

# $VVjj$ production at the LHC – a Standard Model perspective



## *Anomalous Quartic Gauge Couplings*

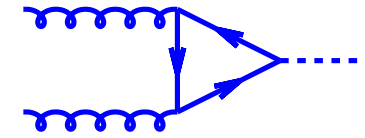
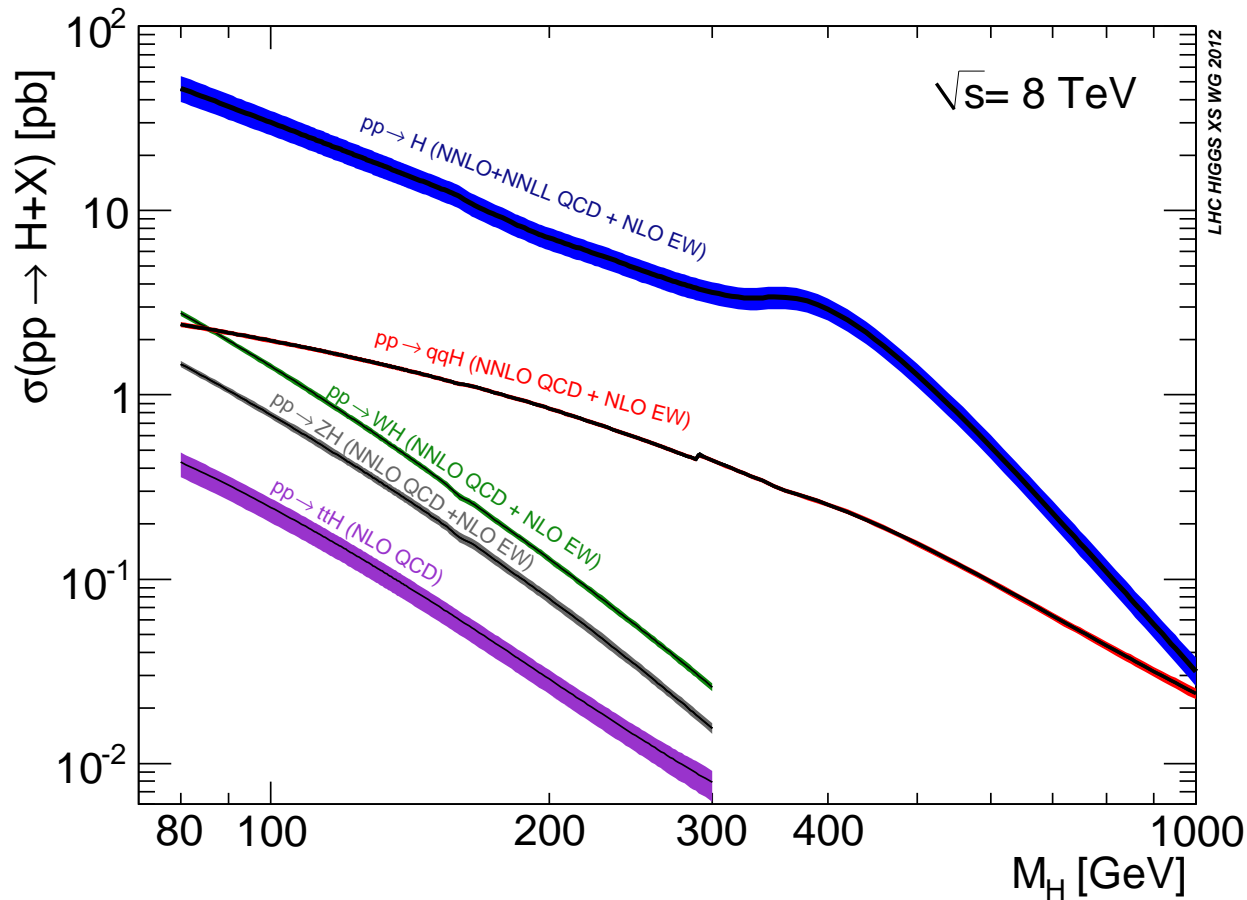
Dresden – September 2013

Barbara Jäger

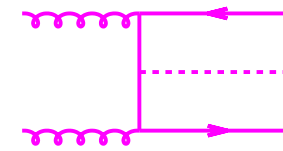
Johannes Gutenberg University Mainz

# Higgs production @ LHC

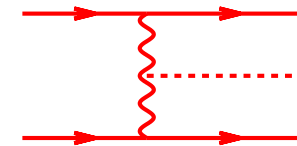
Higgs cross section WG



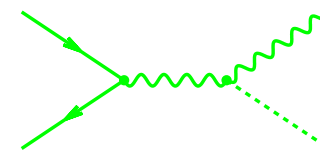
gluon fusion (GF)



$t\bar{t}H$  production



vector boson fusion (VBF)



$W, Z$  bremsstrahlung

## vector boson fusion (VBF)

### ❖ important production mode for:

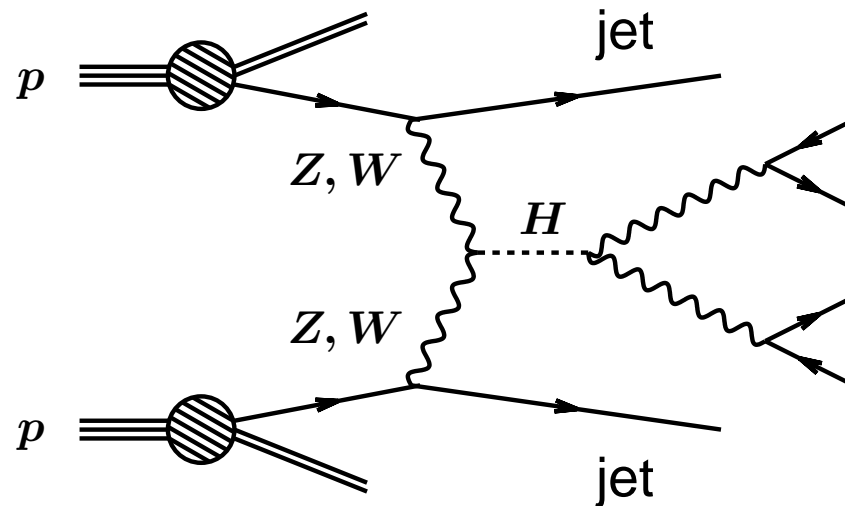
- Higgs boson at  $M_H = 126$ ,
- heavy Higgs boson(s),
- scalar bosons in new physics scenarios

- ❖ perturbatively well under control
- ❖ experimentally clean signature

### ❖ sensitive to Higgs couplings and CP properties

☞ accurate predictions essential!

# $pp \rightarrow Hjj$ via VBF: event topology



suppressed color exchange between quark lines gives rise to

- ❖ little jet activity in central rapidity region
- ❖ scattered quarks  $\rightarrow$  two forward tagging jets (energetic; large rapidity)
- ❖ Higgs decay products typically between tagging jets

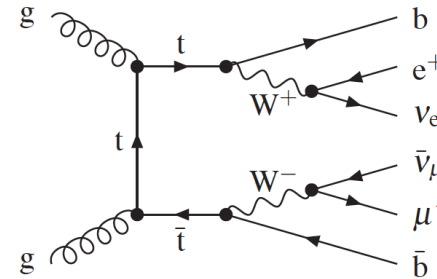
# VBF: signal & backgrounds

distinct event topology of the Higgs signal in

$$pp \rightarrow Hjj \text{ via VBF with}$$
$$H \rightarrow W^+W^- \rightarrow e^\pm \mu^\mp p_T$$

→ important for **suppression of backgrounds**

❖  $t\bar{t} + 0, 1, 2$  jets production  
(note:  $t\bar{t} \rightarrow W^+W^-b\bar{b}$ )



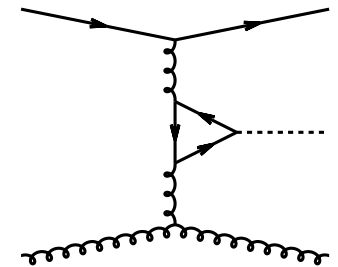
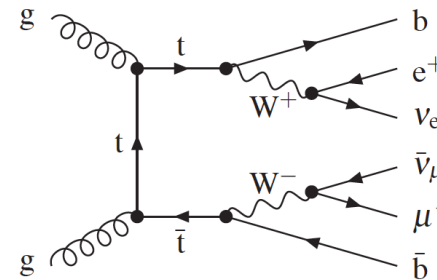
# VBF: signal & backgrounds

distinct event topology of the Higgs signal in

$$pp \rightarrow Hjj \text{ via VBF with}$$
$$H \rightarrow W^+W^- \rightarrow e^\pm \mu^\mp p_T$$

→ important for **suppression of backgrounds**

❖  $t\bar{t} + 0, 1, 2$  jets production  
(note:  $t\bar{t} \rightarrow W^+W^-b\bar{b}$ )



❖  $pp \rightarrow Hjj$  via gluon fusion  
(followed by  $H \rightarrow W^+W^-$ )

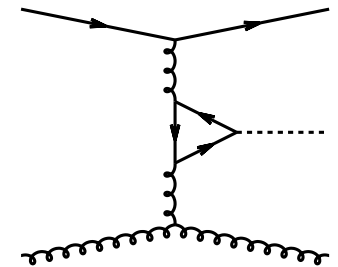
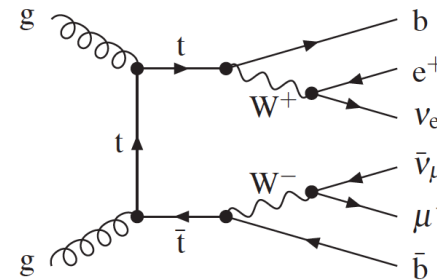
# VBF: signal & backgrounds

distinct event topology of the Higgs signal in

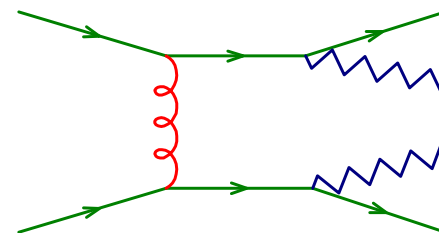
$$pp \rightarrow Hjj \text{ via VBF with}$$
$$H \rightarrow W^+W^- \rightarrow e^\pm \mu^\mp p_T$$

→ important for **suppression of backgrounds**

❖  $t\bar{t} + 0, 1, 2$  jets production  
(note:  $t\bar{t} \rightarrow W^+W^-b\bar{b}$ )



❖  $pp \rightarrow Hjj$  via gluon fusion  
(followed by  $H \rightarrow W^+W^-$ )



❖ QCD  $W^+W^-jj$  production

# VBF: signal & backgrounds

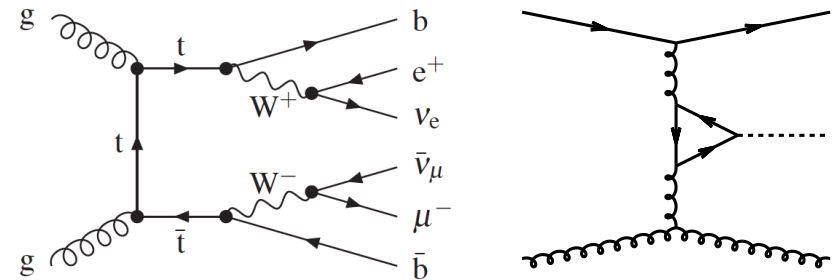
distinct event topology of the Higgs signal in

$$pp \rightarrow Hjj \text{ via VBF with}$$

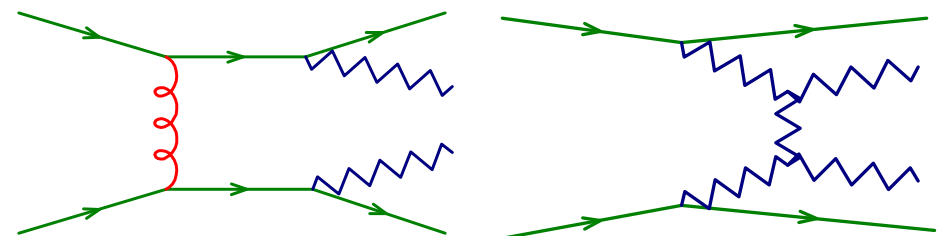
$$H \rightarrow W^+W^- \rightarrow e^\pm \mu^\mp p_T$$

→ important for **suppression of backgrounds**

❖  $t\bar{t} + 0, 1, 2$  jets production  
(note:  $t\bar{t} \rightarrow W^+W^-b\bar{b}$ )



❖  $pp \rightarrow Hjj$  via gluon fusion  
(followed by  $H \rightarrow W^+W^-$ )



❖ QCD  $W^+W^-jj$  production

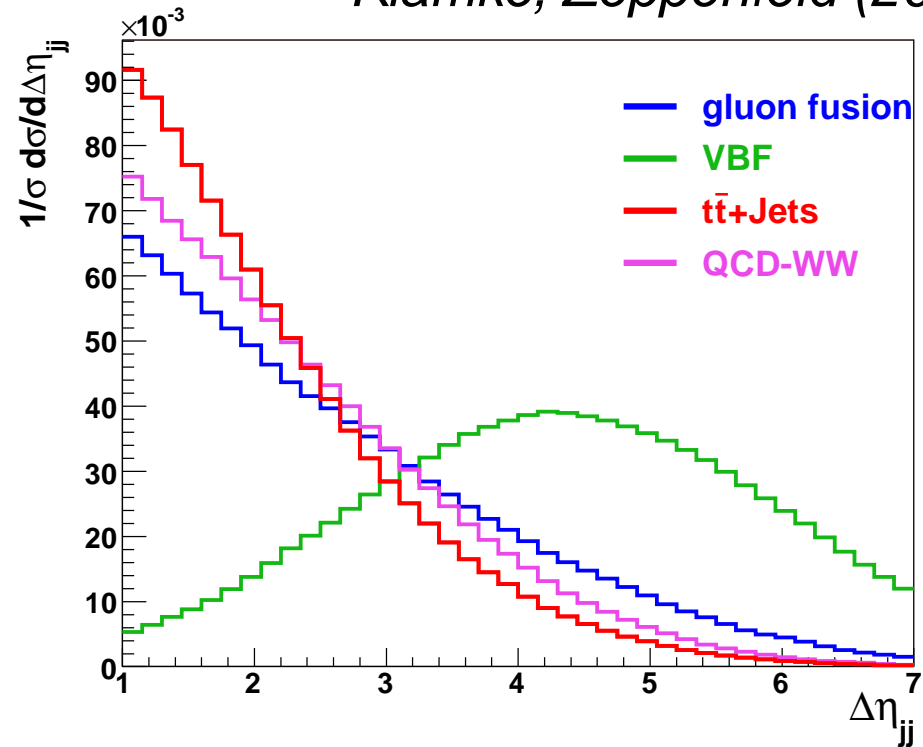
❖ EW  $W^+W^-jj$  production



# tagging jets: properties

rapidity separation of the tagging jets

*Klämke, Zeppenfeld (2007)*



**jets more central** in QCD- than in EW-induced production processes

# angular distribution of charged leptons

in  $H \rightarrow W^+W^-$ : spins anti-correlated



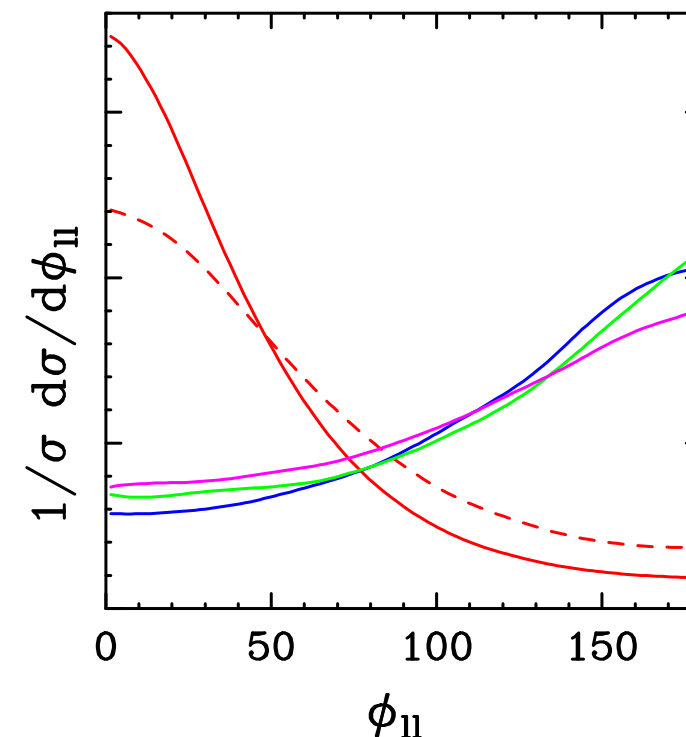
leptons emitted preferentially in same direction

no such correlation, if  $W$  bosons do not stem from the Higgs

*Dittmar, Dreiner (1996)*

distribution for EW  $W^+W^-$  production significantly different from Higgs signal

*Rainwater, Zeppenfeld (1999)*

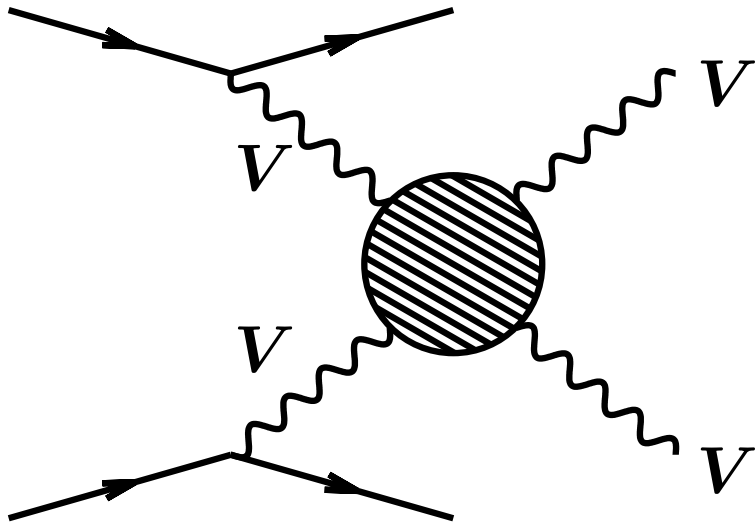


- EW  $W^+W^-jj$
- QCD  $W^+W^-jj$
- $Hjj$  via VBF,  $H \rightarrow WW$
- $t\bar{t} + \text{jets}$



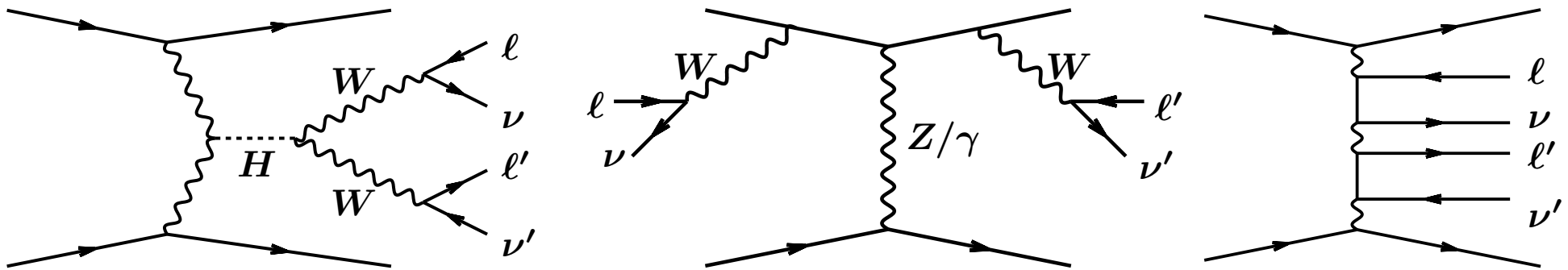
... today's background – tomorrow's signal ... ?

# vector boson scattering: $VV \rightarrow VV$



vector-boson scattering processes  
are extremely **sensitive to**  
**new interactions in the**  
**gauge boson sector**

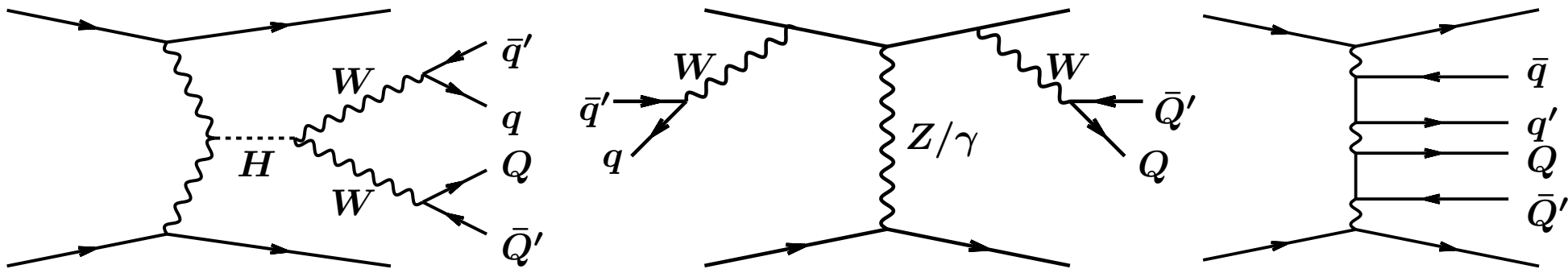
# $pp \rightarrow VVjj$ : vector boson scattering in the Standard Model



experiment: don't observe  $VVjj$  final state, but  
hadronic or leptonic decay products

4leptons +  $jj$   
low statistics  
clean signature

# $pp \rightarrow VVjj$ : vector boson scattering in the Standard Model



experiment: don't observe  $VVjj$  final state, but  
hadronic or leptonic decay products

4jets +  $jj$   
high statistics  
large backgrounds

4leptons +  $jj$   
low statistics  
clean signature

# EW $VVjj$ production in the Standard Model

need **stable, fast & flexible Monte Carlo program** allowing for

- ❖ computation of various jet and lepton observables for

VBF production of

$W^+W^-jj$ ,  $ZZjj$ ,  $W^\pm Zjj$ , and  $W^\pm W^\pm jj$

at NLO-QCD accuracy

(leptonic decay correlations fully taken into account)

- ❖ straightforward implementation of experimental selection cuts

- *G. Bozzi, C. Oleari, D. Zeppenfeld, B. J. (2006–2009)*

- *A. Denner, L. Hosekova, S. Kallweit (2012)*

# ingredients of the calculation

need to compute numerical value for ...

$$|\mathcal{M}_B|^2 = \left| \text{[diagram 1]} + \text{[diagram 2]} + \text{[diagram 3]} + \dots \right|^2$$

... Born amplitude squared in 4 dim

$$|\mathcal{M}_R|^2 = \left| \text{[diagram 1]} + \text{[diagram 2]} + \text{[diagram 3]} + \dots \right|^2$$

... real-emission amplitude squared in 4 dim and counter-terms for infrared-divergent configurations

almost 3000 diagrams → essential: organize calculation **economically!**



# virtual contributions

$$\mathcal{M}_V = \text{[diagram 1]} + \text{[diagram 2]} + \text{[diagram 3]} + \dots$$

$$= \mathcal{M}_B F(Q) \left[ -\frac{2}{\epsilon^2} - \frac{3}{\epsilon} \right] + \tilde{\mathcal{M}}_V^{finite}$$

determined numerically

[c. f. Denner, Dittmaier (2002,2005)]

**combination** of real emission, virtuals,  
and subtraction terms:  
poles canceled analytically → **finite** results

phase-space integration can be performed numerically (Vegas)

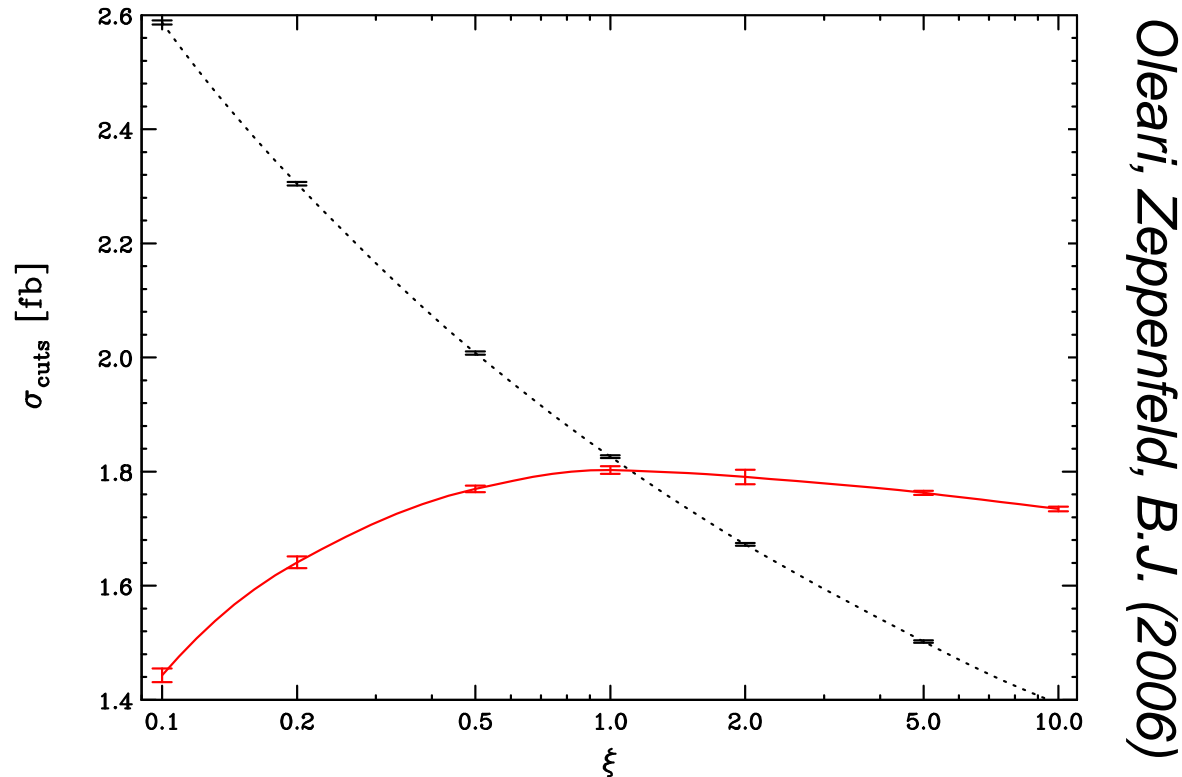
# implementation



... put everything into dedicated  
Monte-Carlo program VBFNLO ...

# EW $W^+W^-jj$ production: theoretical uncertainty

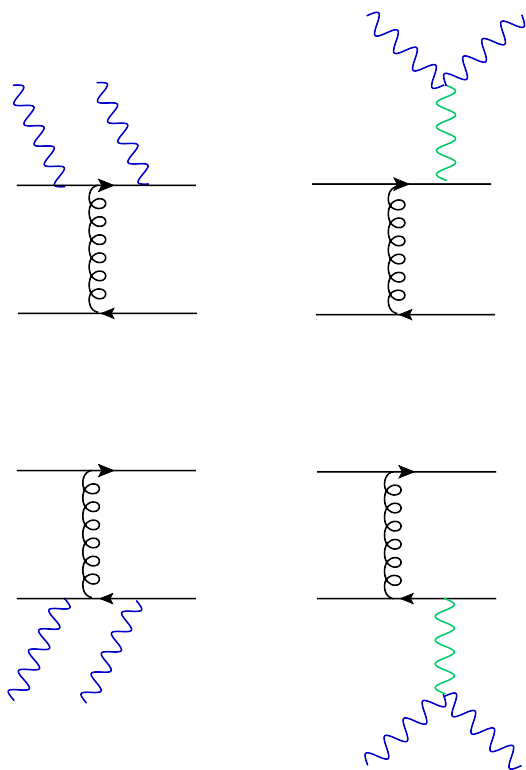
estimate theoretical uncertainty by studying dependence of cross section on unphysical scale parameter  $\mu = \xi M_W$



LO: no control on scale

NLO QCD: scale dependence strongly reduced

# QCD-induced $VVjj$ production



QCD-induced  $W^+W^-jj$  production  
constitutes irreducible background to

$$pp \rightarrow Hjj \rightarrow W^+W^-jj$$

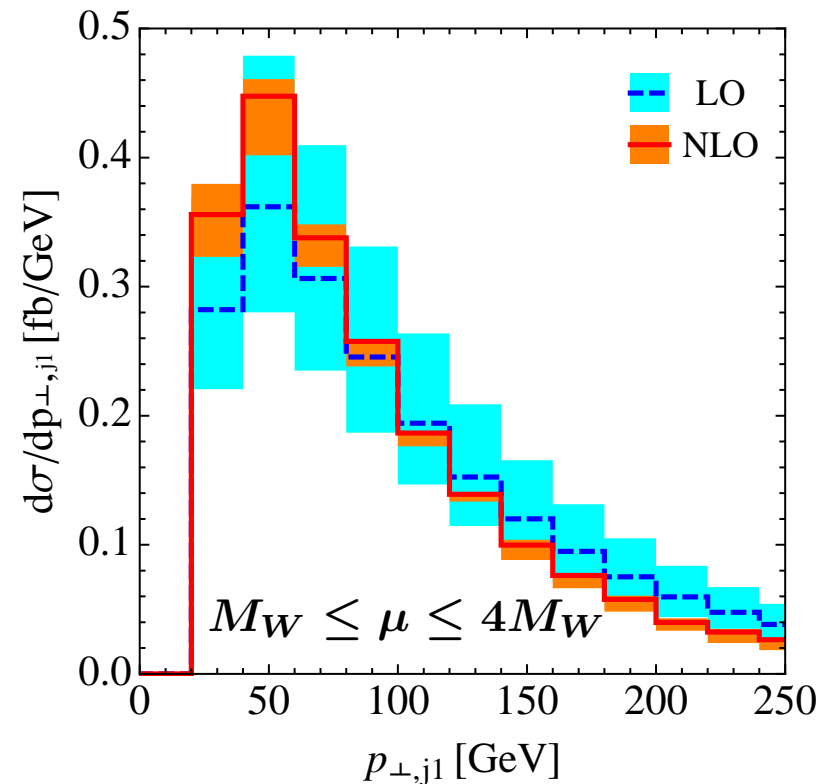
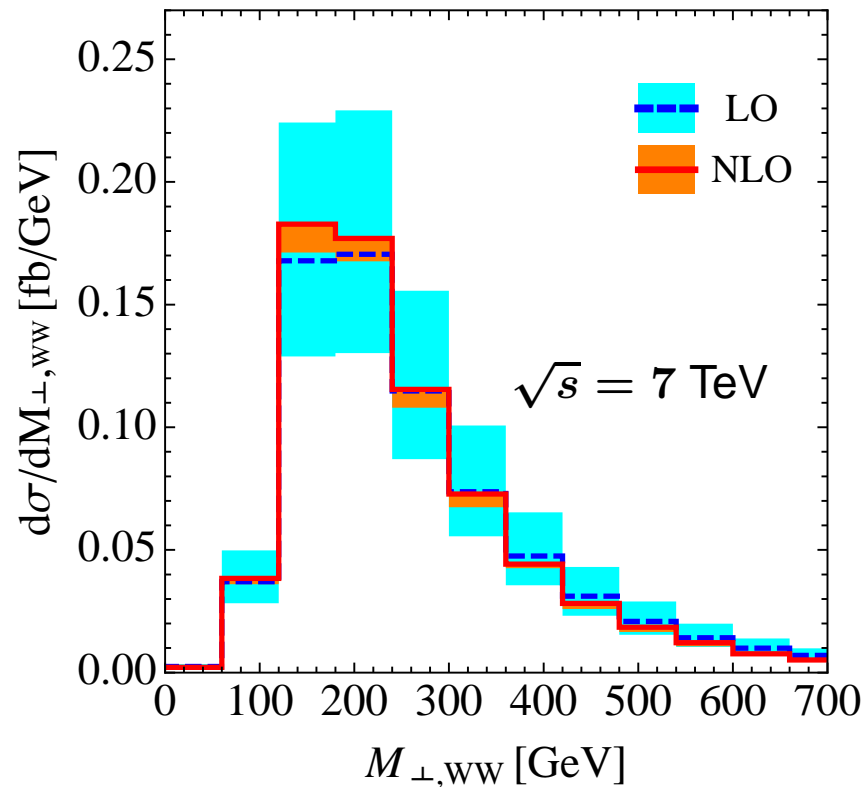
NLO-QCD predictions available

*Melia, Melnikov, Rontsch, Zanderighi (2011);*

*Greiner et al. (2012)*

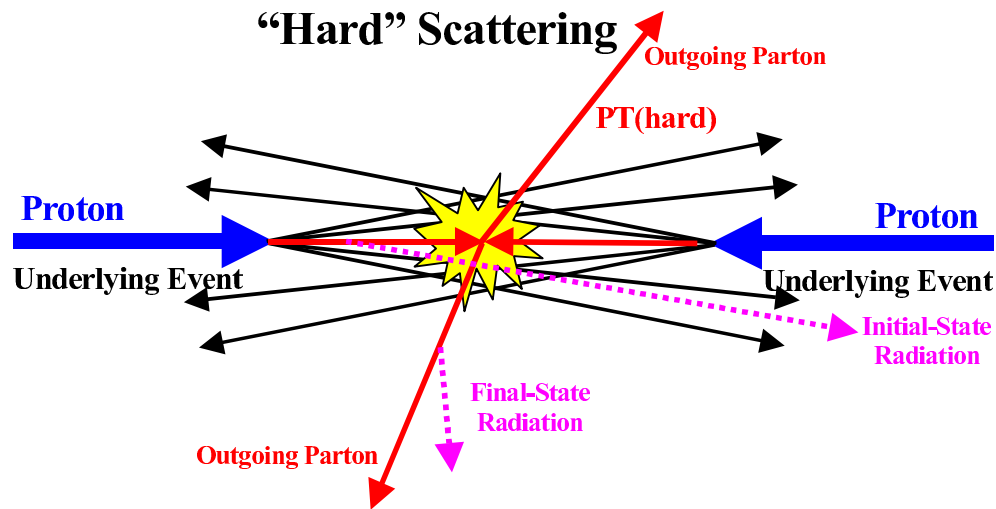
# QCD-induced $W^+W^-jj$ production at NLO

*Melia, Melnikov, Rontsch, Zanderighi (2011)*



NLO-QCD corrections significantly reduce  
scale uncertainty

# more realistic simulation

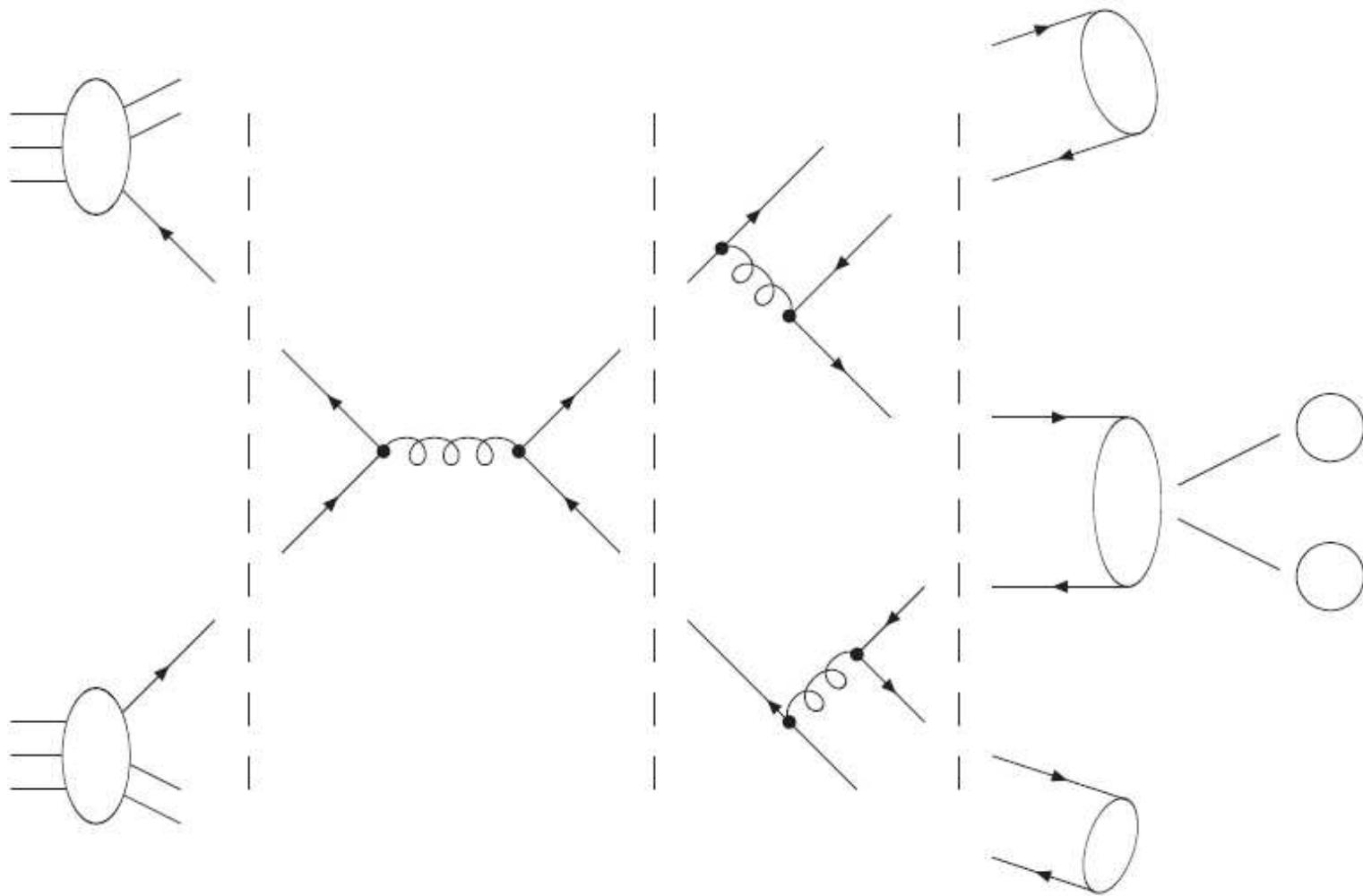


for realistic description of scattering processes at hadron colliders:

- ❖ combine matrix elements for hard scattering with programs for simulation of underlying event, parton shower, and hadronization

(PYTHIA, HERWIG, SHERPA, ...)

# stages of a hadronic collision



hard partonic  
scattering

$$\mu \sim Q \gg \Lambda_{\text{QCD}}$$

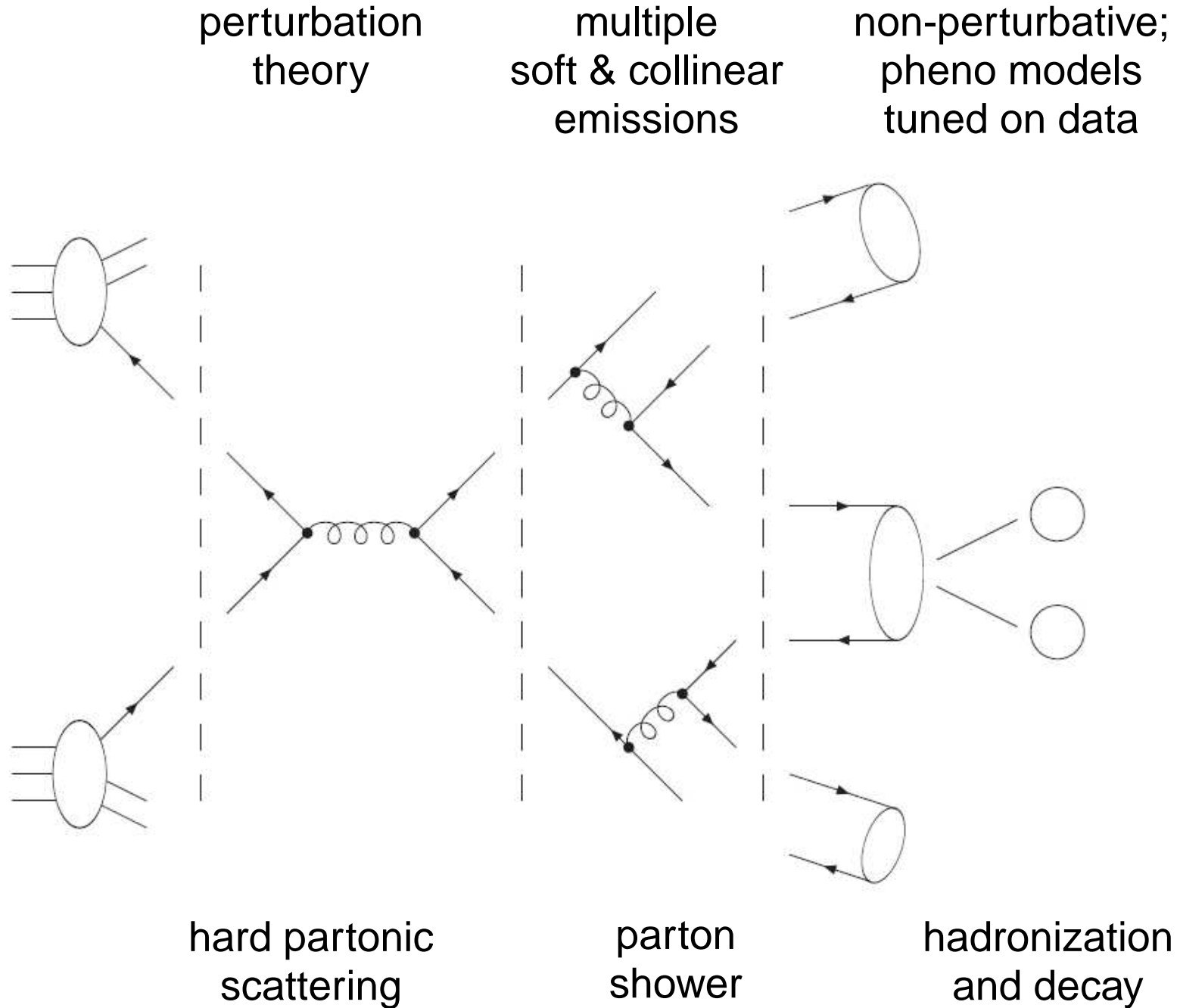
parton  
shower

$$Q > \mu > \Lambda_{\text{QCD}}$$

hadronization  
and decay

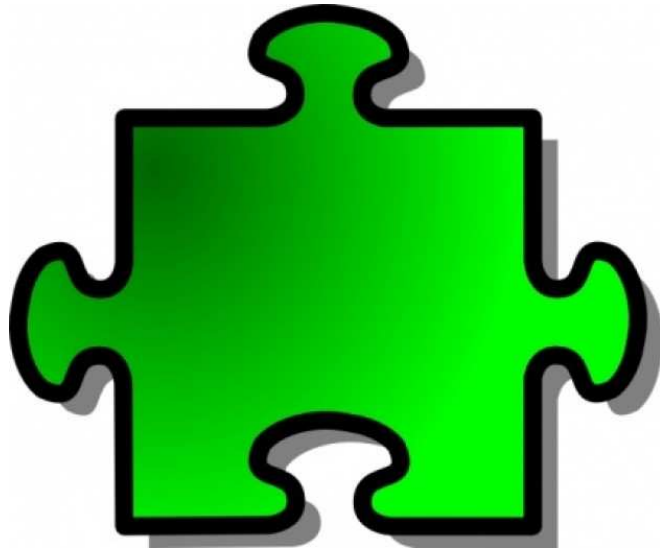
$$\mu \sim \Lambda_{\text{QCD}}$$

# stages of a hadronic collision





# realistic & precise predictions



exploit merits of flexible  
Monte Carlo tools



retain NLO accuracy  
for hard scattering



# NLO-QCD vs. Shower Monte Carlo

## NLO QCD:

- ✓ accurate shapes at high  $p_T$
- ✓ normalization accurate at NLO
- ✓ reduced scale dependence
- ✗ wrong shapes at low  $p_T$
- ✗ description only at parton level

## LO Shower Monte Carlo:

- ✗ bad description at high  $p_T$
- ✗ normalization accurate only at LO
- ✓ Sudakov suppression at low  $p_T$
- ✓ events at hadron level

☞ merge the two approaches, keeping the advantages of both:

- MC@NLO [*Frixione, Webber*]
- POWHEG [*Nason et al.*]

# parton showers & NLO-QCD: the POWHEG method

POsitive Weight Hardest Emission Generator

general prescription for **matching** parton-level **NLO-QCD**  
calculations with **parton shower programs**

*[Frixione, Nason, Oleari]*

- ❖ generate partonic event with single emission at NLO-QCD
- ❖ all subsequent radiation must be softer than the first one
- ❖ event is written on a file in standard Les Houches format
  - can be processed by default  
parton shower program  
(HERWIG, PYTHIA, ...)

# parton showers & NLO-QCD: the POWHEG method

POsitive W eight Hardest E mission G enerator

general prescription for **matching** parton-level **NLO-QCD**  
calculations with **parton shower programs**

*[Frixione, Nason, Oleari]*

- ❖ applicable to any  $p_T$ -ordered parton shower program
- ❖ no double counting of real-emission contributions
- ❖ produces events with positive weights
- ❖ tools for “do-it-yourself” implementation  
publicly available (the POWHEG-BOX)

*[Alioli, Nason, Oleari, Re]*

# NLO cross sections

reminder: differential **NLO cross section**

$$d\sigma_{\text{NLO}} = d\Phi_n \left\{ B(\Phi_n) + V(\Phi_n) + \left[ R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] d\Phi_r \right\}$$

Born
real emission and counter-terms

finite virtuals:
radiation phase space:

$$V_b(\Phi_n) + \int d\phi_r C(\Phi_n, \Phi_r)$$

$$d\Phi_r = dt dz d\phi$$

# shower Monte Carlo cross sections

leading order **shower Monte Carlo** cross section

Born

first emission  
(governed by  
splitting function  $P$ )

$$d\sigma_{\text{LO-SMC}} = d\Phi_n B(\Phi_n) \left\{ \Delta_{t_0} + \Delta_t \frac{\alpha_s}{2\pi} P(z) \frac{1}{t} d\Phi_r \right\}$$

Sudakov factor:

$$\Delta_t = \exp \left[ - \int d\Phi'_r \frac{\alpha_s}{2\pi} P(z') \frac{1}{t'} \theta(t' - t) \right]$$

... probability for no emission at scale  $t' > t$

# POWHEG cross sections

$$\bar{B} = \left\{ B(\Phi_n) + V(\Phi_n) + \int d\Phi_r \left[ R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] \right\}$$

$$d\sigma_{\text{POWHEG}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n, p_T^{\min}) + \Delta(\Phi_n, p_T) \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n, \Phi_r)} d\Phi_r \right\}$$

POWHEG “Sudakov” factor:

$$\Delta(\Phi_n, p_T) = \exp \left[ - \int d\Phi'_r \frac{R(\Phi_n, \Phi'_r)}{B(\Phi_n)} \theta(k_T(\Phi_n, \Phi'_r) - p_T) \right]$$

# the POWHEG cross section

$$d\sigma_{\text{NLO}} = d\Phi_n \left\{ B(\Phi_n) + V(\Phi_n) + \left[ R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] d\Phi_r \right\}$$

$$d\sigma_{\text{LO-SMC}} = d\Phi_n B(\Phi_n) \left\{ \Delta_{t_0} + \Delta_t \frac{\alpha_s}{2\pi} P(z) \frac{1}{t} d\Phi_r \right\}$$

$$d\sigma_{\text{POWHEG}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n, p_T^{\min}) \right. \\ \left. + \Delta(\Phi_n, p_T) \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n, \Phi_r)} d\Phi_r \right\}$$



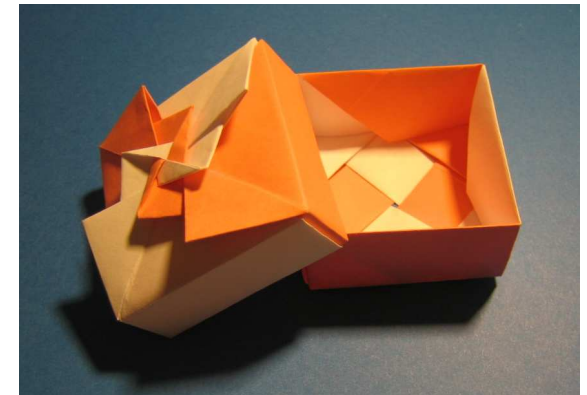
# parton showers & NLO-QCD: the POWHEG-BOX

- ✗ **user** has to supply process-specific quantities:
  - ❖ lists of flavor structures for Born and real emission processes
  - ❖ Born phase space
  - ❖ Born amplitudes squared, color-and spin-correlated amplitudes
  - ❖ real-emission amplitudes squared
  - ❖ finite part of the virtual corrections
  - ❖ Born color structure in the limit of a large number of colors
- ✓ all general, process-independent aspects of the matching are **provided by the POWHEG-BOX**

# parton showers & NLO-QCD: the POWHEG-BOX

up-to-date info on the POWHEG-BOX  
and code download:

<http://powhegbox.mib.infn.it/>



selected processes in the POWHEG-BOX:

- ❖  $Hjj$  production via VBF [Oleari, Nason (2009)]
- ❖  $Hjj$  production via gluon fusion [Campbell et al. (2012)]
- ❖ QCD  $W^+W^+jj$  production [Melia, Nason, Rontsch, Zanderighi (2011)]
- ❖ EW  $W^+W^+jj$  production [Zanderighi, B.J. (2011)]
- ❖ EW  $W^+W^-jj$  production [Zanderighi, B.J. (2013)]

# $pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

## QCD-induced production

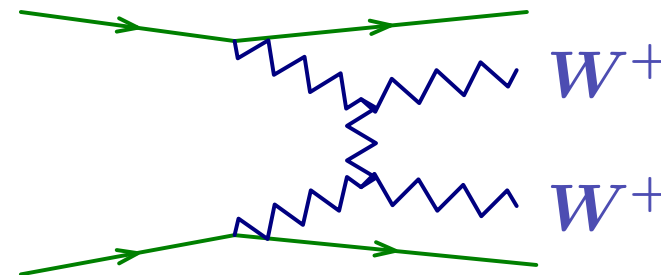
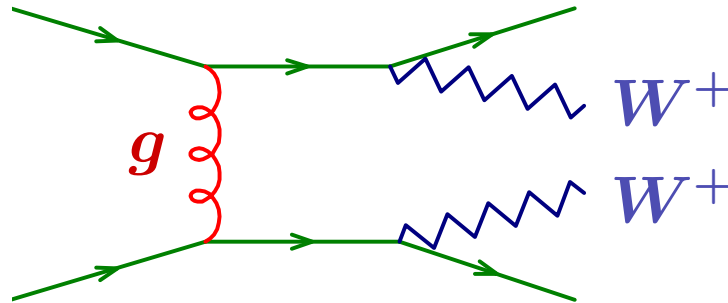
*Melia, Melnikov, Rontsch, Zanderighi (2010);*

*Melia, Nason, Rontsch, Zanderighi (2011)*

## EW production

*Oleari, Zeppenfeld, B.J. (2009);*

*Zanderighi, B.J. (2011)*



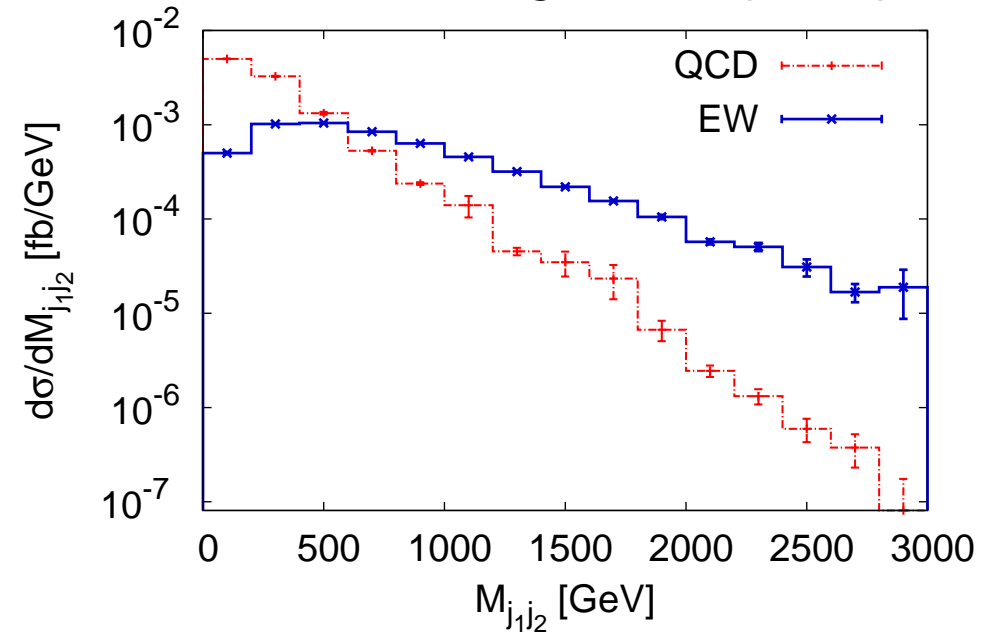
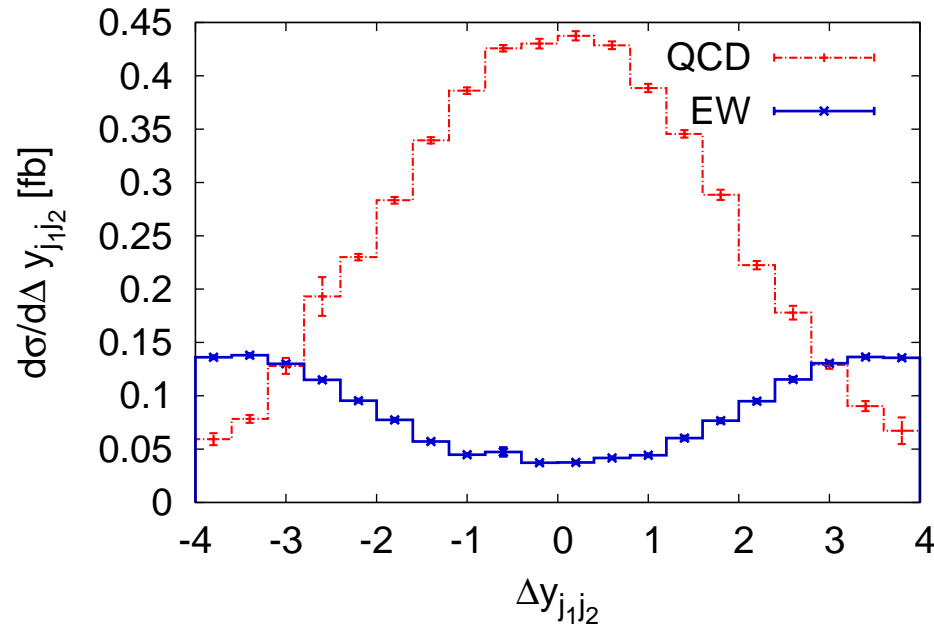
NLO-QCD results for  $\sqrt{s} = 7$  TeV with basic jet cuts only ( $p_T^{\text{tag}} > 20$  GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

# $pp \rightarrow W^+W^+jj$ : QCD versus EW production

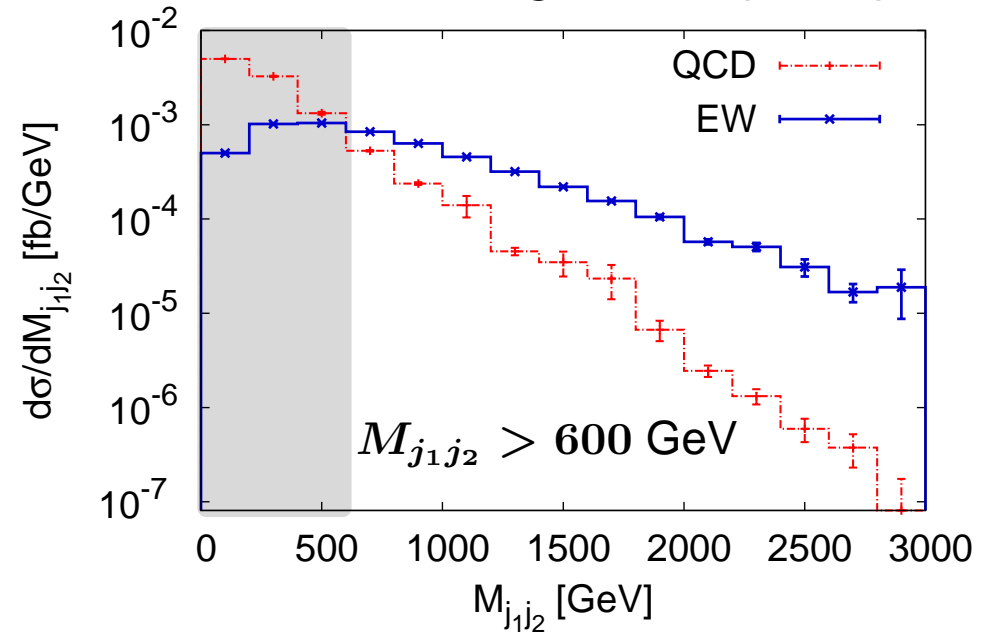
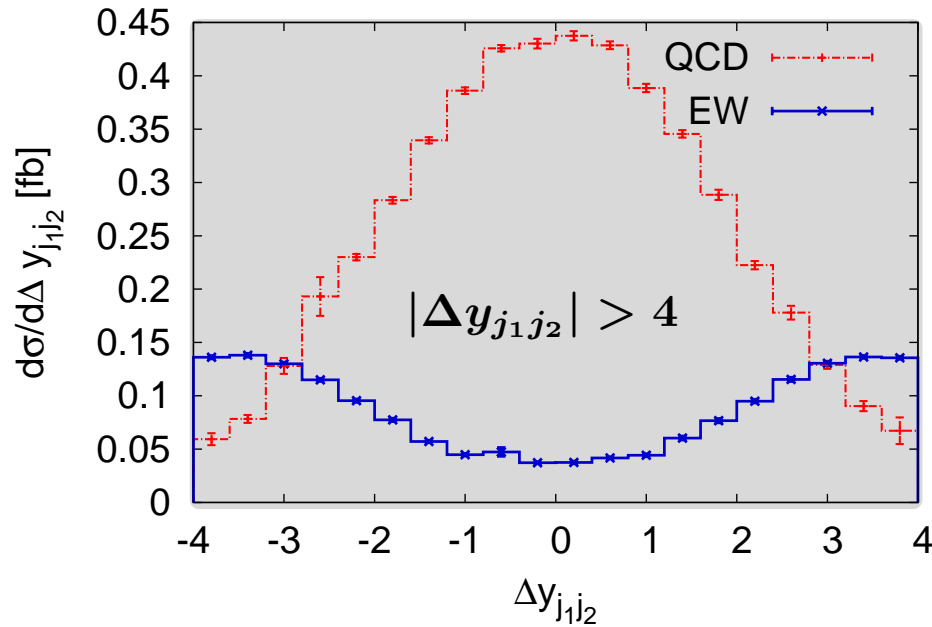
Zanderighi, B.J. (2011)



- $\sqrt{s} = 7$  TeV
- basic jet cuts only
- NLO-QCD accuracy

# $pp \rightarrow W^+W^+jj$ : QCD versus EW production

Zanderighi, B.J. (2011)

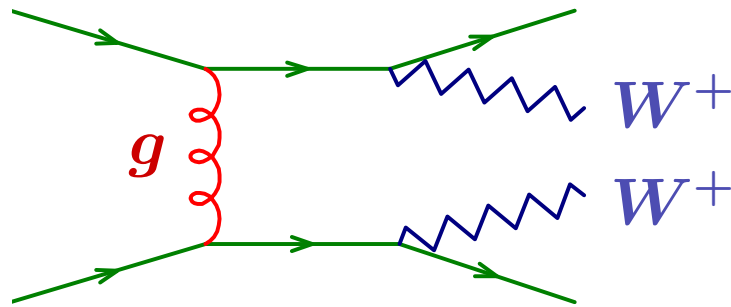


- $\sqrt{s} = 7 \text{ TeV}$
- basic jet cuts only
- NLO-QCD accuracy

# $pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

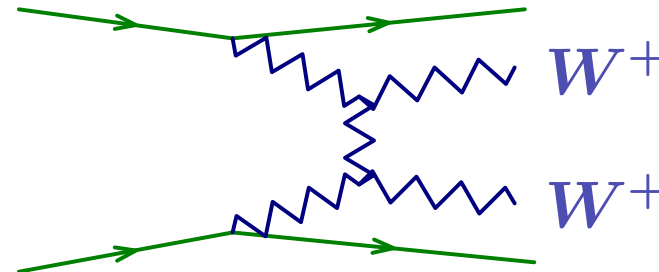
## QCD-induced production

*Melia, Melnikov, Rontsch, Zanderighi (2010);  
Melia, Nason, Rontsch, Zanderighi (2011)*



## EW production

*Oleari, Zeppenfeld, B.J. (2009);  
Zanderighi, B.J. (2011)*



NLO results for  $\sqrt{s} = 7$  TeV with basic jet cuts only ( $p_T^{\text{tag}} > 20$  GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

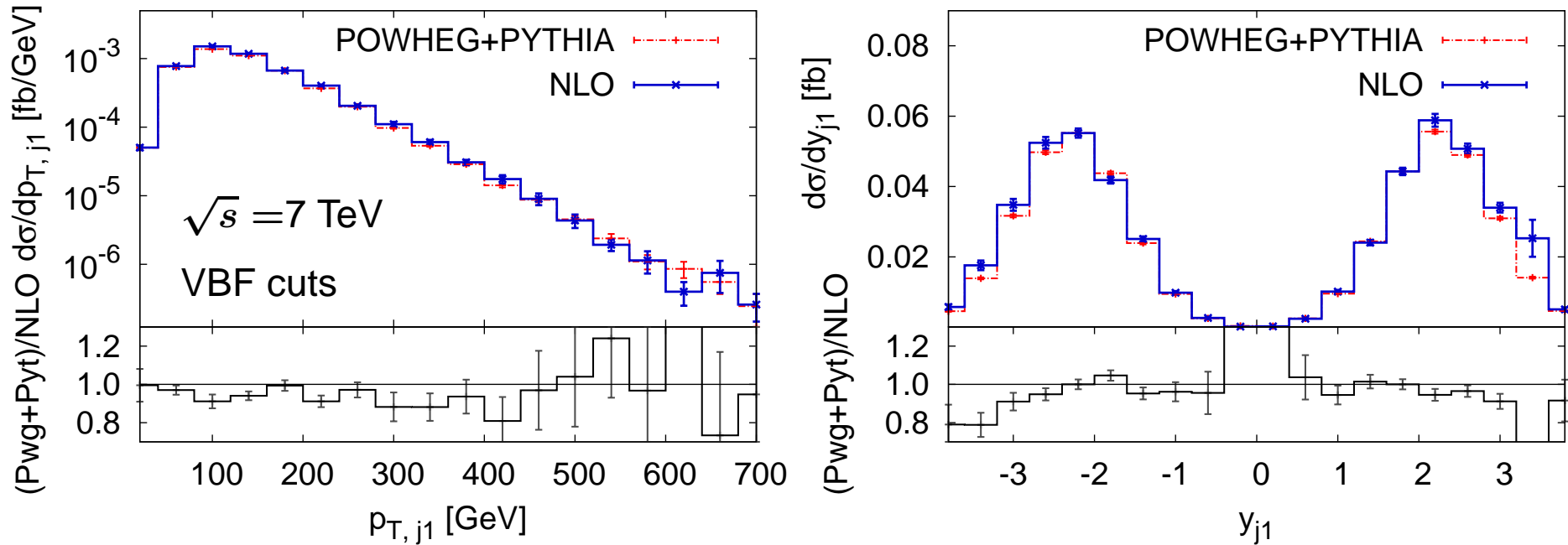
NLO results with VBF cuts:

$$\sigma_{\text{QCD}}^{\text{cuts}} = 0.0074 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{cuts}} = 0.201 \text{ fb}$$

# $pp \rightarrow W^+ W^+ jj$ in the POWHEG-BOX

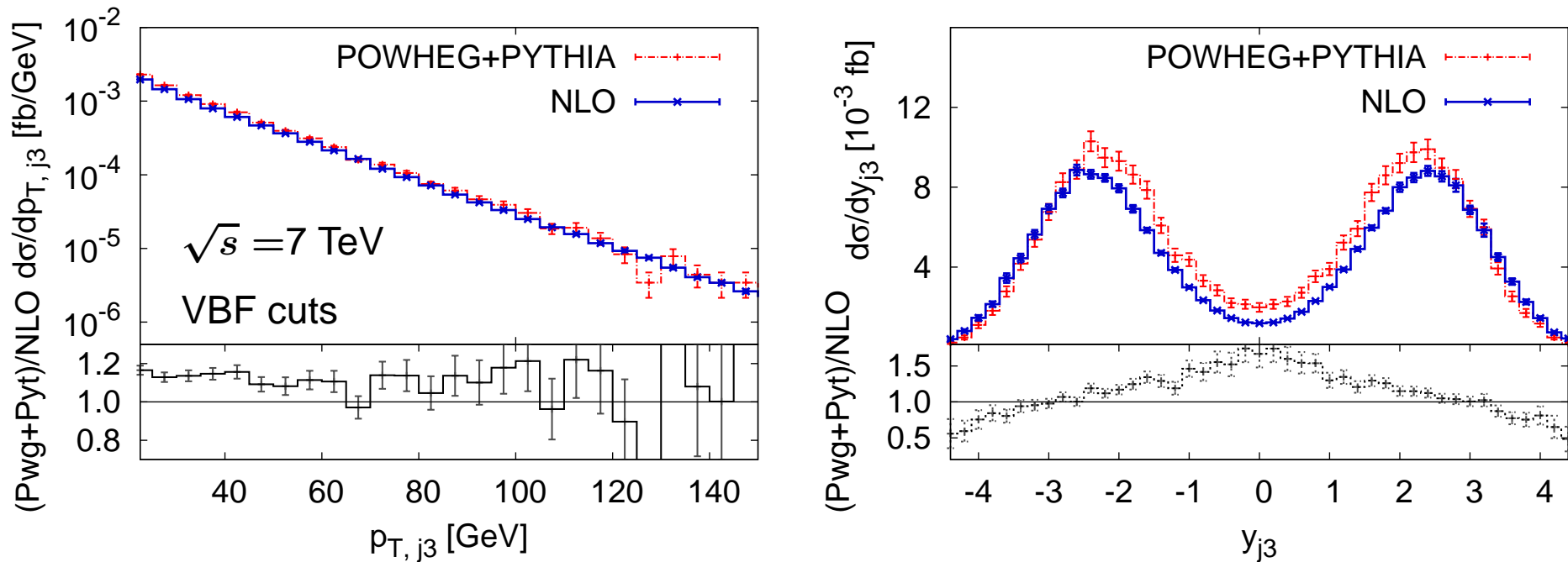
Zanderighi, B.J. (2011)



**good agreement** between parton-level NLO calculation and POWHEG matched with PYTHIA for many observables

# $pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

Zanderighi, B.J. (2011)



typical for VBF processes: little jet activity at central rapidities  
→ exploited by central-jet veto techniques

note: parton-shower effects slightly enhance central jet activity



the next step:  $pp \rightarrow W^+W^-jj$



# $pp \rightarrow W^+W^-jj$ in the POWHEG-BOX

full description of EW process  $pp \rightarrow W^+W^-jj$ ,  
including fully leptonic and semi-leptonic decays:

matching of hard matrix elements  
with parton shower at NLO QCD

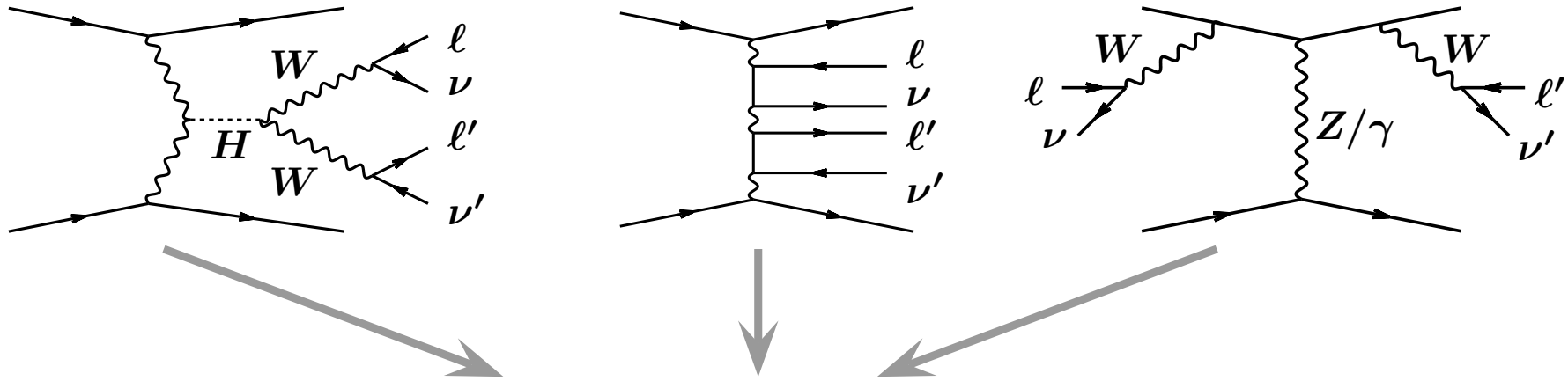
✓ provide implementation in versatile  
public program package POWHEG-BOX

✗ challenge: complex multi-leg process with  
involved resonance structure

→ conceptually and computationally demanding\*

\* requires about 12 hours  $\times$  100 nodes on a HPC cluster

# $pp \rightarrow W^+W^-jj$ : technicalities



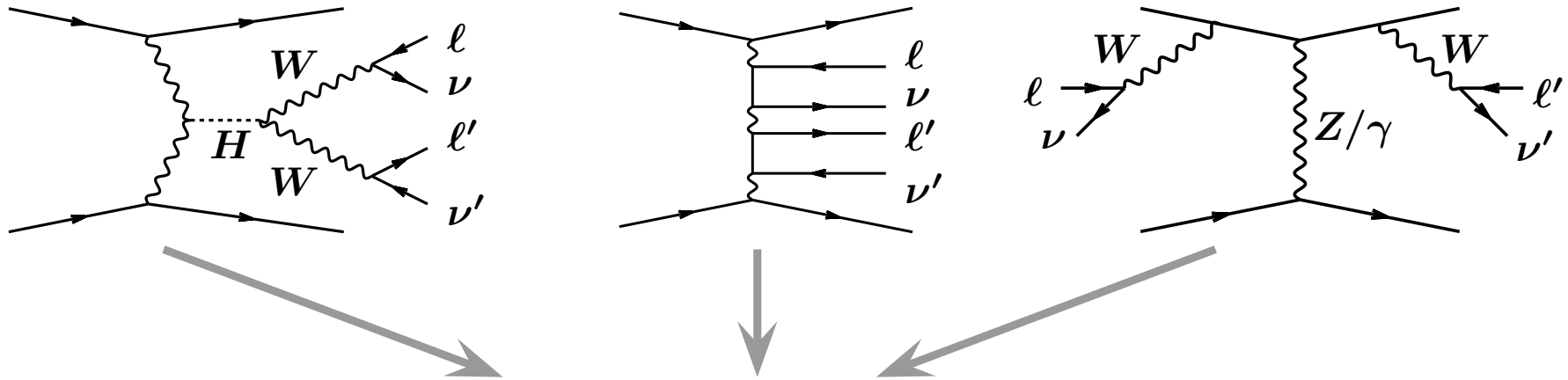
different topologies populate different regions in phase space

☞ split phase space into two regions for :

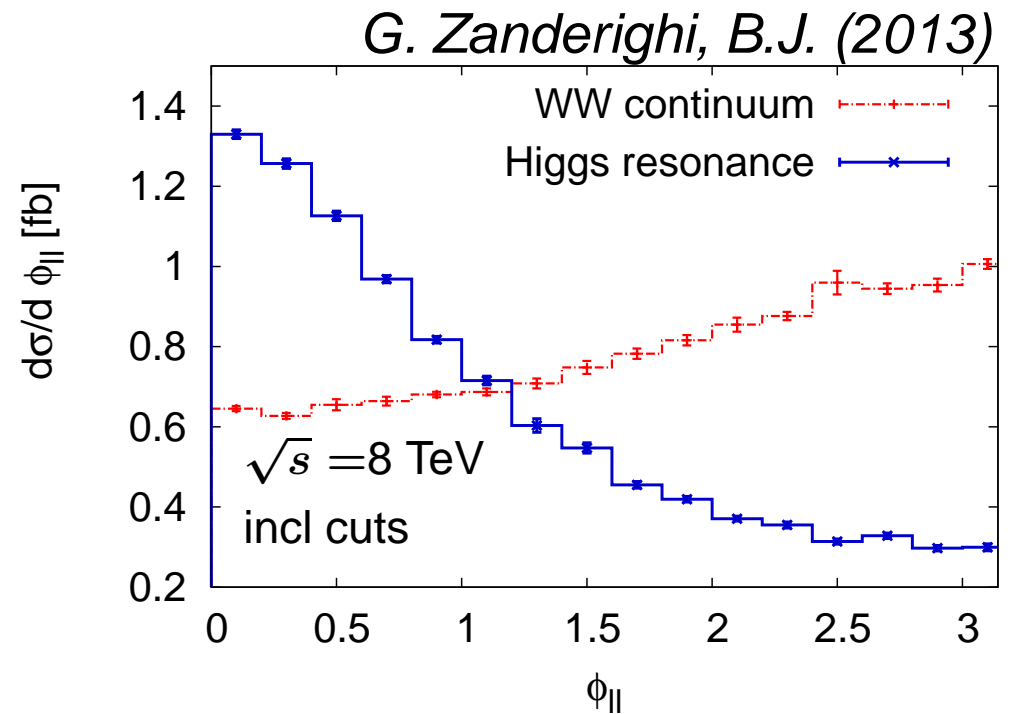
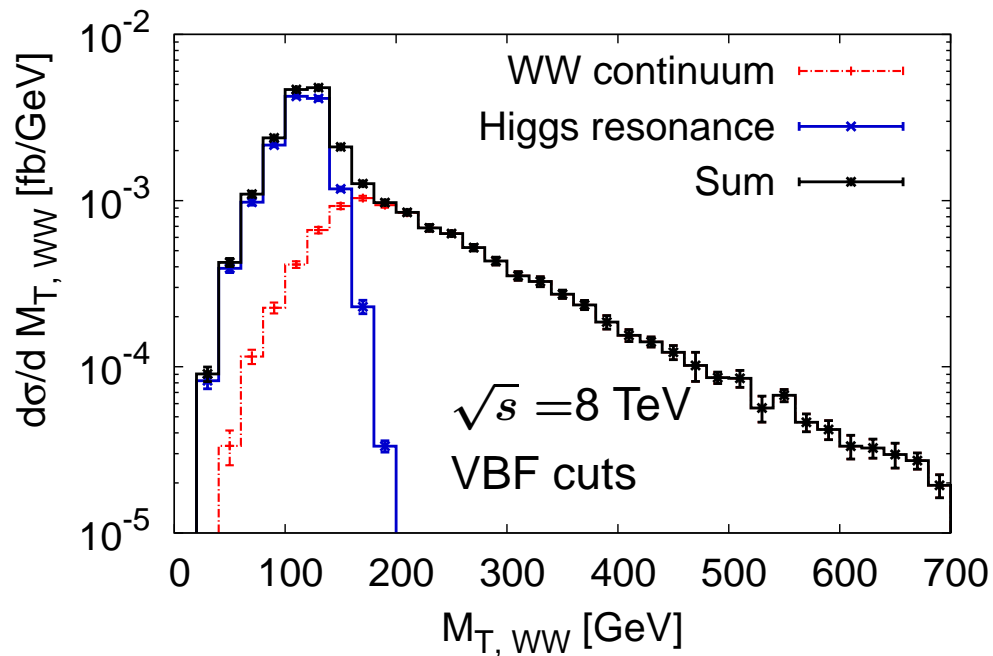
$$\blacklozenge M_H - \Delta M \leq M_{2\ell 2\nu} \leq M_H + \Delta M$$

☞ all other values of  $M_{2\ell 2\nu}$

# $pp \rightarrow W^+W^-jj$ : technicalities



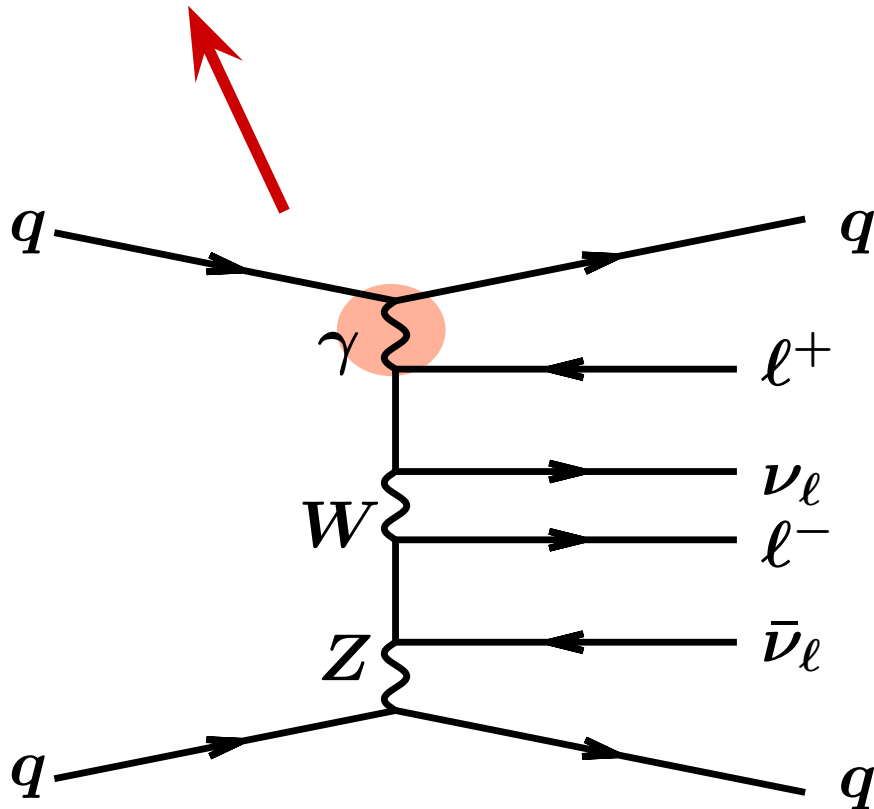
different topologies populate different regions in phase space:



G. Zanderighi, B.J. (2013)

# $pp \rightarrow W^+W^-jj$ : technicalities

photon propagator  $\sim 1/Q_\gamma^2$



need to handle

singularities for photons in  $t$ -channel

with  $Q_\gamma^2 \rightarrow 0$

(numerically irrelevant for meaningful observables)

(1) damping factor to effectively suppress matrix elements

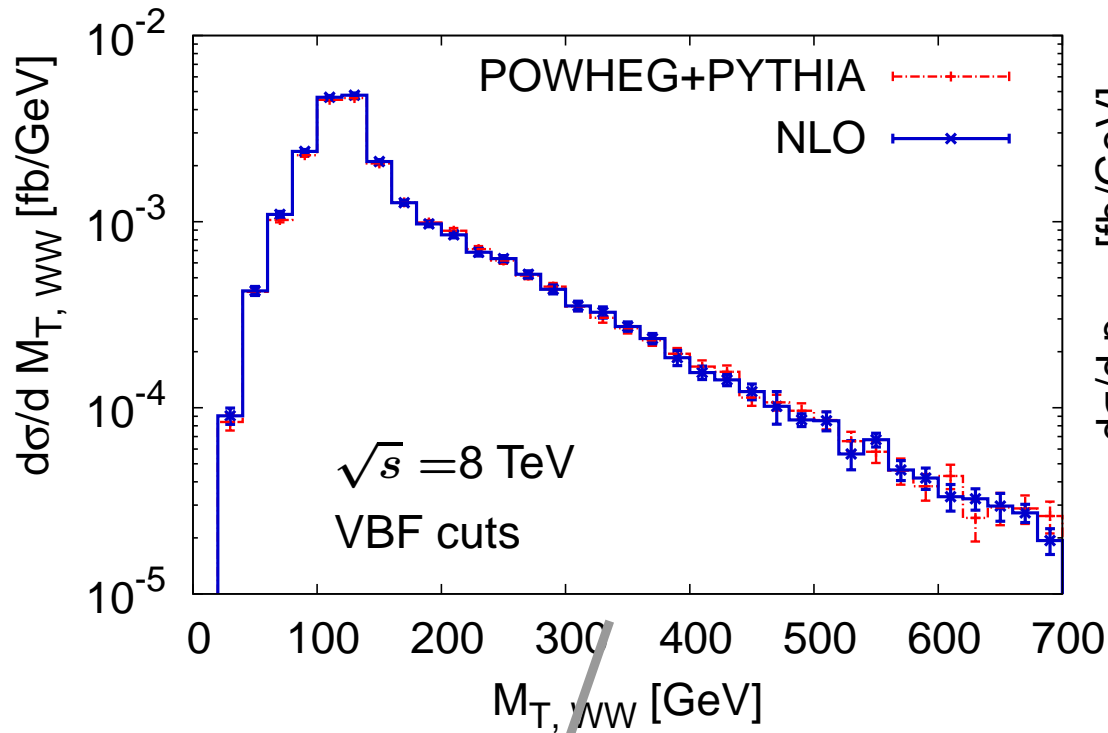
(2) Born-suppression factor to achieve efficient phase space integration

$$F \sim \left( \frac{p_{T,1}^2}{p_{T,1}^2 + \Lambda^2} \right)^2 \left( \frac{p_{T,2}^2}{p_{T,2}^2 + \Lambda^2} \right)^2$$

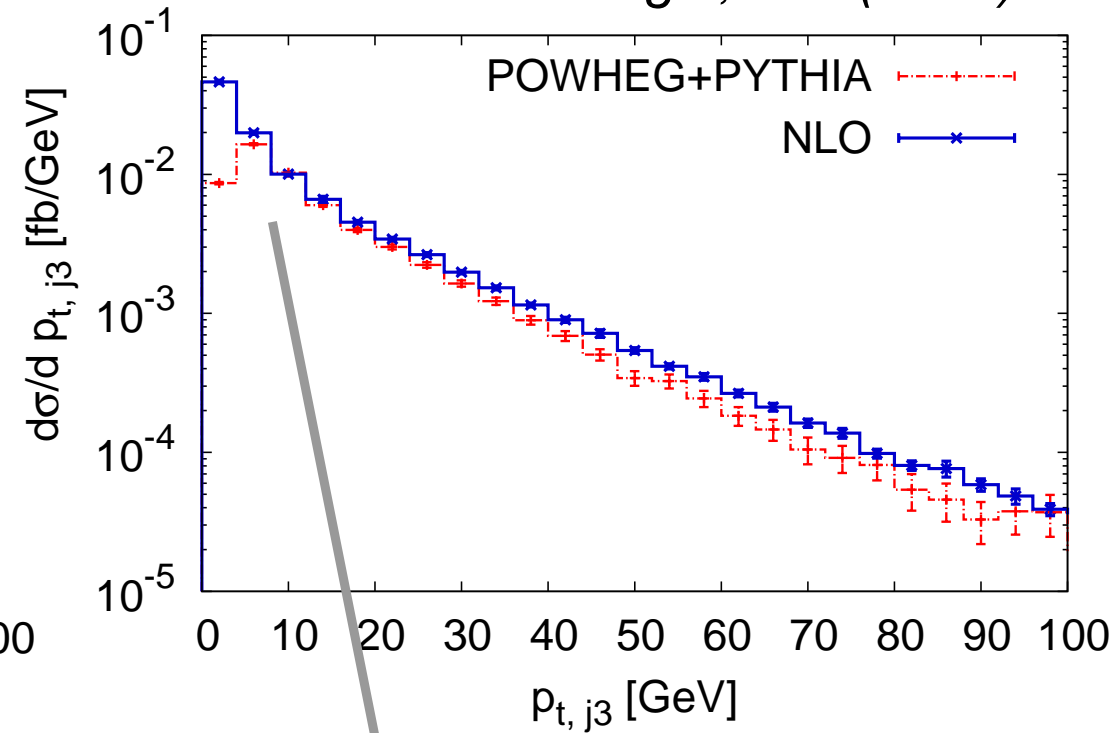
(alternative: explicit generation cuts)

# $pp \rightarrow W^+W^-jj$ with leptonic decays: results

G. Zanderighi, B.J. (2013)

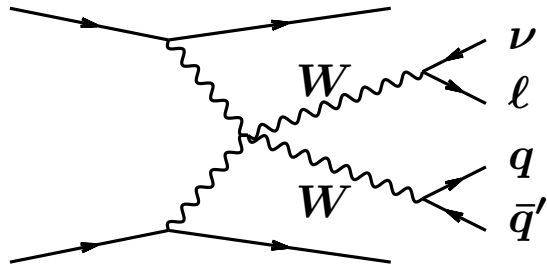


leptonic observables  
not very sensitive to  
parton shower



growth of jet distribution  
tamed by Sudakov factor

# $pp \rightarrow W^+ W^- jj$ with semi-leptonic decays



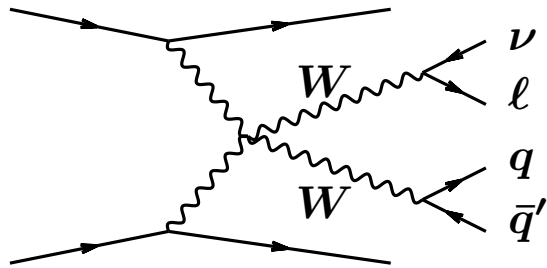
“semi-leptonic” final state:

$$W^+ W^- \rightarrow \ell \nu + q \bar{q}'$$

different from fully leptonic modes:

- ✓ branching ratio  $\text{BR}_{W \rightarrow q \bar{q}'} \approx 3 \times \text{BR}_{W \rightarrow \ell \nu} \rightarrow$  larger x-sec
- ✓ only one neutrino  $\rightarrow$  on-shell:  $M_{WW}$  reconstruction possible
- ✗ sophisticated analysis techniques needed to isolate signal

# $pp \rightarrow W^+W^-jj$ with semi-leptonic decays



consider fictitious scenario with heavy Higgs

$$m_H = 400 \text{ GeV} > 2M_W$$

→  $W$  bosons are typically on-shell

❖ require VBF topology for tagging jets:

$$p_{T,j}^{\text{tag}} > 25 \text{ GeV}, \quad |y_j^{\text{tag}}| < 4.5$$

$$\Delta y_{jj}^{\text{tag}} > 3, \quad m_{jj}^{\text{tag}} > 600 \text{ GeV}$$

❖ two decay jets have to be compatible with  $W$  decay

$$M_W - 10 \text{ GeV} \leq m_{jj}^{\text{dec}} \leq M_W + 10 \text{ GeV}$$



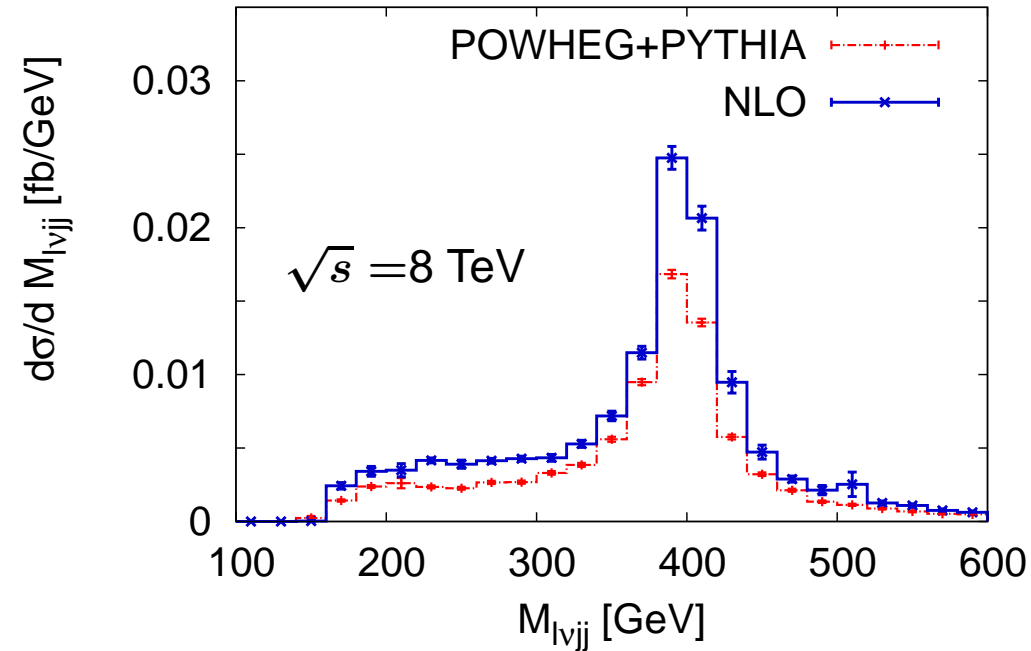
# $pp \rightarrow W^+W^-jj$ with semi-leptonic decays

- ◆ reconstruct  $M_{\ell\nu jj}$  using the assumption that

$$M_{\ell\nu} = M_W$$

( $\rightarrow$  neutrino momentum)

- ✗  $M_{\ell\nu jj}$  distribution very sensitive to parton-shower effects!

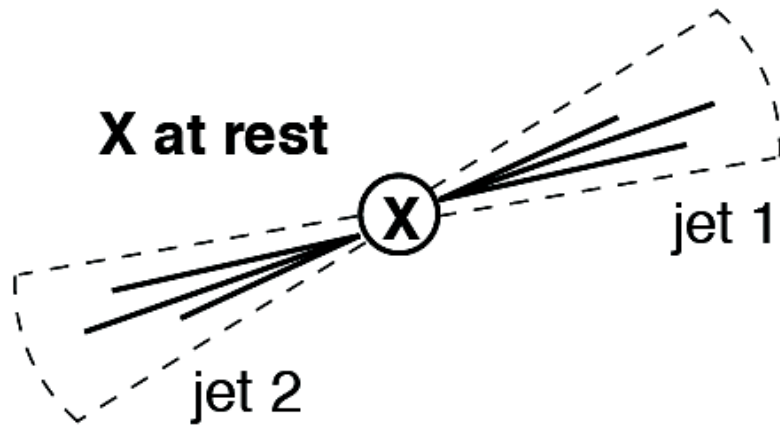


soft radiation smears distribution of  $W$  decay jets

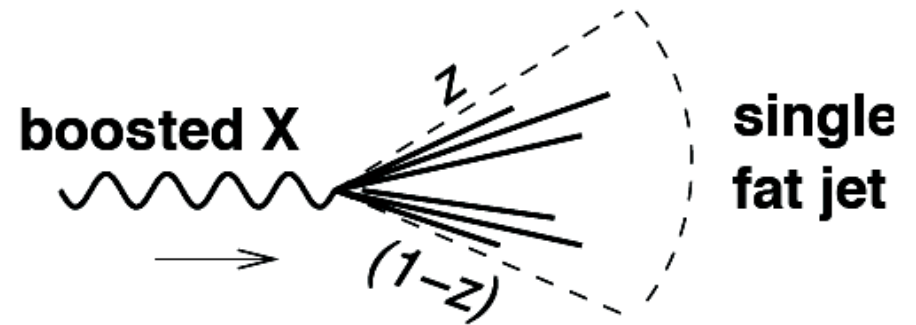
$\rightarrow m_{jj}^{\text{dec}} \sim M_W$  requirement no longer fulfilled

# boosted jet techniques

Normal analyses: two quarks from  $X \rightarrow q\bar{q}$  reconstructed as two jets



**High- $p_t$  regime: EW object X is boosted, decay is collimated,  $q\bar{q}$  both in same jet**



- ❖ pioneering work on  $WW$  scattering at the LHC

*Butterworth, Cox, Forshaw (2002)*

- ❖ break-through in  $pp \rightarrow VH$

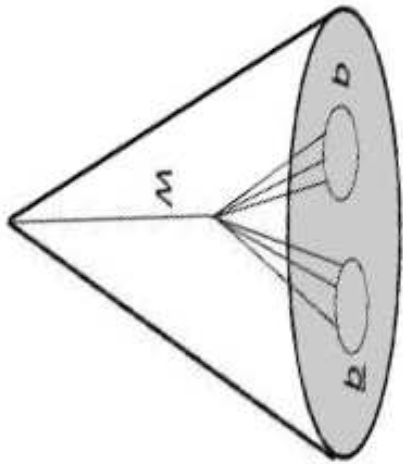
*Butterworth, Davison, Rubin, Salam (2008)*

- ❖ today: established field in its own

# $pp \rightarrow W^+W^-jj$ with semi-leptonic decays

$$pp \rightarrow W^+(q\bar{q}')W^-(\ell\nu)jj:$$

require a **highly boosted fat jet**  
with invariant mass close to  $M_W$



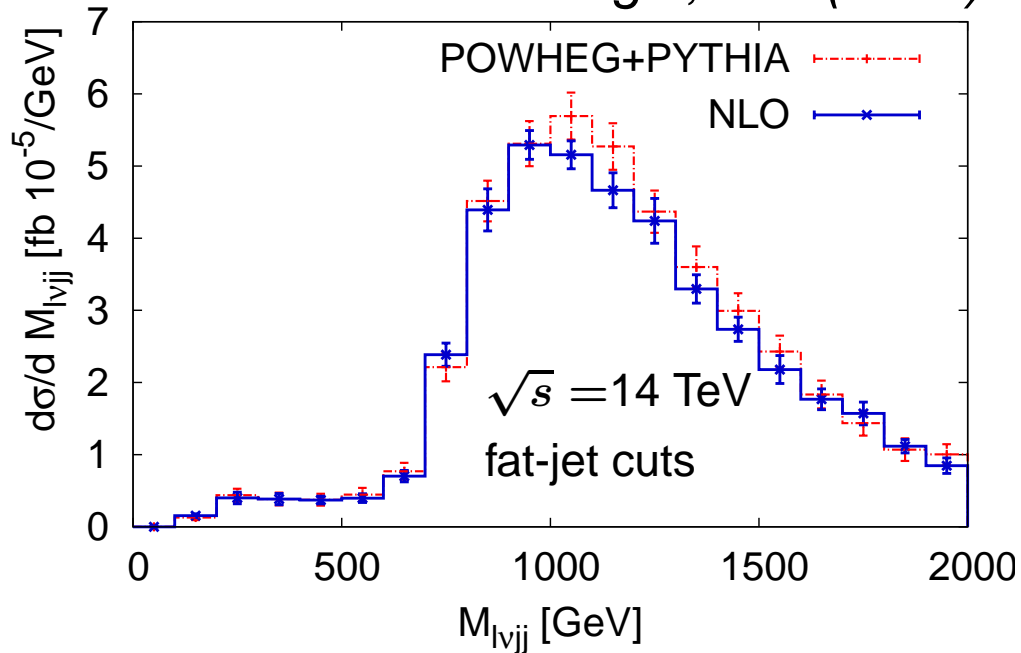
make use of jet properties / composition:

→ distinguish hadronically decaying  
heavy bosons  
from ordinary QCD jets

(stable against parton-shower effects)

# $pp \rightarrow W^+W^-jj$ with semi-leptonic decays

G. Zanderighi, B.J. (2013)



results stable against  
parton-shower effects

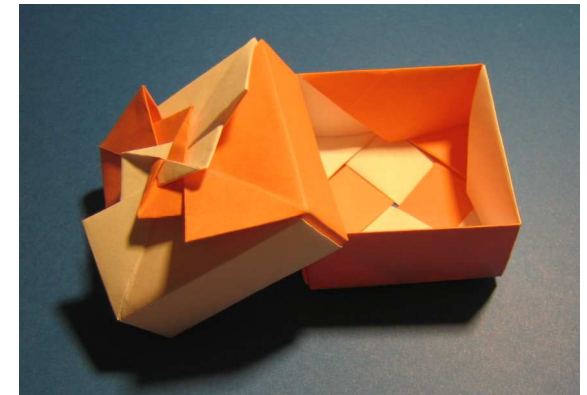
selection cuts  
specific for fat-jet analysis:

$$p_{T,J}^{\text{boosted}} > 300 \text{ GeV},$$
$$M_J \in (M_W \pm 10 \text{ GeV}),$$
$$p_{T,\ell} > 300 \text{ GeV}$$

cuts enforce highly energetic  
 $WW$  system  
(above light Higgs resonance)

# VBF in the POWHEG-BOX: getting started

- ❖ get access to a computing farm
- ❖ download the POWHEG-BOX from:  
`http://powhegbox.mib.infn.it/`
- ❖ go to the directory of the process you are interested in, e.g.,  
`$ cd POWHEG-BOX/VBF_Wp_Wm`
- ❖ for instructions on running the code refer to  
the documentation in `POWHEG-BOX/VBF_Wp_Wm/Docs`
- ❖ use sample files for input and analysis,  
or replace them with your own files



# summary

VBF crucial for understanding mechanism of electroweak symmetry breaking:

- \*  $Hjj$ : very clean Higgs production channel
- \*  $VVjj$ : sensitive to signatures of new physics in the gauge boson sector

important pre-requisites:

- ✓ explicit calculations revealed that VBF reactions are **perturbatively well-behaved** (NLO-QCD corrections and parton-shower effects moderate)

# summary

recent years have seen much progress on the theory side:

- ✓ precision calculations for  $VVjj$  processes
- ✓ tool development: public codes including
  - NLO-QCD corrections
  - parton-shower effects

... can develop their **full potential only**  
**if used by experimentalists ...**



...for your attention