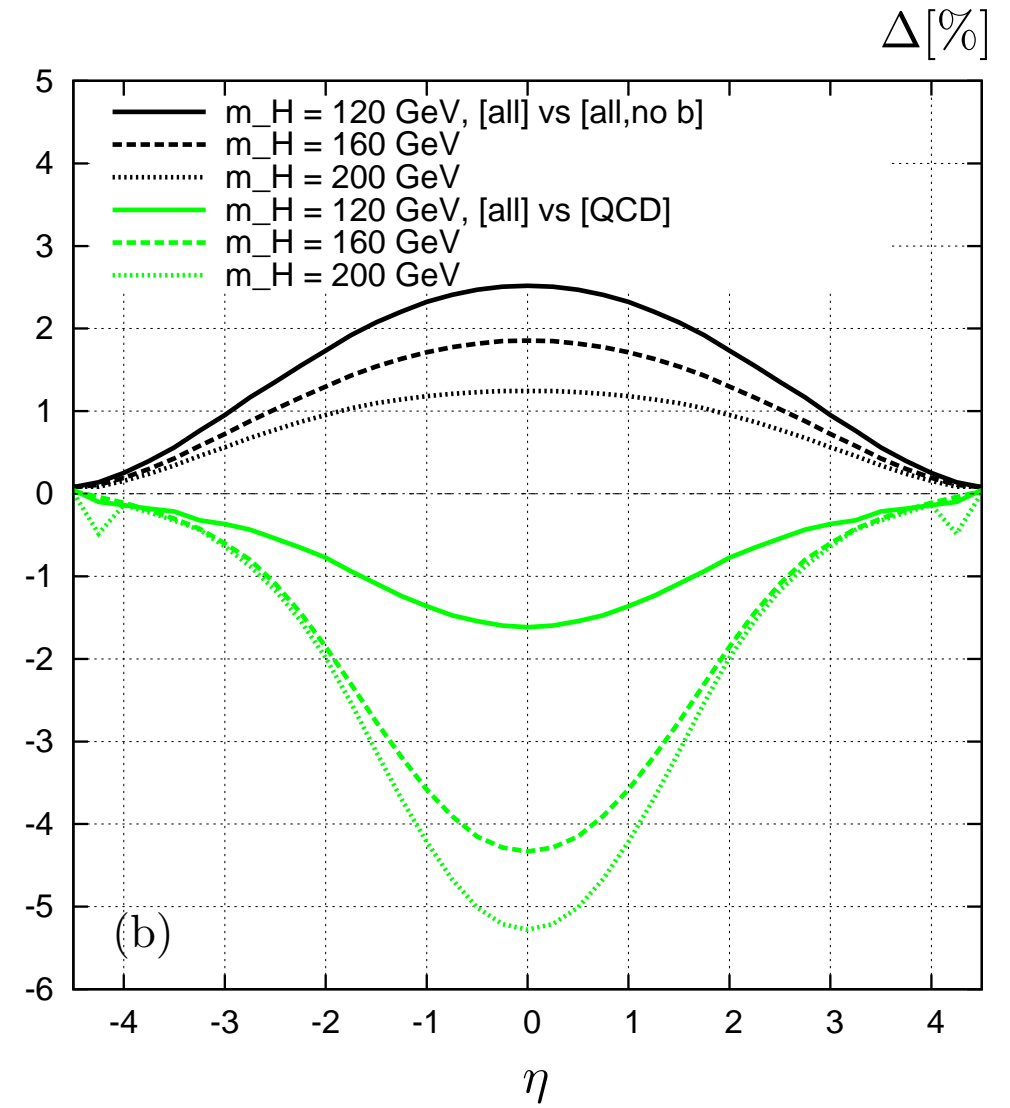
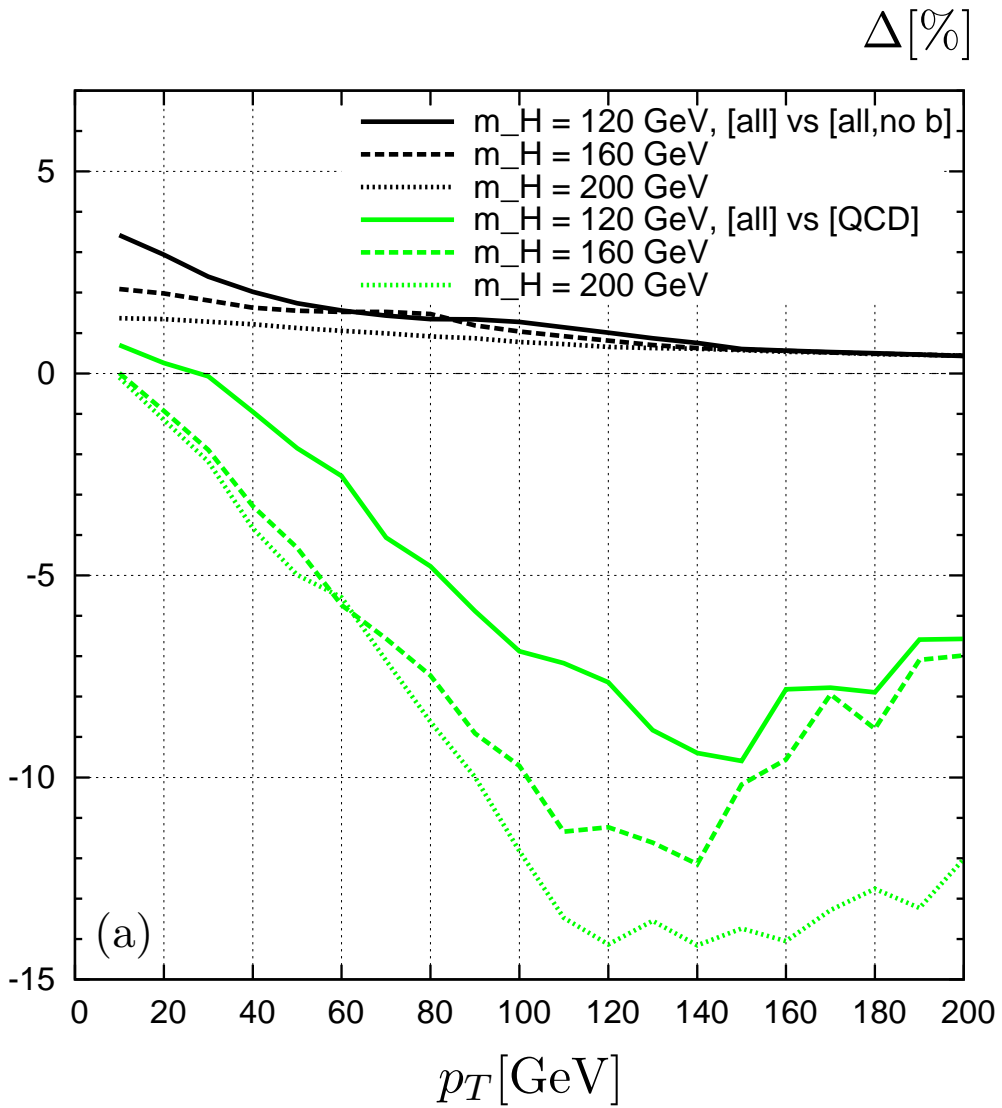
$\Delta [\%]$



$d\sigma_{b\bar{b}}/d\eta [\text{fb}]$



effects on the of the total Higgs + Jet distributions: ($m_H = 120$ GeV)



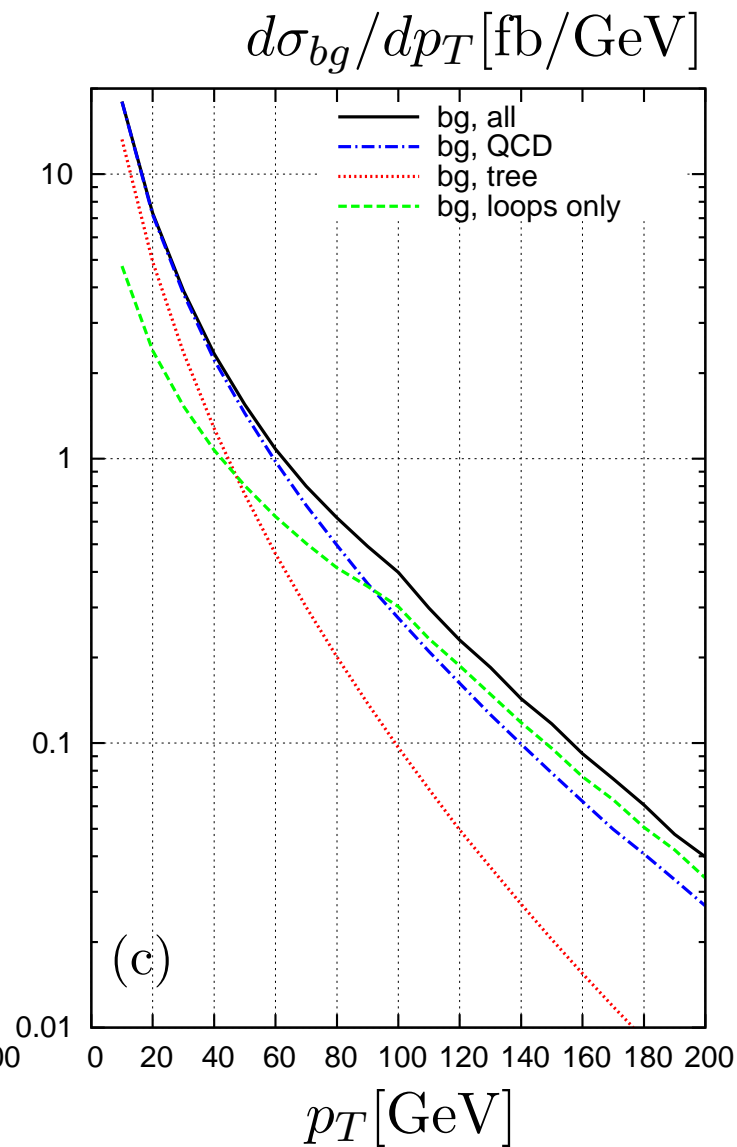
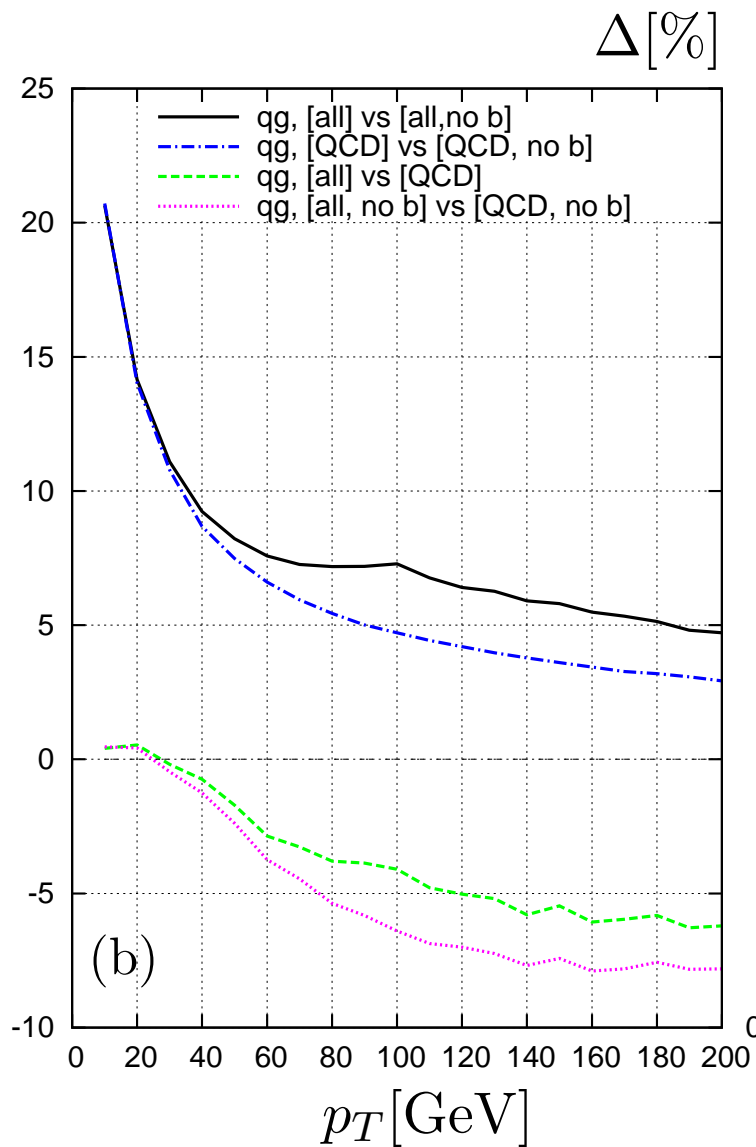
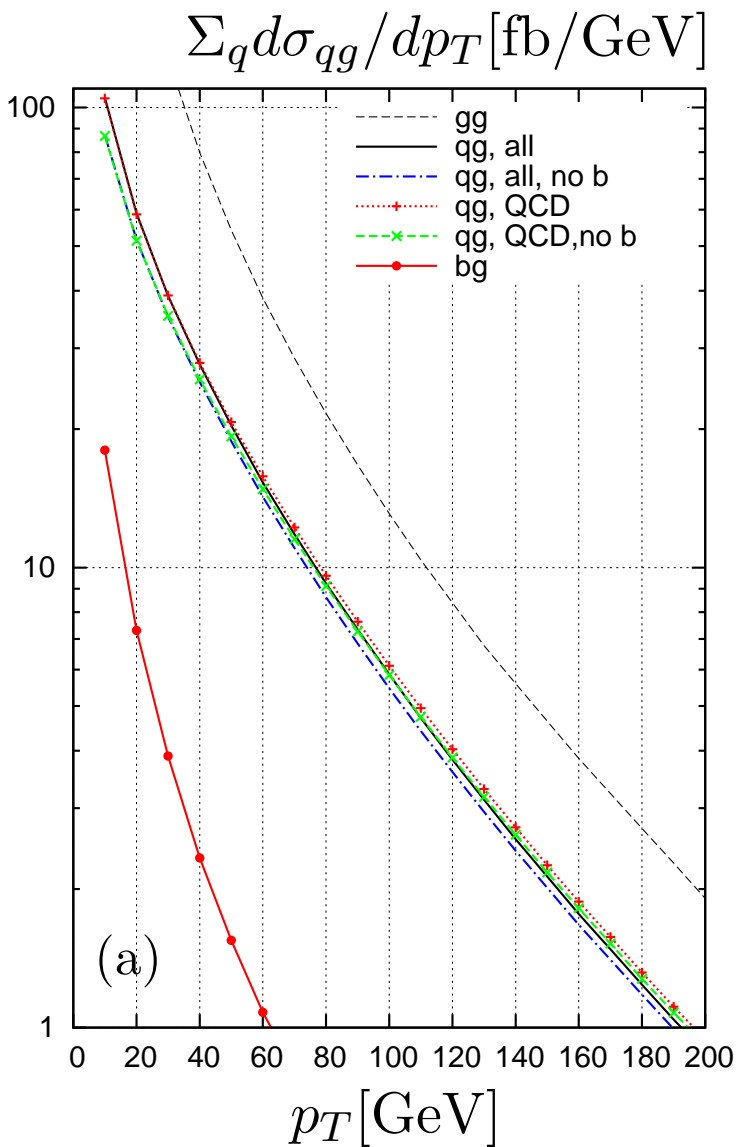
– LHC

differential hadronic cross sections for $\sqrt{S} = 10$ TeV

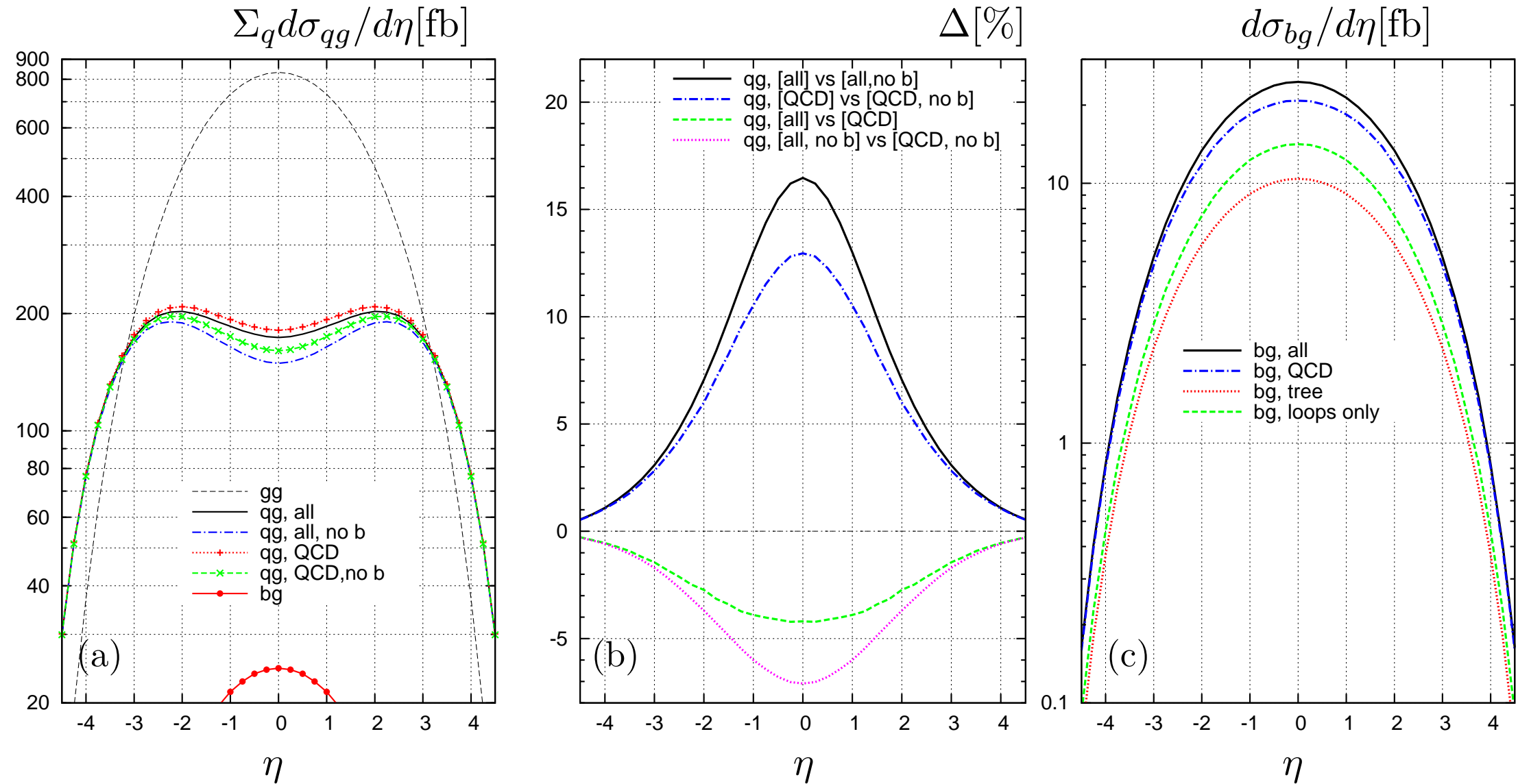
$$\frac{d\sigma(S, p_{T,\text{jet}})}{dp_{T,\text{jet}}}, \quad |\eta_{\text{jet}}| < 4.5$$

$$\frac{d\sigma(S, \eta_{\text{jet}})}{d\eta_{\text{jet}}}, \quad p_{T,\text{jet}} > 30 \text{ GeV}$$

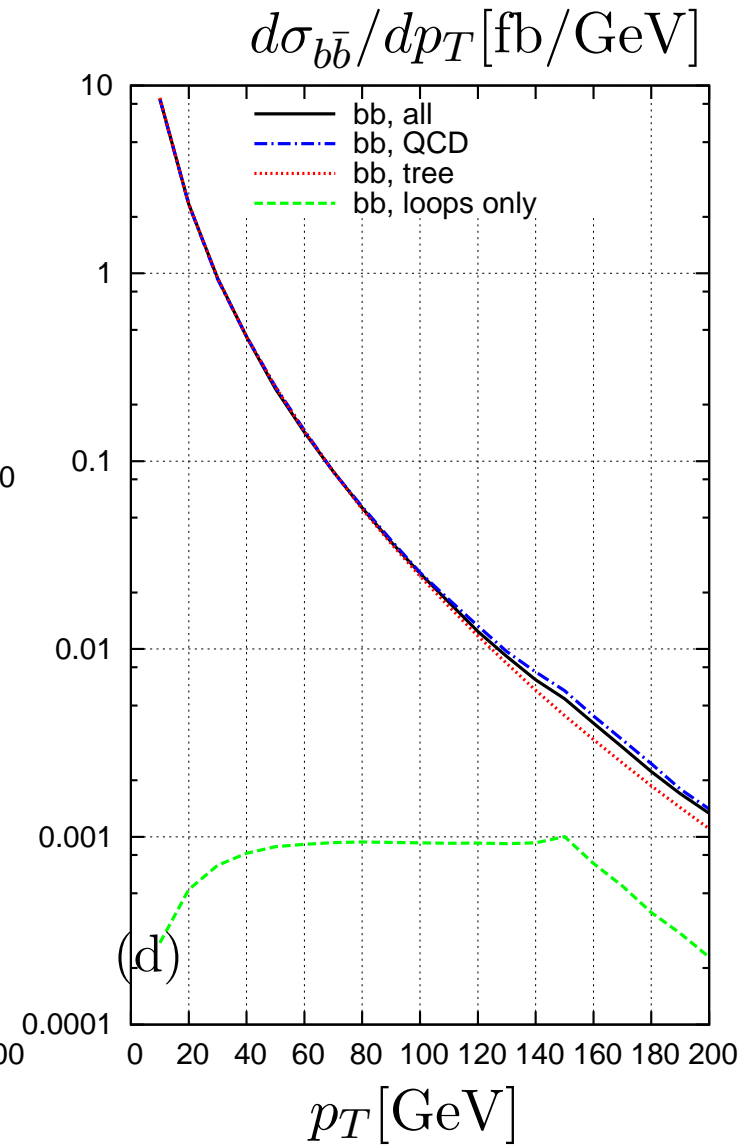
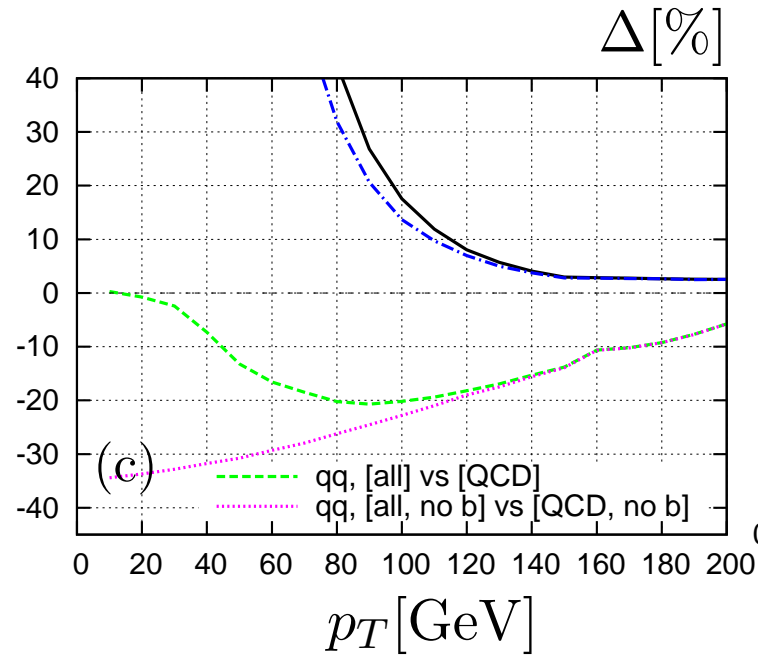
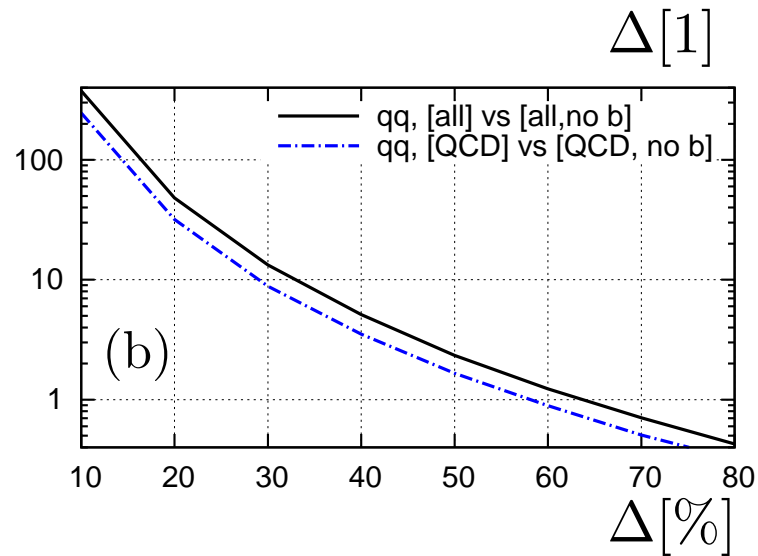
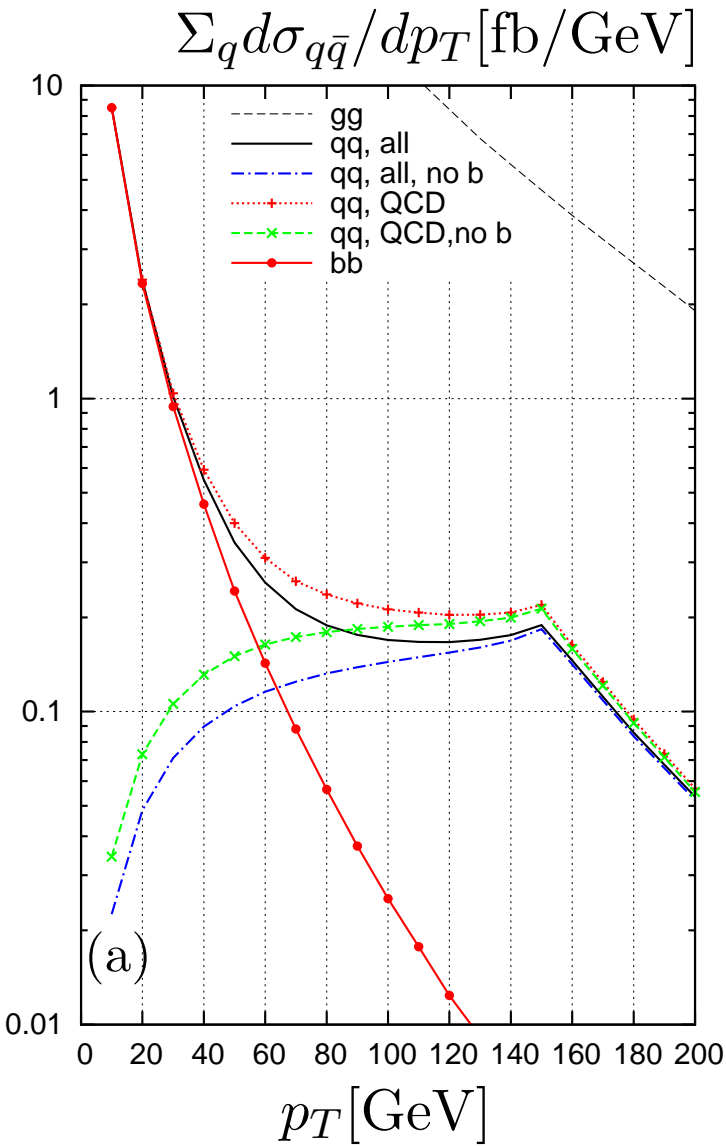
$p_{T,\text{jet}}$ distribution : quark-gluon scattering ($m_H = 120$ GeV)



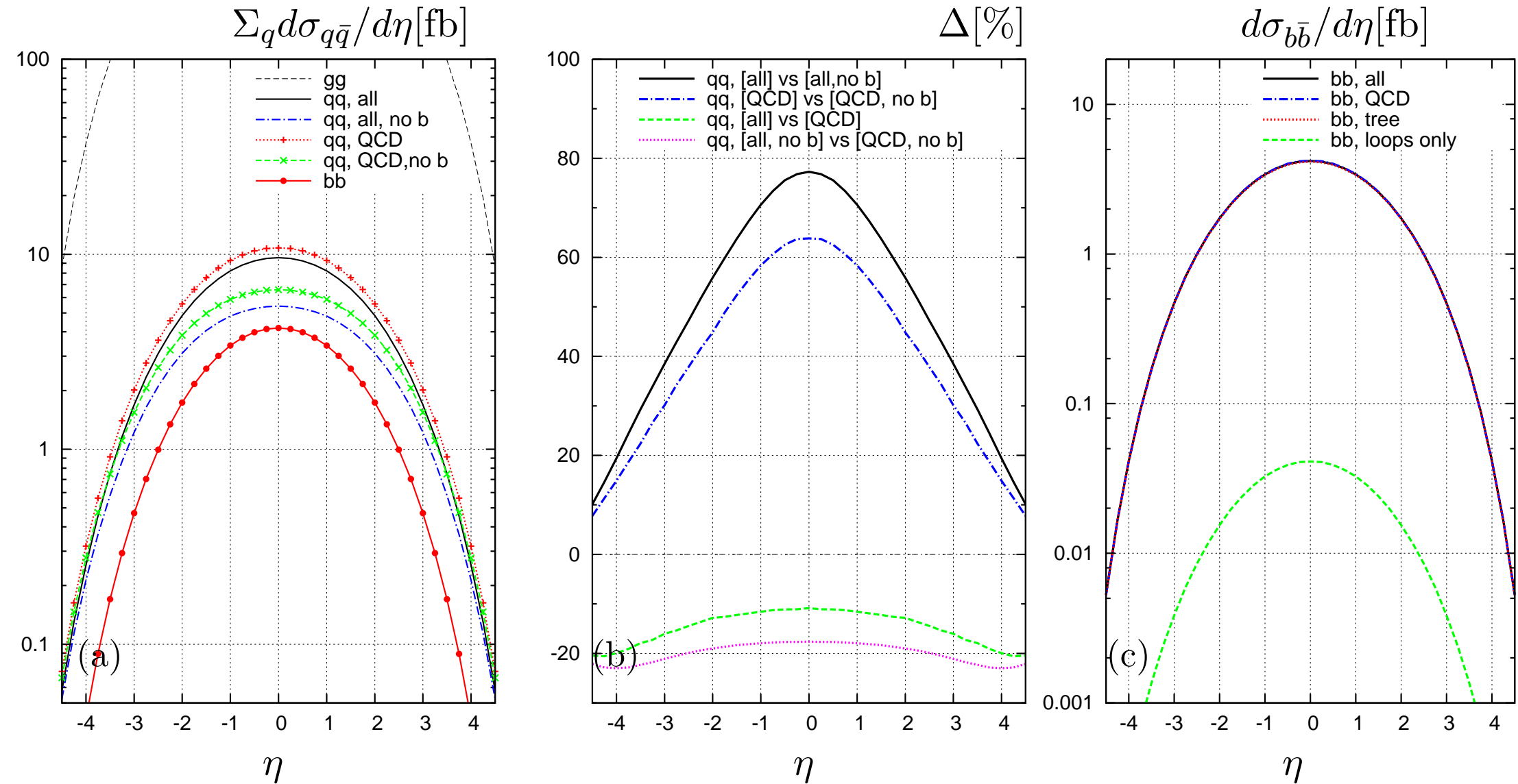
η_{jet} distribution : quark–gluon scattering ($m_H = 120 \text{ GeV}$)



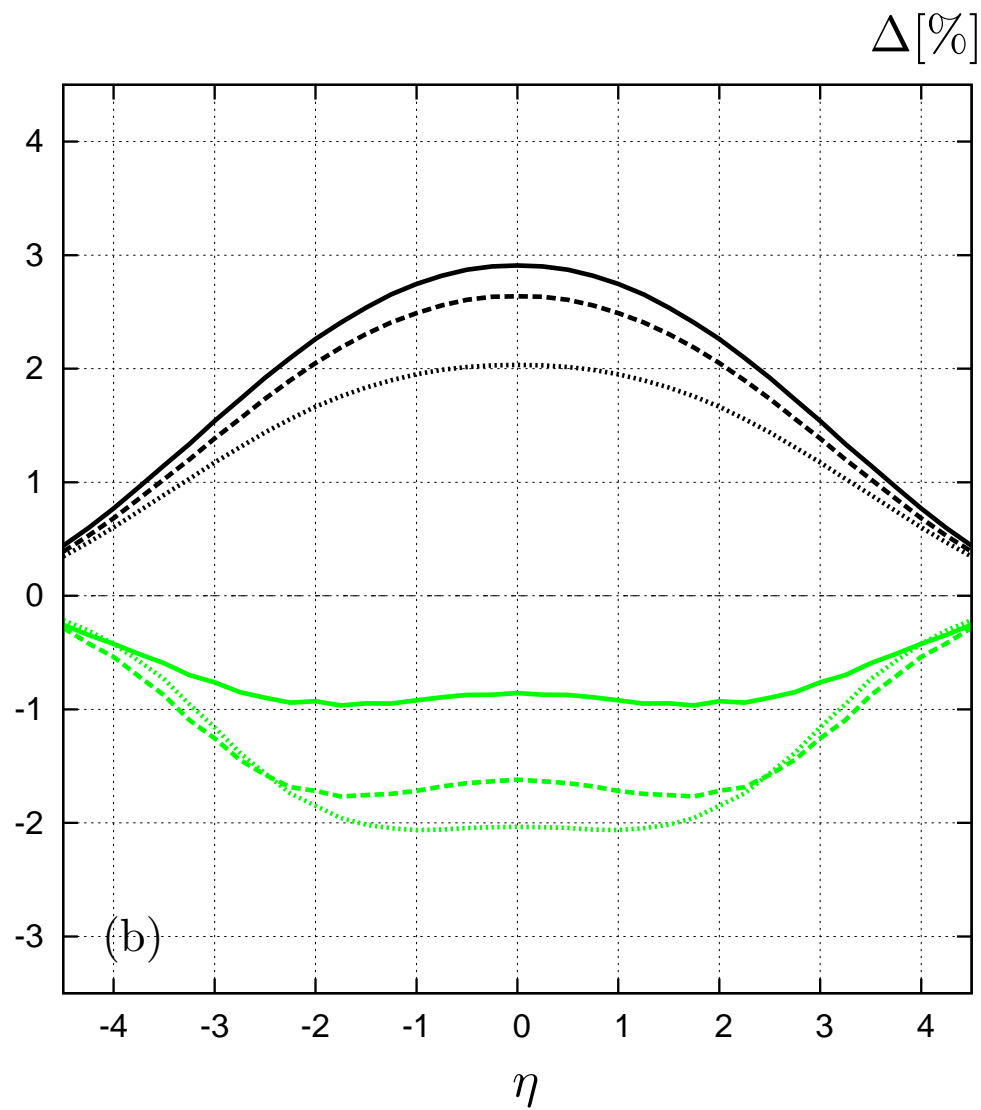
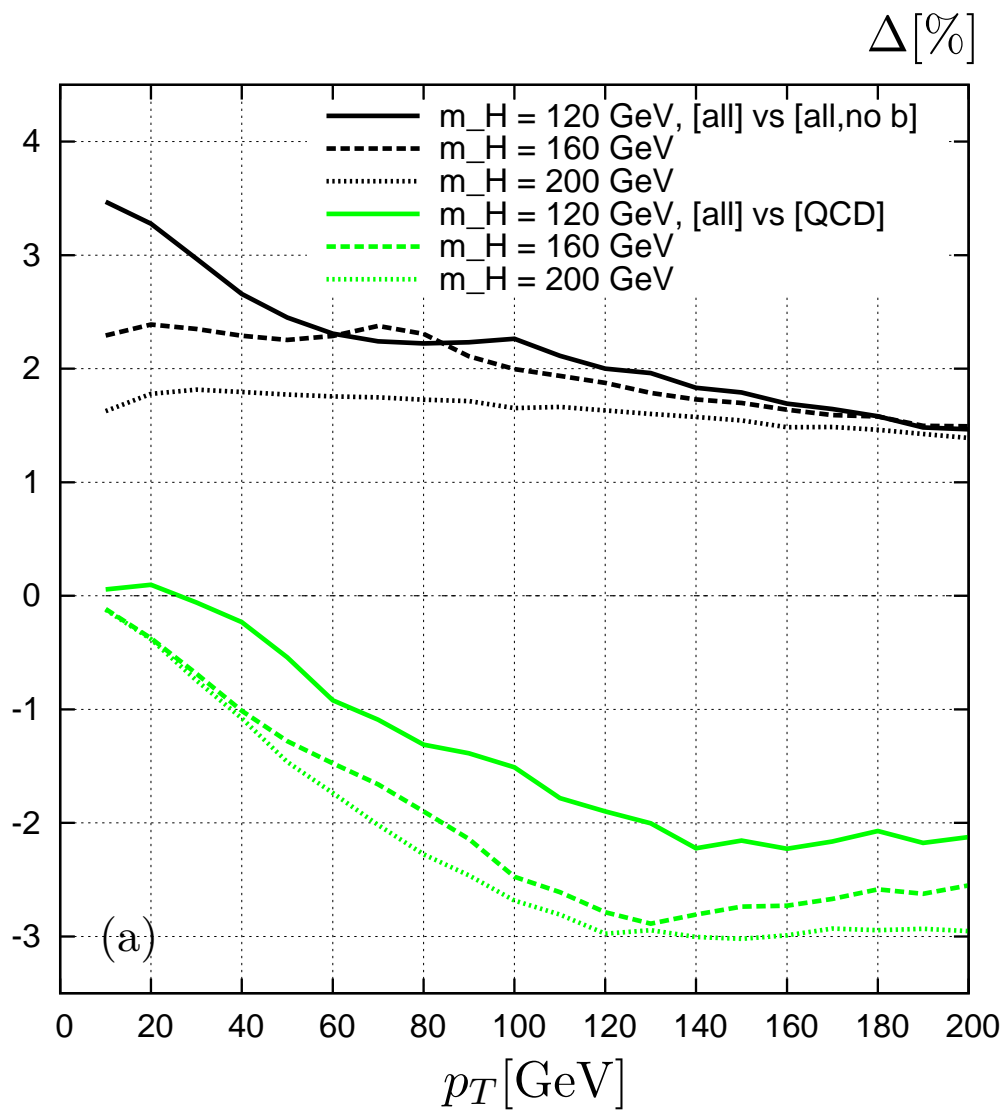
$p_{T,\text{jet}}$ distribution : $q\bar{q}$ annihilation ($m_H = 120$ GeV)



η_{jet} distribution : $q\bar{q}$ annihilation ($m_H = 120$ GeV)



effects on the of the total Higgs + Jet distributions: ($m_H = 120$ GeV)



summary

- SM simulations show: Higgs + high- p_T jet production is a promising supplement to the inclusive production.
- More precise predictions are needed in order to be useful for experimental analyses at the LHC.
- Improvements over the present NLO QCD accuracy for the H + jet final state can be made by considering:
 - going beyond the large m_t approx in NLO QCD
 - NNLO QCD contributions
 - electroweak one-loop contributions
 - bottom parton process contributions